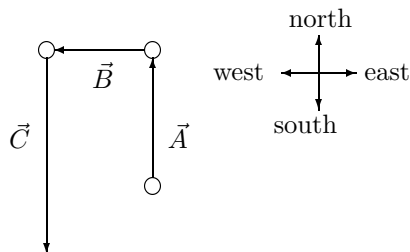


12. We label the displacement vectors \vec{A} , \vec{B} and \vec{C} (and denote the result

of their vector sum as \vec{r}). We choose *east* as the \hat{i} direction ($+x$ direction) and *north* as the \hat{j} direction ($+y$ direction). All distances are understood to be in kilometers. Therefore,



$$\begin{aligned}\vec{A} &= 3.1 \hat{j} \\ \vec{B} &= -2.4 \hat{i} \\ \vec{C} &= -5.2 \hat{j} \\ \vec{r} = \vec{A} + \vec{B} + \vec{C} &= -2.1 \hat{i} - 2.4 \hat{j}\end{aligned}$$

which means

that its magnitude is

$$|\vec{r}| = \sqrt{(-2.1)^2 + (-2.4)^2} \approx 3.2 \text{ km} .$$

and the two possibilities for its angle are

$$\tan^{-1} \left(\frac{-2.4}{-2.1} \right) = 41^\circ, \text{ or } 221^\circ .$$

We choose the latter possibility since \vec{r} is in the third quadrant. It should be noted that many graphical calculators have polar \leftrightarrow rectangular “shortcuts” that automatically produce the correct answer for angle (measured counterclockwise from the $+x$ axis). We may phrase the angle, then, as 221° counterclockwise from East (a phrasing that sounds peculiar, at best) or as 41° south from west or 49° west from south. The resultant \vec{r} is not shown in our sketch; it would be an arrow directed from the “tail” of \vec{A} to the “head” of \vec{C} .