

$$V = \int_0^{2\pi} \int_0^2 \int_{-\sqrt{9-R^2}}^{\sqrt{9-R^2}} 1 \cdot R dz dr d\theta = \int_0^{2\pi} \int_0^2 R [2\sqrt{9-R^2}] dr d\theta =$$

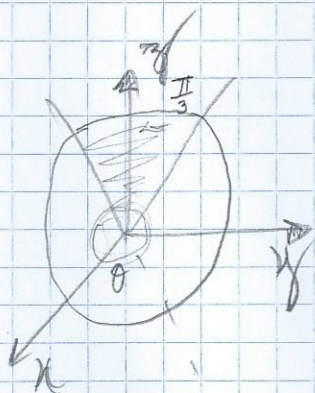
$$= \int_0^{2\pi} \left[\frac{-2(9-R^2)^{3/2}}{3/2} \right]_0^2 d\theta = \left[-\frac{2}{3} (9-4)^{3/2} + \frac{2}{3} (9-0)^{3/2} \right] 2\pi =$$

$$= \left[-\frac{2}{3} 5\sqrt{5} + \frac{2}{3} 3^3 \right] 2\pi$$

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9) Volume ? (com esféricos) do sólido limitado sup. $\rho=4$ e inf. por $\varphi = \frac{\pi}{3}$

$$\rho=4 \quad \rho^2=16 \quad x^2+y^2+z^2=16$$



$$\begin{cases} x = \rho \sin \varphi \cos \theta \\ y = \rho \sin \varphi \sin \theta \\ z = \rho \cos \varphi \end{cases} \quad \begin{matrix} 0 \leq \theta \leq 2\pi \\ 0 \leq \varphi \leq \pi/3 \\ 0 \leq \rho \leq 4 \end{matrix}$$

$$|\mathbf{r}| = \rho^2 \sin \varphi$$

$$V = \int_0^{2\pi} \int_0^{\pi/3} \int_0^4 \rho^2 \sin \varphi d\rho d\varphi d\theta =$$

$$= \int_0^{2\pi} \int_0^{\pi/3} \left[\frac{\rho^3}{3} \right]_0^4 \sin \varphi d\varphi d\theta = \int_0^{2\pi} \int_0^{\pi/3} \frac{4^3}{3} \sin \varphi d\varphi d\theta =$$

$$= \frac{4^3}{3} \int_0^{2\pi} \left[-\cos \varphi \right]_0^{\pi/3} d\theta = \frac{4^3}{3} \left(-\frac{1}{2} + 1 \right) 2\pi = \frac{4^3}{3} \frac{1}{2} 2\pi = \frac{64}{3} \pi$$