

12. We note that r_A (the distance from the origin to sphere A , which is the same as the separation between A and B) is 0.5, $r_C = 0.8$, and $r_D = 0.4$ (with SI units understood). The force \vec{F}_k that the k^{th} sphere exerts on m_B has magnitude $Gm_k m_B / r_k^2$ and is directed from the origin towards m_k so that it is conveniently written as

$$\vec{F}_k = \frac{Gm_k m_B}{r_k^2} \left(\frac{x_k}{r_k} \hat{i} + \frac{y_k}{r_k} \hat{j} \right) = \frac{Gm_k m_B}{r_k^3} (x_k \hat{i} + y_k \hat{j}) .$$

Consequently, the vector addition (where k equals A, B and D) to obtain the net force on m_B becomes

$$\begin{aligned} \vec{F}_{\text{net}} &= \sum_k \vec{F}_k \\ &= Gm_B \left(\left(\sum_k \frac{m_k x_k}{r_k^3} \right) \hat{i} + \left(\sum_k \frac{m_k y_k}{r_k^3} \right) \hat{j} \right) \\ &= 3.7 \times 10^{-5} \hat{j} \text{ N} . \end{aligned}$$