

43. (a) We take the initial gravitational potential energy to be  $U_i = 0$ . Then the final gravitational potential energy is  $U_f = -mgL$ , where  $L$  is the length of the tree. The change is

$$U_f - U_i = -mgL = -(25 \text{ kg}) (9.8 \text{ m/s}^2) (12 \text{ m}) = -2.9 \times 10^3 \text{ J} .$$

- (b) The kinetic energy is

$$K = \frac{1}{2}mv^2 = \frac{1}{2}(25 \text{ kg})(5.6 \text{ m/s})^2 = 3.9 \times 10^2 \text{ J} .$$

- (c) The changes in the mechanical and thermal energies must sum to zero. The change in thermal energy is  $\Delta E_{\text{th}} = fL$ , where  $f$  is the magnitude of the average frictional force; therefore,

$$f = -\frac{\Delta K + \Delta U}{L} = -\frac{3.92 \times 10^2 \text{ J} - 2.94 \times 10^3 \text{ J}}{12 \text{ m}} = 210 \text{ N} .$$