83. (a) The impulse on the ball is

$$\vec{J} = \Delta \vec{p} = m\vec{v} - 0 = (46 \times 10^{-3} \text{ kg})(50 \text{ m/s})\hat{i} = (2.3 \text{ N} \cdot \text{s})\hat{i}$$

where we choose  $\hat{i}$  to be in the direction of the velocity  $\vec{v}$  of the ball as it leaves the club (at 30° above horizontal – so it is like the x axis of an inclined plane problem).

- (b) The impulse on the club is, by Newton's third law,  $\vec{J'} = -\vec{J} = -(2.3 \,\mathrm{N \cdot s})\hat{i}$ . We note that it is directed opposite to the direction of motion.
- (c) Using Eq. 10-8, the average force on the ball is

$$\vec{F}_{\text{avg}} = \frac{\vec{J}}{\Delta t} = \frac{(2.3)\hat{i}}{1.7 \times 10^{-3}} = 1400\,\hat{i}$$
 N .

(d) The work done on the ball is

$$W = \Delta K = \frac{1}{2}mv^2 = \frac{1}{2}(46 \times 10^{-3})(50)^2 = 58 \text{ J}.$$