

38. Our notation (and, implicitly, our choice of coordinate system) is as follows: the mass of the original body is m ; its initial velocity is $\vec{v}_0 = v \hat{i}$; the mass of the less massive piece is m_1 ; its velocity is $\vec{v}_1 = 0$; and, the mass of the more massive piece is m_2 . We note that the conditions $m_2 = 3m_1$ (specified in the problem) and $m_1 + m_2 = m$ generally assumed in classical physics (before Einstein) lead us to conclude

$$m_1 = \frac{1}{4} m \quad \text{and} \quad m_2 = \frac{3}{4} m .$$

Conservation of linear momentum requires

$$\begin{aligned} m\vec{v}_0 &= m_1\vec{v}_1 + m_2\vec{v}_2 \\ mv\hat{i} &= 0 + \frac{3}{4} m \vec{v}_2 \end{aligned}$$

which leads to

$$\vec{v}_2 = \frac{4}{3} v \hat{i} .$$

The increase in the system's kinetic energy is therefore

$$\begin{aligned} \Delta K &= \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 - \frac{1}{2} m v_0^2 \\ &= 0 + \frac{1}{2} \left(\frac{3}{4} m \right) \left(\frac{4}{3} v \right)^2 - \frac{1}{2} m v^2 \\ &= \frac{1}{6} m v^2 . \end{aligned}$$