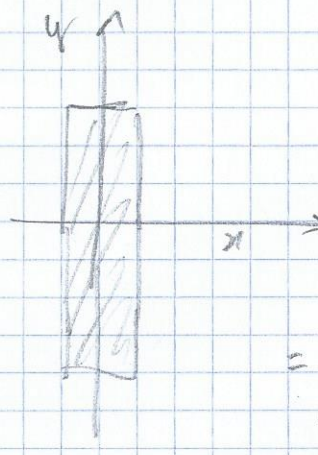


Intégrale double

- 1) Calculer $\iint_R 4xy^3 \, dA$ sur $R = \{(x,y) \in \mathbb{R}^2 : -1 \leq x \leq 1 \wedge -2 \leq y \leq 2\}$



$$\begin{aligned} \int_{-1}^1 \left[\int_{-2}^2 4xy^3 \, dy \right] dx &= \int_{-1}^1 4x \int_{-2}^2 y^3 \, dy \, dx = \\ &= \int_{-1}^1 4x \left[\frac{y^4}{4} \right]_{-2}^2 dx = \int_{-1}^1 x(2^4 - (-2)^4) dx = 0 \end{aligned}$$

- 2) $\iint_R x \sqrt{1-x^2} \, dA$ $R = \{(x,y) \in \mathbb{R}^2 : 0 \leq x \leq 1 \wedge 2 \leq y \leq 3\}$

$$\begin{aligned} \int_0^1 \left(\int_2^3 x \sqrt{1-x^2} \, dy \right) dx &= \int_0^1 x \sqrt{1-x^2} [y]_2^3 dx = \\ &= (3-2) \left(-\frac{1}{2} \right) \int_0^1 -2x \sqrt{1-x^2} dx = -\frac{1}{2} \left[\frac{(1-x^2)^{\frac{1}{2}+1}}{\frac{1}{2}+1} \right]_0^1 = \end{aligned}$$

$$\begin{aligned} \text{Area} &= \iint 1 \, dA \\ u &= 1-x^2 \\ u' &= -2x \end{aligned} \quad \left| \quad = -\frac{1}{2} \times \frac{2}{3} \left[(1-x^2)^{3/2} \right]_0^1 = -\frac{1}{3} [0-1] = \frac{1}{3} \right.$$

$$\left(\sqrt{\sin^2 x + 8e^x} \right)' = \left((\sin^2 x + 8e^x)^{\frac{1}{2}} \right)' = \frac{1}{2} (\sin^2 x + 8e^x)^{-\frac{1}{2}} \cdot (2 \sin x \cos x + 8e^x)$$