

11. We take the magnitude of the force to be $F = At$, where A is a constant of proportionality. The condition that $F = 50\text{ N}$ when $t = 4.0\text{ s}$ leads to $A = (50\text{ N})/(4.0\text{ s}) = 12.5\text{ N/s}$. The magnitude of the impulse exerted on the object is

$$J = \int_0^{4.0} F \, dt = \int_0^{4.0} At \, dt = \frac{1}{2}At^2 \Big|_0^{4.0} = \frac{1}{2}(12.5)(4.0)^2 = 100\text{ N}\cdot\text{s} .$$

This equals the magnitude of the change in the momentum of the object (by the impulse-momentum theorem), and since the ball started from rest, we have $J = mv_f$. Therefore, $v_f = J/m = (100\text{ N}\cdot\text{s})/(10\text{ kg}) = 10\text{ m/s}$.