- 23. We adopt the positive direction choices used in the textbook so that equations such as Eq. 4-22 are directly applicable. The coordinate origin is throwing point (the stone's initial position). The x component of its initial velocity is given by $v_{0x} = v_0 \cos \theta_0$ and the y component is given by $v_{0y} = v_0 \sin \theta_0$, where $v_0 = 20$ m/s is the initial speed and $\theta_0 = 40.0^{\circ}$ is the launch angle.
 - (a) At $t = 1.10 \,\mathrm{s}$, its x coordinate is

$$x = v_0 t \cos \theta_0 = (20.0 \,\mathrm{m/s})(1.10 \,\mathrm{s}) \cos 40.0^\circ = 16.9 \,\mathrm{m}$$

(b) Its y coordinate at that instant is

$$y = v_0 t \sin \theta_0 - \frac{1}{2} g t^2 = (20.0 \,\mathrm{m/s})(1.10 \,\mathrm{s}) \sin 40^\circ - \frac{1}{2} (9.80 \,\mathrm{m/s}^2)(1.10 \,\mathrm{s})^2 = 8.21 \,\mathrm{m}$$
.

(c) At $t' = 1.80 \,\mathrm{s}$, its x coordinate is

$$x = (20.0 \,\mathrm{m/s})(1.80 \,\mathrm{s})\cos 40.0^{\circ} = 27.6 \,\mathrm{m}$$

(d) Its y coordinate at t' is

$$y = (20.0 \,\mathrm{m/s})(1.80 \,\mathrm{s}) \sin 40^{\circ} - \frac{1}{2} \left(9.80 \,\mathrm{m/s^2}\right) (1.80 \,\mathrm{s})^2 = 7.26 \,\mathrm{m}$$
.

(e) and (f) The stone hits the ground earlier than $t=5.0\,\mathrm{s}$. To find the time when it hits the ground solve $y=v_0t\sin\theta_0-\frac{1}{2}gt^2=0$ for t. We find

$$t = \frac{2v_0}{g} \sin \theta_0 = \frac{2(20.0 \,\mathrm{m/s})}{9.8 \,\mathrm{m/s}^2} \sin 40^\circ = 2.62 \;\mathrm{s} \;.$$

Its x coordinate on landing is

$$x = v_0 t \cos \theta_0 = (20.0 \,\mathrm{m/s})(2.62 \,\mathrm{s}) \cos 40^\circ = 40.2 \,\mathrm{m}$$

(or Eq. 4-26 can be used). Assuming it stays where it lands, its coordinates at $t=5.00\,\mathrm{s}$ are $x=40.2\,\mathrm{m}$ and y=0.