81. (a) During the final d = 12 m of motion, we use

$$K_1 + U_1 = K_2 + U_2 + f_k d \implies \frac{1}{2}mv^2 + 0 = 0 + 0 + f_k d$$

where v = 4.2 m/s. This gives  $f_k = 0.31$  N. Therefore, the thermal energy change is  $f_k d = 3.7$  J.

- (b) Using  $f_k = 0.31$  N we obtain  $f_k d_{\text{total}} = 4.3$  J for the thermal energy generated by friction; here,  $d_{\text{total}} = 14$  m.
- (c) During the initial d' = 2 m of motion, we have

$$K_0 + U_0 + W_{\text{app}} = K_1 + U_1 + f_k d' \implies 0 + 0 + W_{\text{app}} = \frac{1}{2}mv^2 + 0 + f_k d'$$

which essentially combines Eq. 8-31 and Eq. 8-29. This leads to the result  $W_{\text{app}} = 4.3$  J, and – reasonably enough – is the same as our answer in part (b).