

45. The free-body diagram (for the airplane of mass  $m$ ) is shown below. We note that  $\vec{F}_\ell$  is the force of aerodynamic lift and  $\vec{a}$  points rightwards in the figure. We also note that  $|\vec{a}| = v^2/R$  where  $v = 480 \text{ km/h} = 133 \text{ m/s}$ .

Applying Newton's law to the axes of the problem ( $+x$  rightward and  $+y$  upward) we obtain

$$\vec{F}_\ell \sin \theta = m \frac{v^2}{R}$$

$$\vec{F}_\ell \cos \theta = mg$$

where  $\theta = 40^\circ$ . Eliminating mass from these equations leads to

$$\tan \theta = \frac{v^2}{gR}$$

which yields  $R = v^2/g \tan \theta = 2.2 \times 10^3 \text{ m}$ .

