

41. Suppose that a mass Δm of water is pumped in time Δt . The pump increases the potential energy of the water by Δmgh , where h is the vertical distance through which it is lifted, and increases its kinetic energy by $\frac{1}{2}\Delta mv^2$, where v is its final speed. The work it does is $\Delta W = \Delta mgh + \frac{1}{2}\Delta mv^2$ and its power is

$$P = \frac{\Delta W}{\Delta t} = \frac{\Delta m}{\Delta t} \left(gh + \frac{1}{2}v^2 \right) .$$

Now the rate of mass flow is $\Delta m/\Delta t = \rho_w Av$, where ρ_w is the density of water and A is the area of the hose. The area of the hose is $A = \pi r^2 = \pi(0.010 \text{ m})^2 = 3.14 \times 10^{-4} \text{ m}^2$ and $\rho_w Av = (1000 \text{ kg/m}^3)(3.14 \times 10^{-4} \text{ m}^2)(5.0 \text{ m/s}) = 1.57 \text{ kg/s}$. Thus,

$$\begin{aligned} P &= \rho Av \left(gh + \frac{1}{2}v^2 \right) \\ &= (1.57 \text{ kg/s}) \left((9.8 \text{ m/s}^2)(3.0 \text{ m}) + \frac{(5.0 \text{ m/s})^2}{2} \right) = 66 \text{ W} . \end{aligned}$$