Interactive Data Visualization

07

Visualization Techniques Multivariate Data



Notice

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Table of Contents

Introduction

Point-Based Techniques

Line-Based Techniques

Region-Based Techniques

Combinations of Techniques

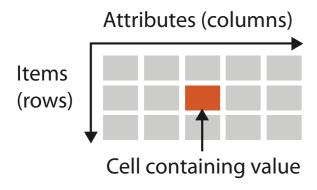
Interactive Data Visualization

Introduction

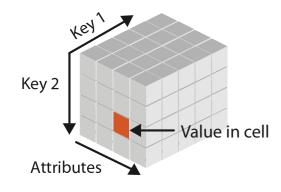


Dataset Types: Table

→ Tables



→ Multidimensional Table



Α	В	С	S	T	U
Order ID	Order Date	Order Priority	Product Container	Product Base Margin	Ship Date
3	10/14/06	5-Low	Large Box	0.8	10/21/06
6	2/21/08	4-Not Specified	Small Pack	0.55	2/22/08
32	7/16/07		Small Pack	0.79	7/17/07
32	7/16/07	2-High	Jumbo Box	•1	7/17/07
32	7/16/07	2-High	Medium Box	attribute	7/18/07
32	7/16/07	2-High	Medium Box	0.03	7/18/07
35	10/23/07	4-Not Specified	Wrap Bag	0.52	10/24/07
35		4-Not Specified	Small Box	0.58	10/25/07
36	11/3/07	1-Urgent	Small Box	0.55	11/3/07
65		1-Urgent	Small Pack	0.49	3/19/07
66	1 (20 (05	5-Low	Wrap Bag	0.56	1/20/0
69	litem 5	4-Not Specified	Small Pack	0.44	6/6/0
69		4-Not Specified	Wrap Bag	0.6	6/6/0
70	12/18/06		Small Box	0.59	12/23/0
70	12/18/06	5-Low	Wrap Bag	0.82	12/23/06
96	4/17/05	2-High	Small Box	0.55	4/19/0
97	1/29/06	3-Medium	Small Box	0.38	1/30/0
129	11/19/08	5-Low	Small Box	0.37	11/28/0
130	5/8/08	2-High	Small Box	0.37	5/9/0
130	5/8/08	2-High	Medium Box	0.38	5/10/08
130	5/8/08	2-High	Small Box	0.6	5/11/08
132	6/11/06	3-Medium	Medium Box	0.6	6/12/0
132	6/11/06	3-Medium	Jumbo Box	0.69	6/14/0
134	5/1/08	4-Not Specified	Large Box	0.82	5/3/08
135		4-Not Specified	Small Pack	0.64	10/23/07
166	9/12/07		Small Box	0.55	9/14/07
193		1-Urgent	Medium Box	0.57	8/10/06
194		3-Medium	Wrap Bag	0.42	4/7/08

A multidimensional table has a more complex structure for indexing into a cell, with multiple keys.

Tamara Munzner



Multivariate Data

- Data that does not generally have an explicit spatial attribute
- **Point-Based Techniques**
 - Project records from an n-dimensional data space to an arbitrary k-dimensional display space, such that data records map to k-dimensional points. (e.g. Scatterplots)
- **Line-Based Techniques**
 - Points corresponding to a particular record or dimension are linked together with straight or curved lines. (e.g. Line Graphs, Parallel Coordinates)
- **Region-Based Techniques**
 - Filled polygons are used to convey values, based on their size, shape, color, or other attributes. (e.g. Bar Charts/Histograms)



Interactive Data Visualization

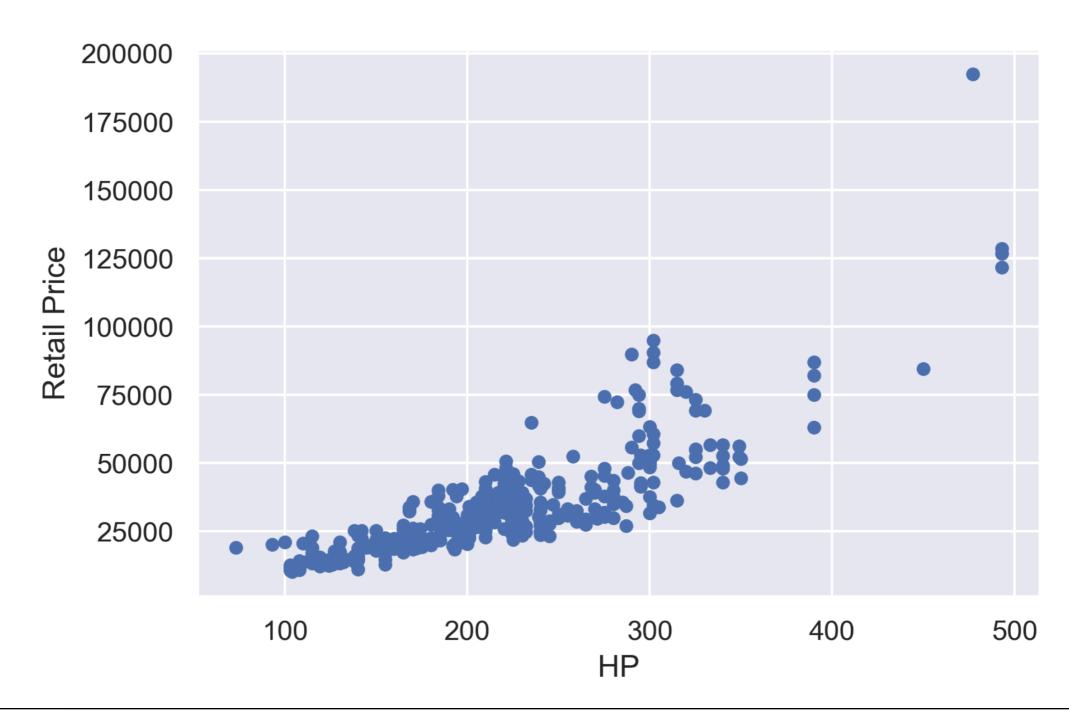
Point-Based Techniques



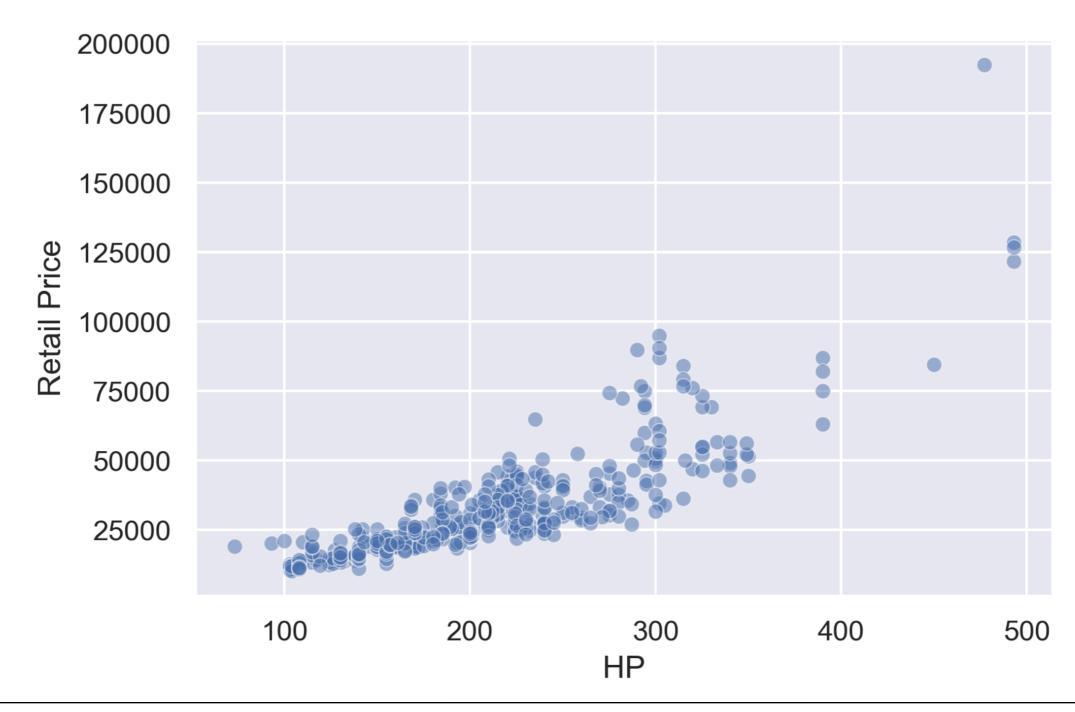
- **Scatterplots and Scatterplot Matrices**
 - Their success stems from our innate abilities to judge relative position within a bounded space

- As the dimensionality of the data increases, the choices for visual analysis consist of:
 - dimension subsetting (user selection or algorithm based suggestion);
 - dimension embedding (mapping dimensions to other graphical attributes besides position, such as color, size, and shape);
 - multiple displays (either superimposed or juxtaposed e. g. scatterplot matrix);
 - dimension reduction (to transform the high-dimensional data to data of lower dimension).





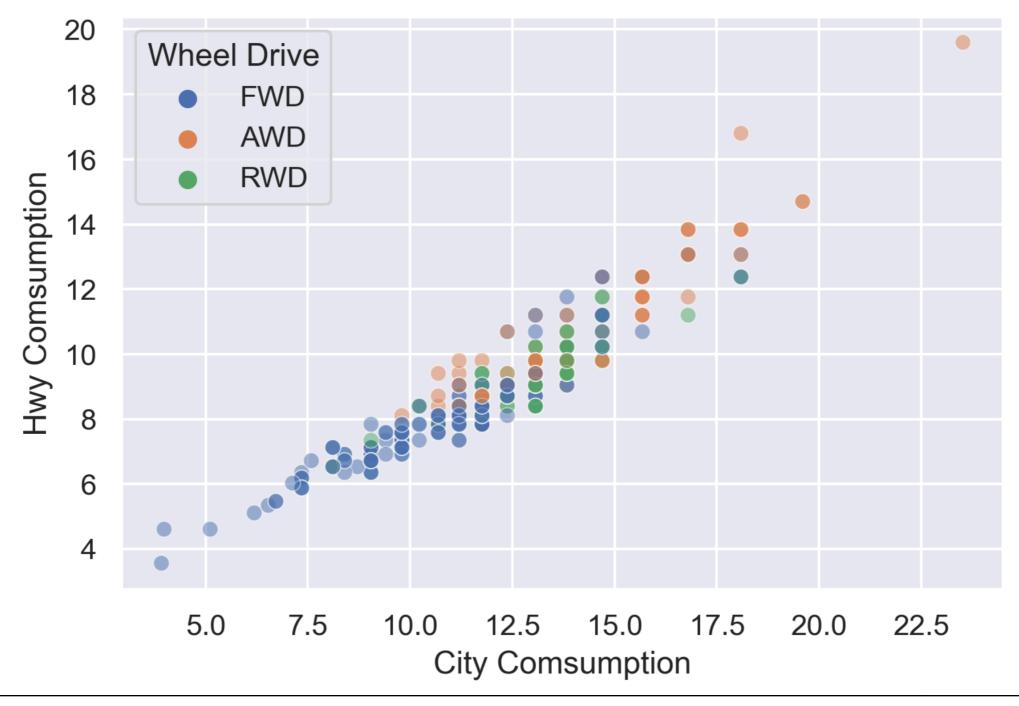




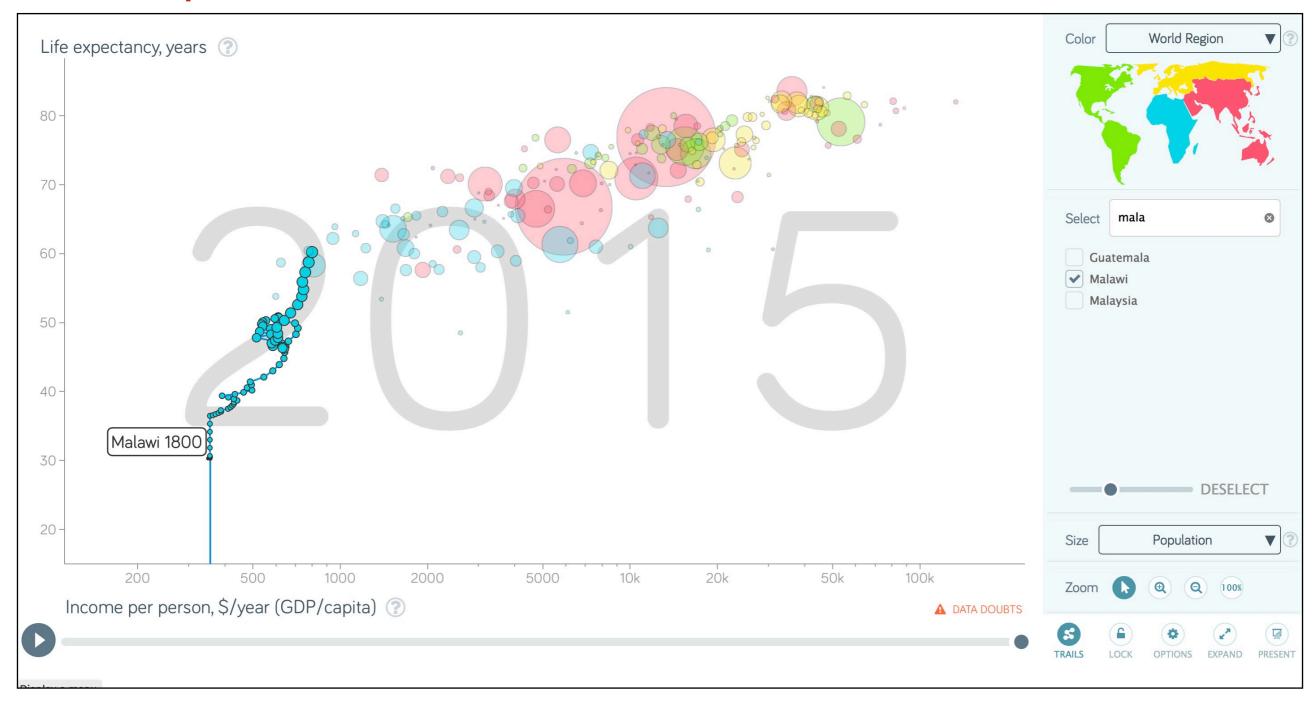








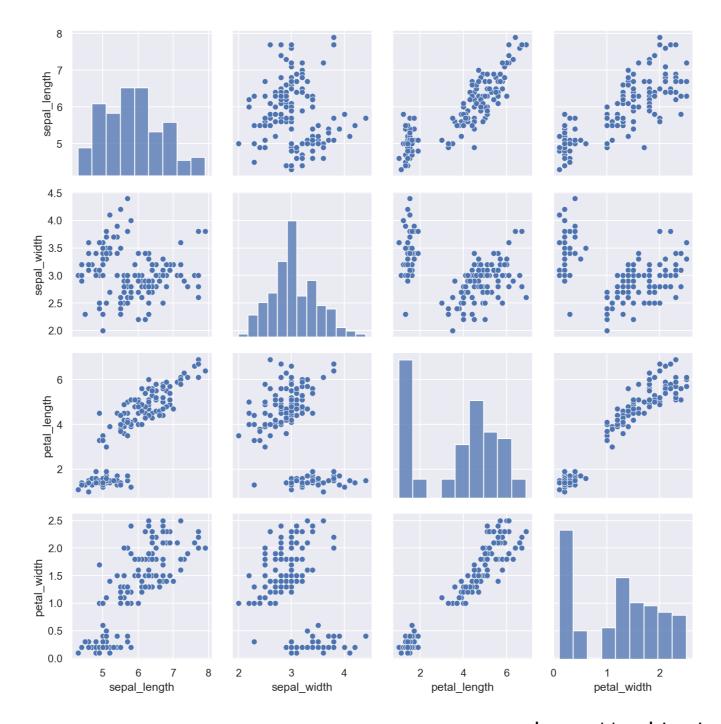






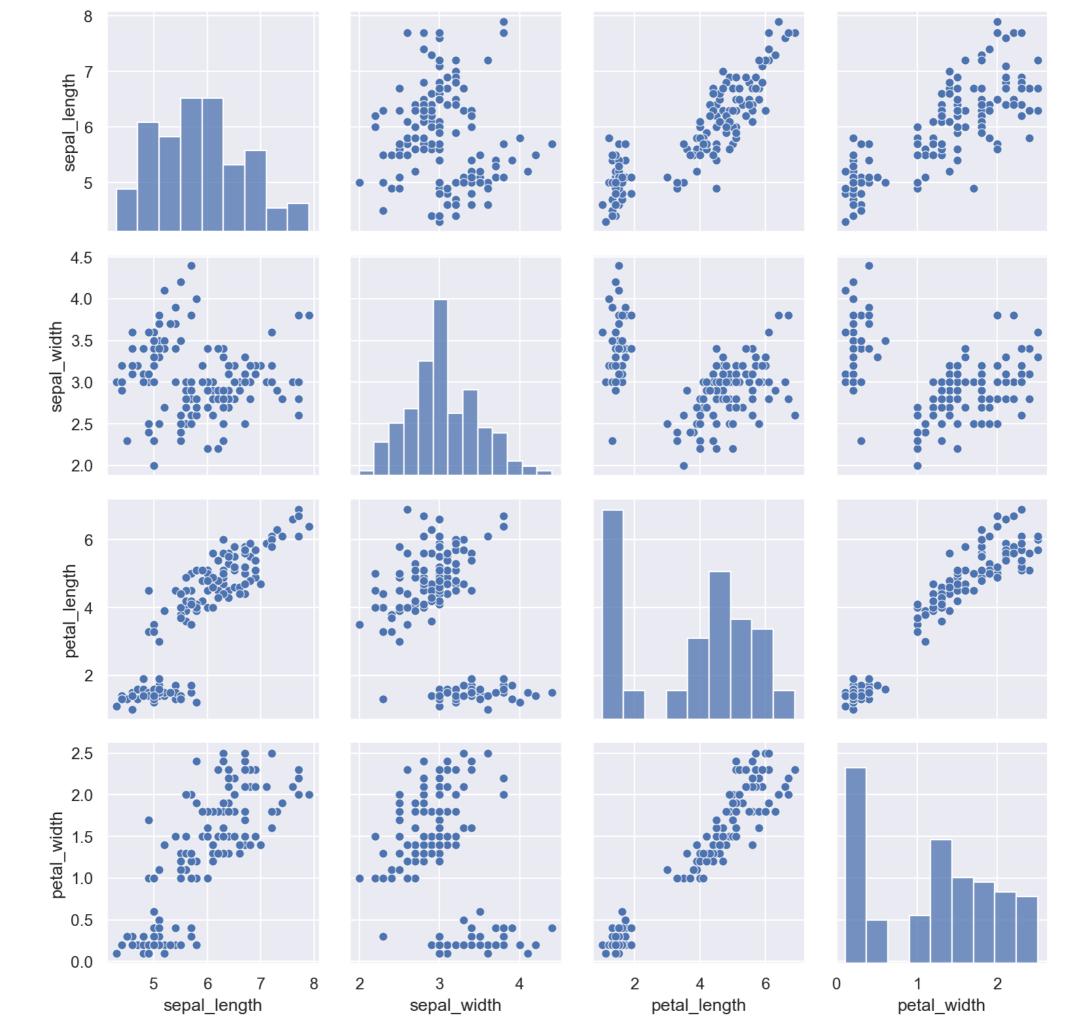
Scatterplots

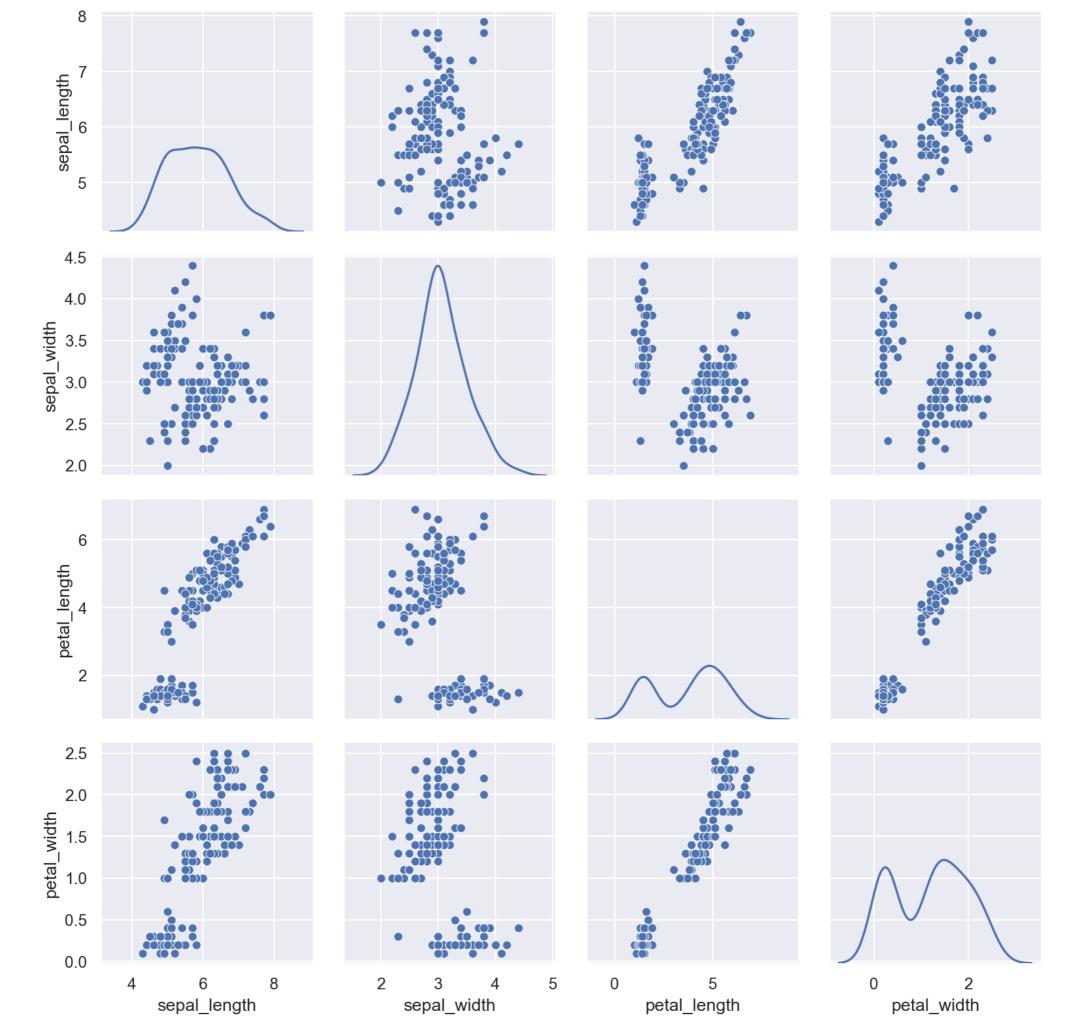
Matrix

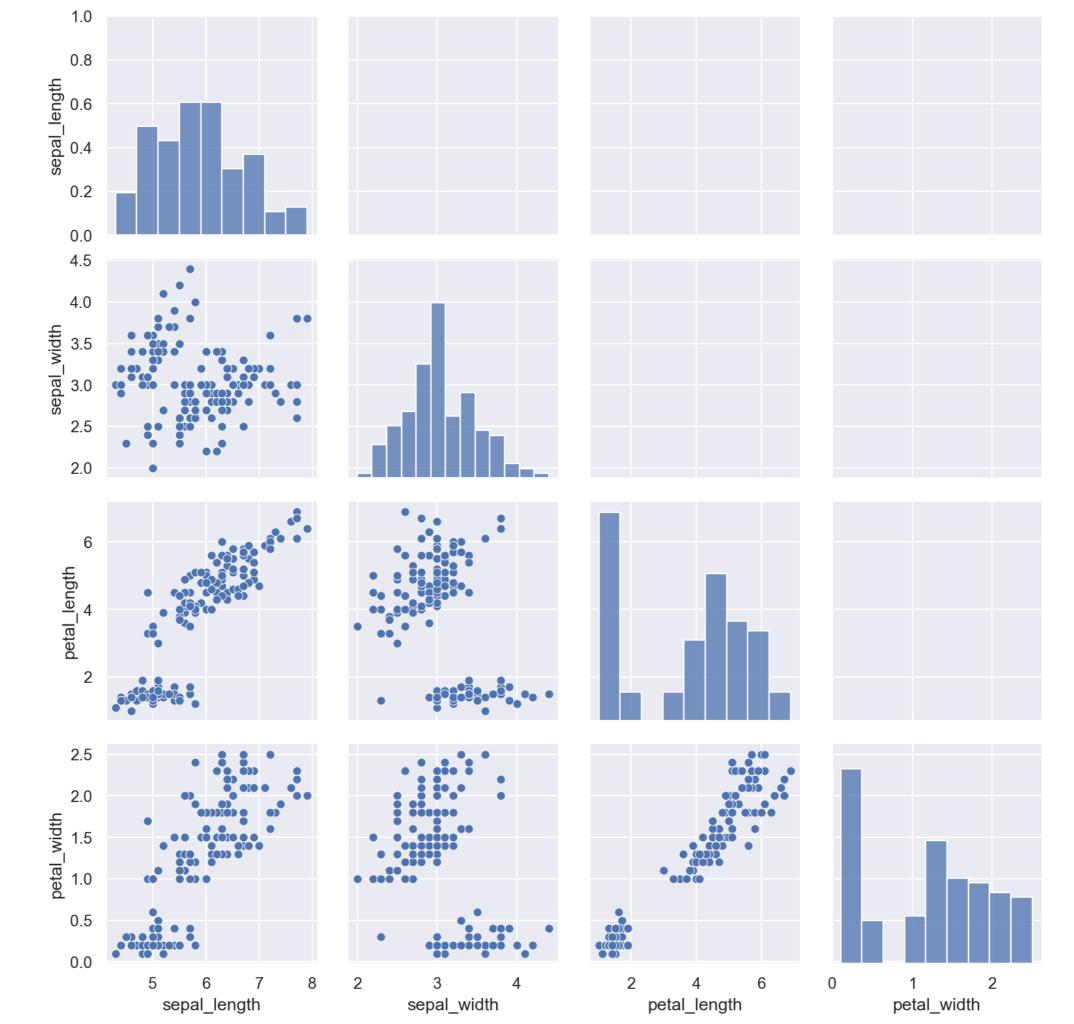


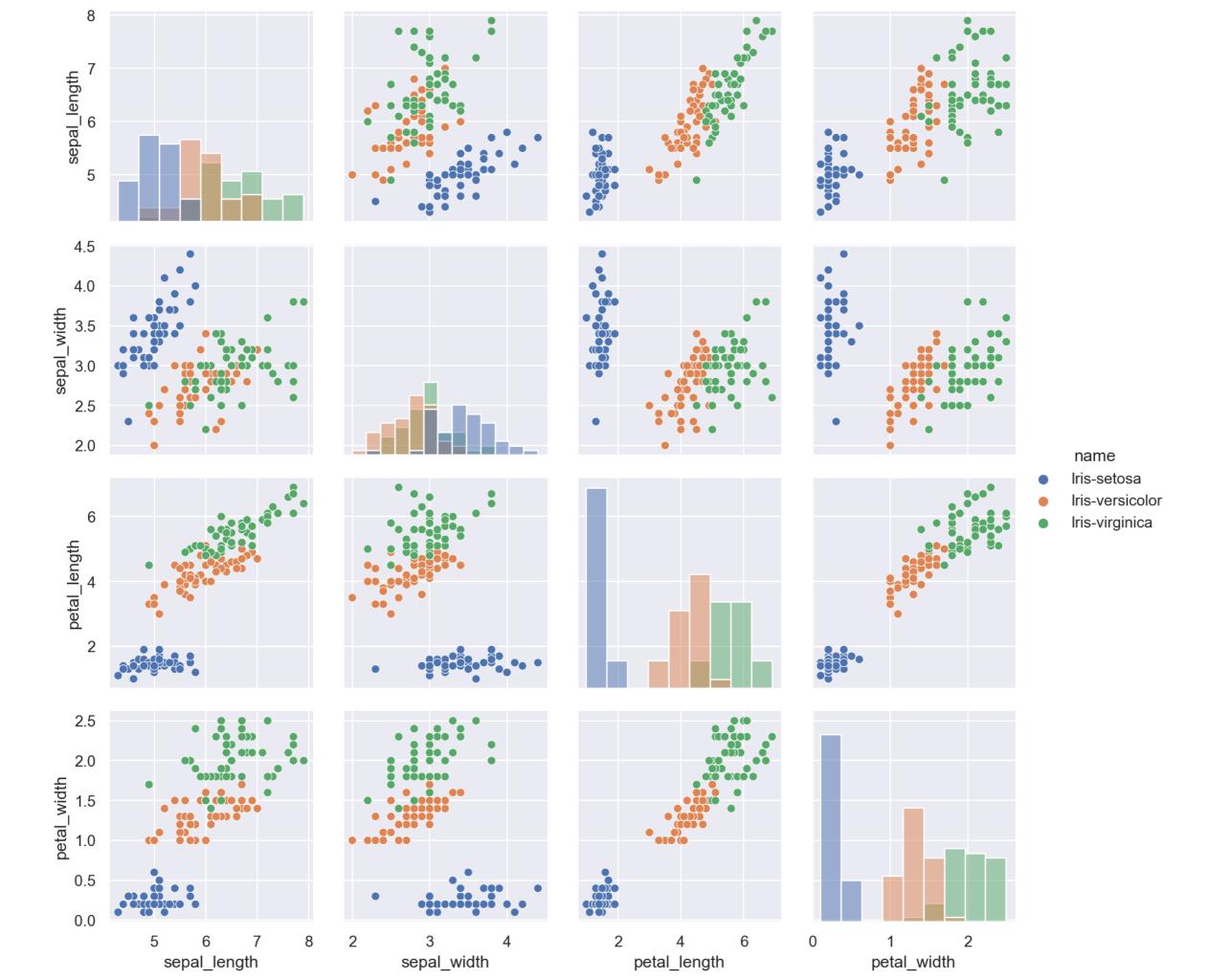
https://archive.ics.uci.edu/ml/datasets/iris



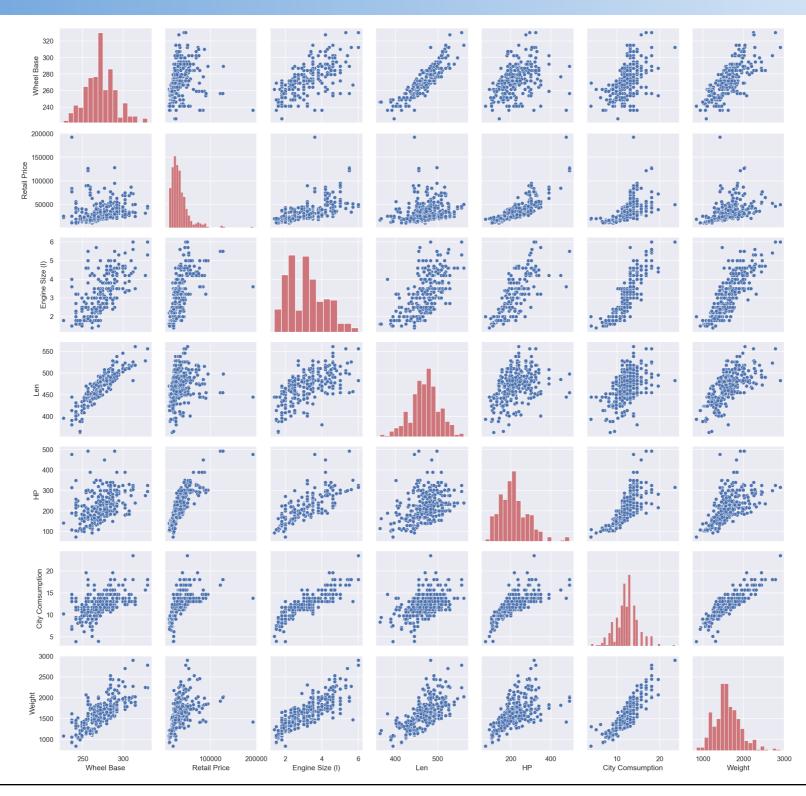




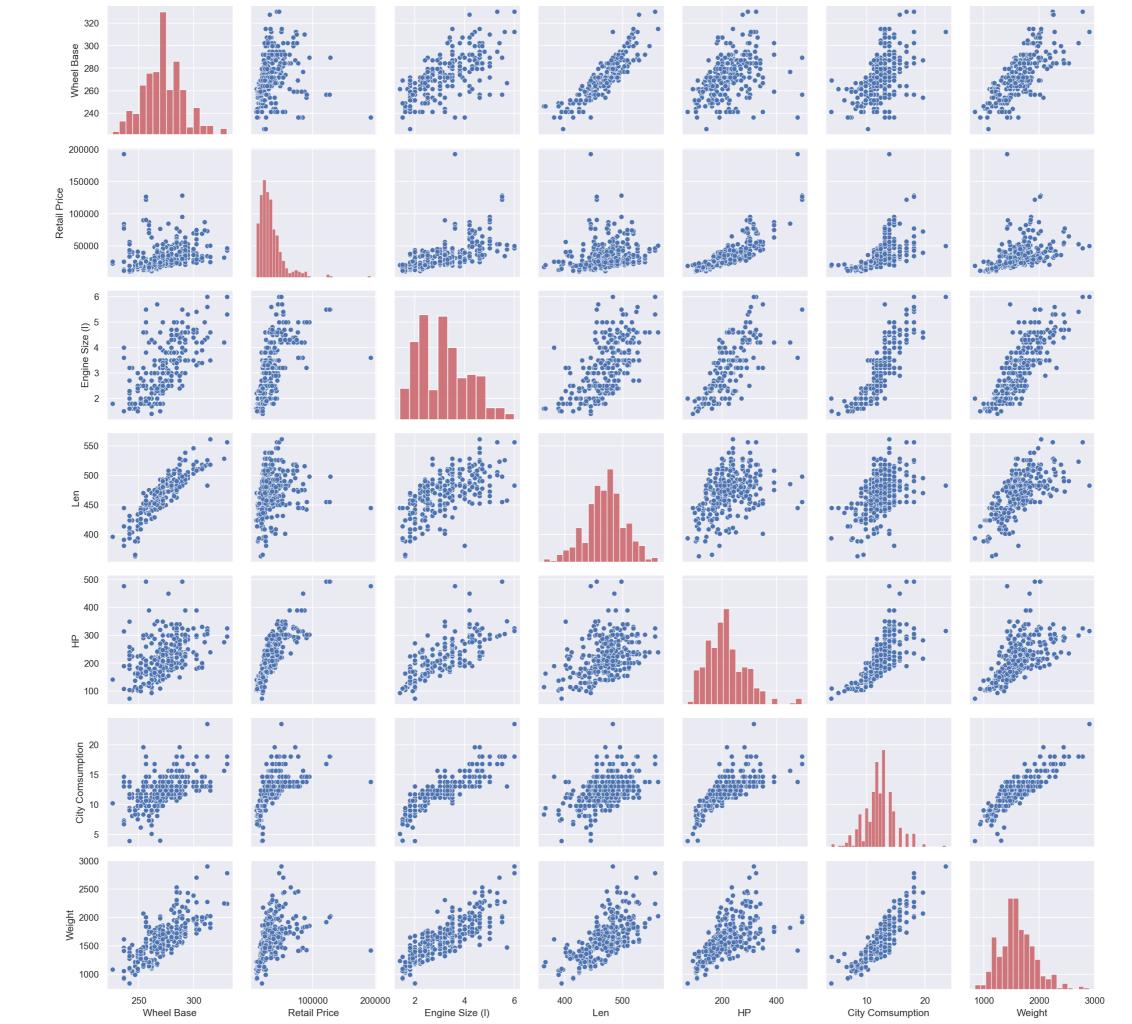


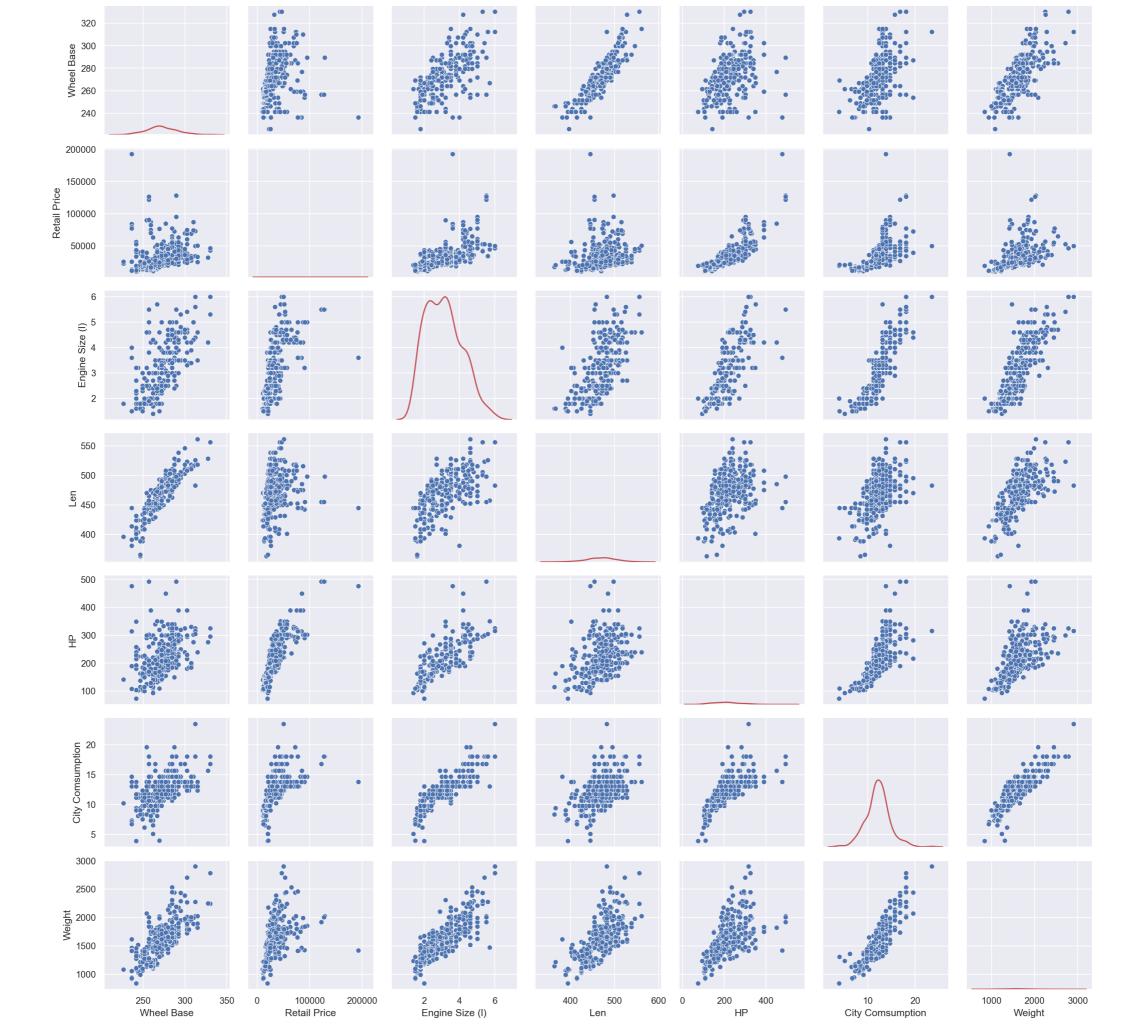


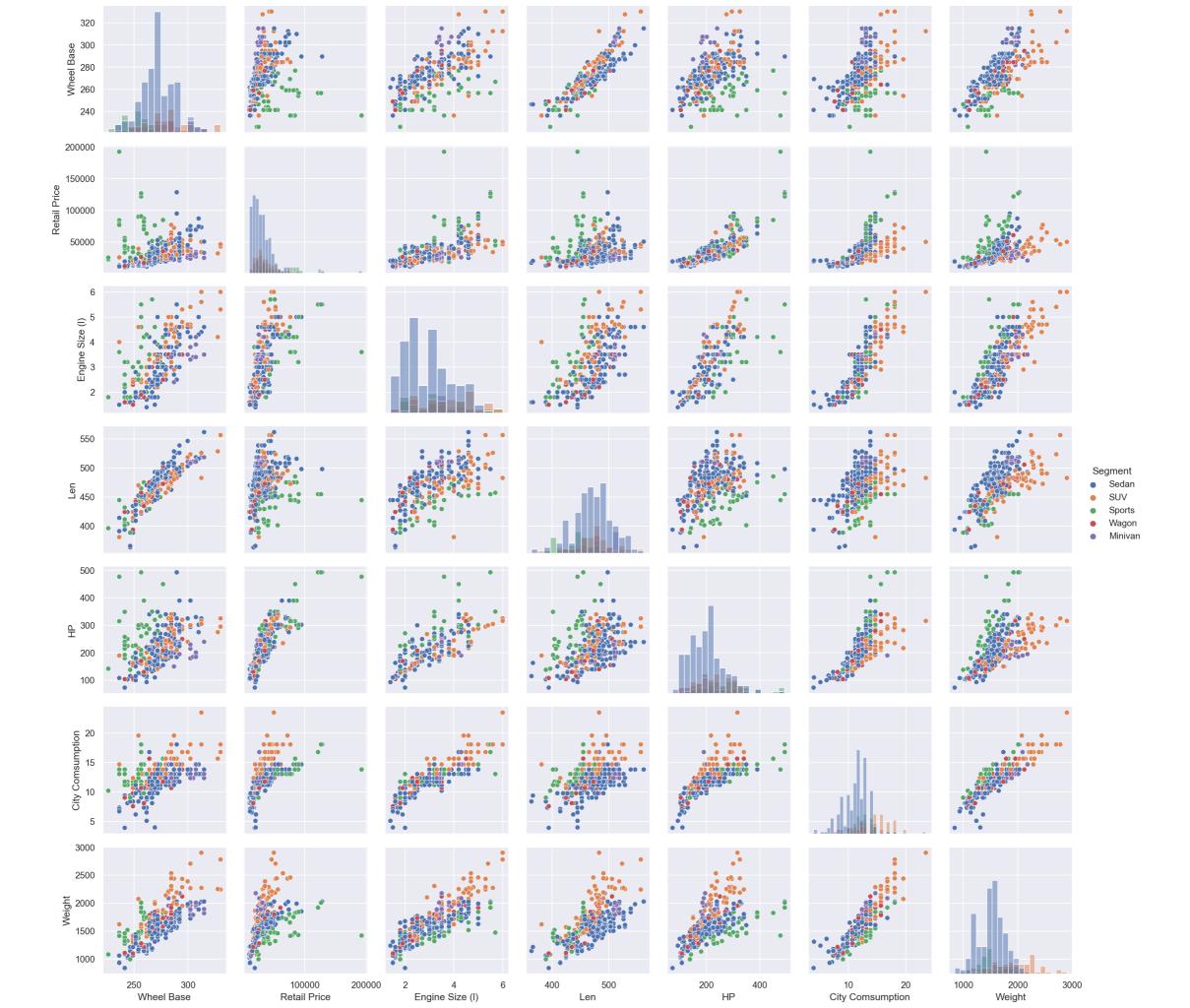
Scatter matrix (in Python)





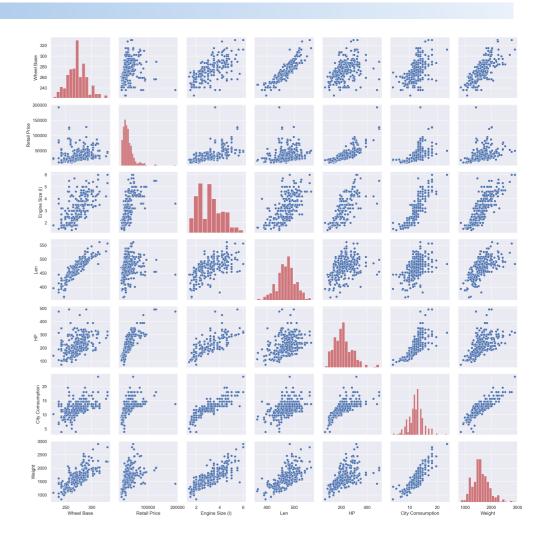




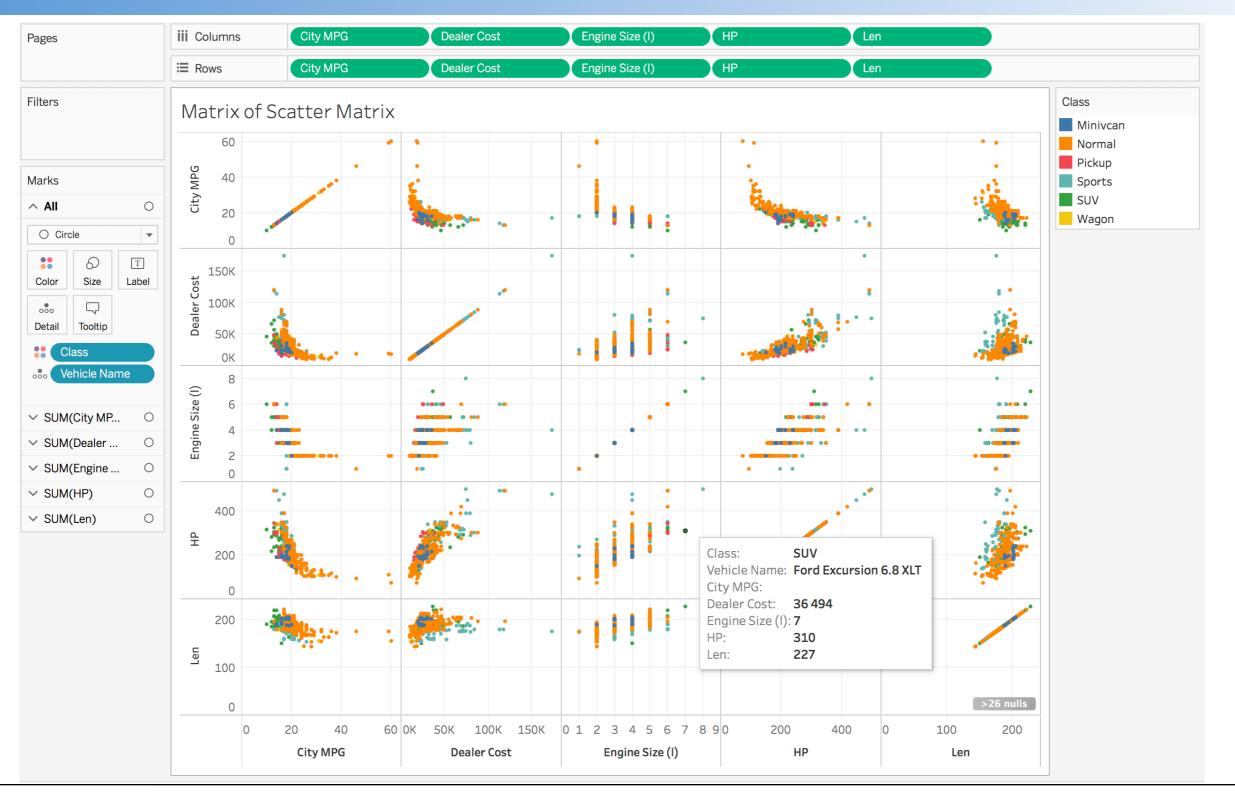


Scatter matrix (in Python)

```
scatter_matrix(frame,
   alpha=0.5, figsize=None,
   ax=None, grid=False,
   diagonal='hist',
   marker='.',
   density_kwds=None,
   hist_kwds=None,
   range_padding=0.05,
   **kwds)
```

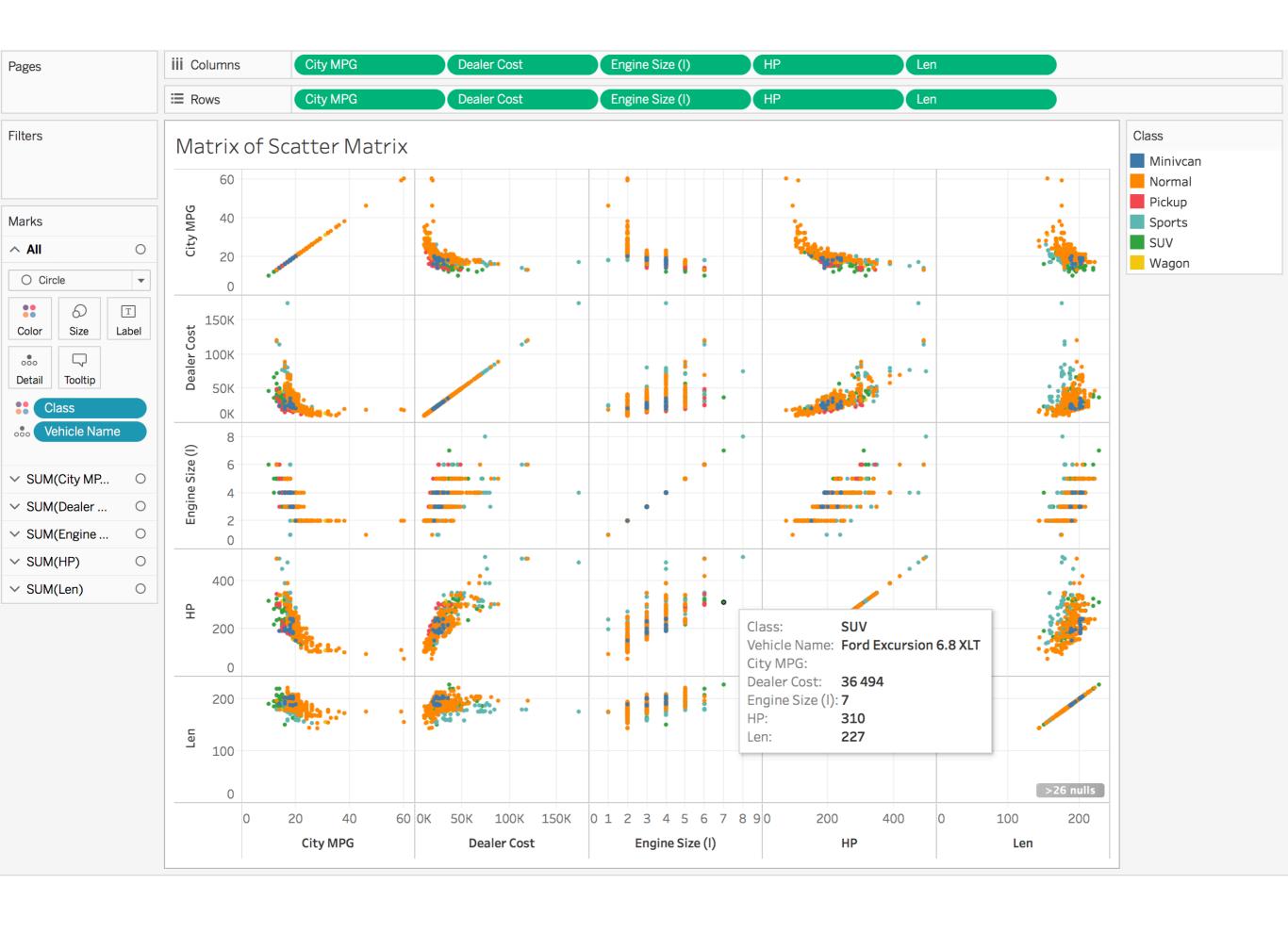


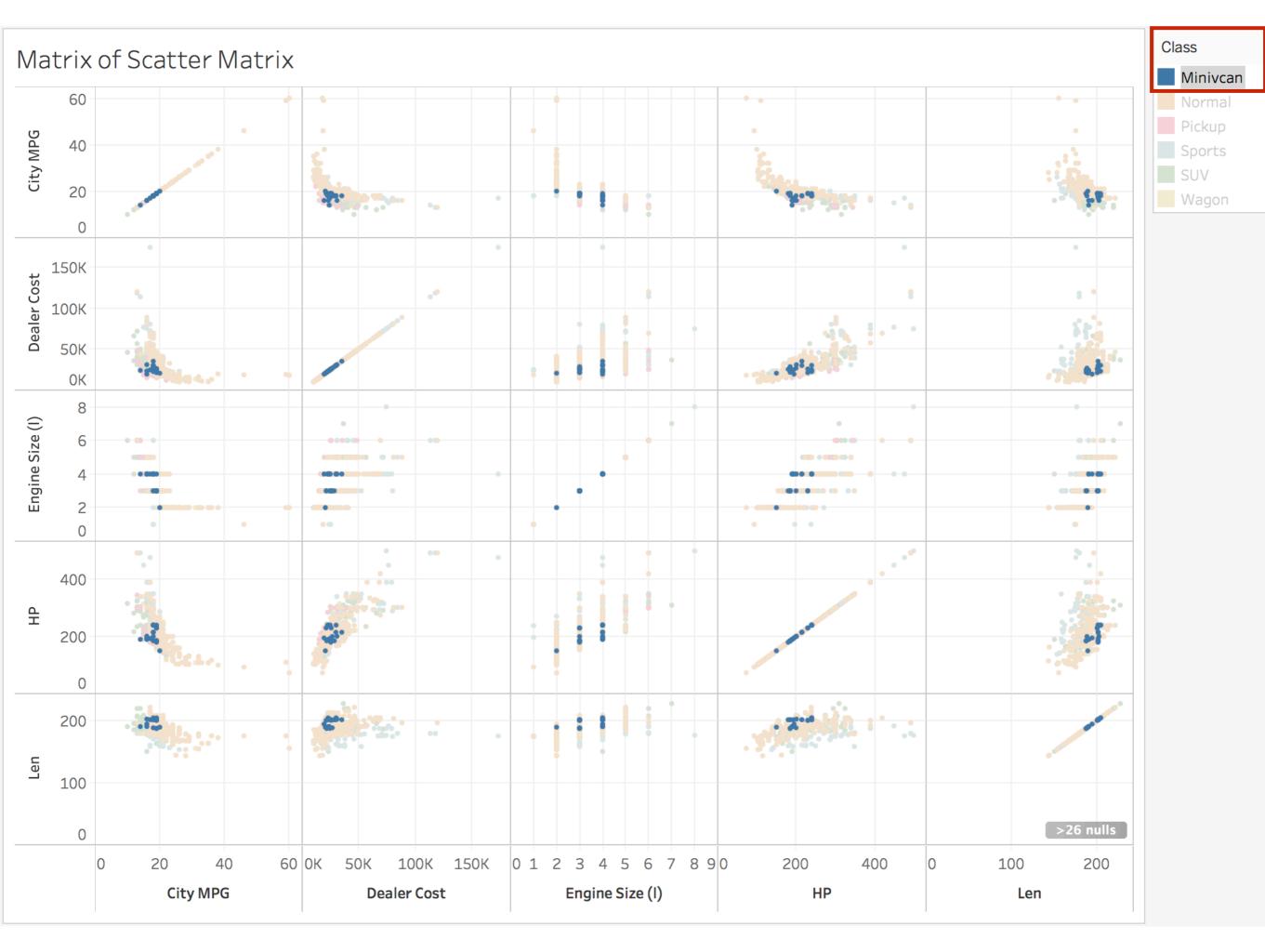
Scatter Matrix (in Tableau)

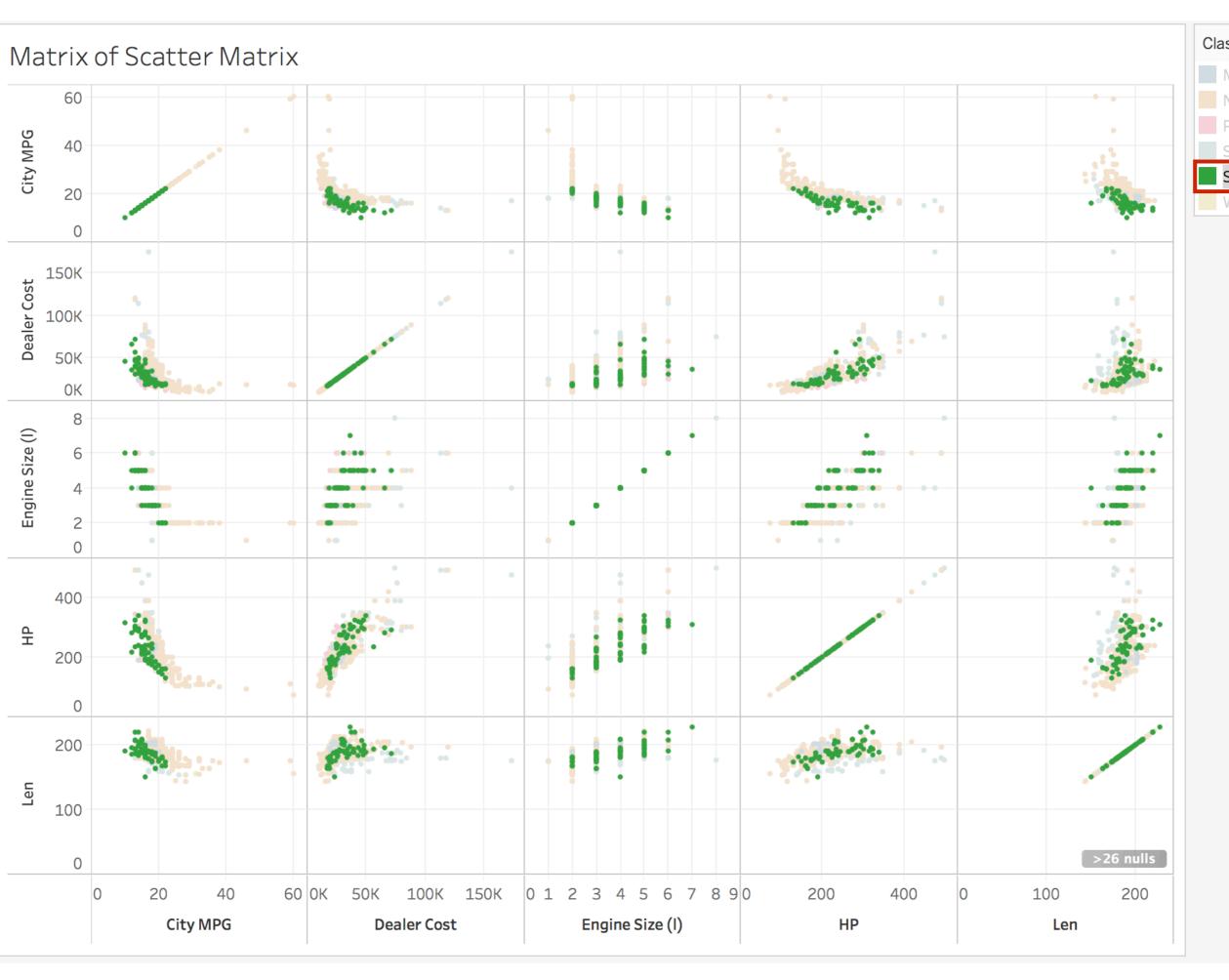


Scatter Matrix (in Tableau)







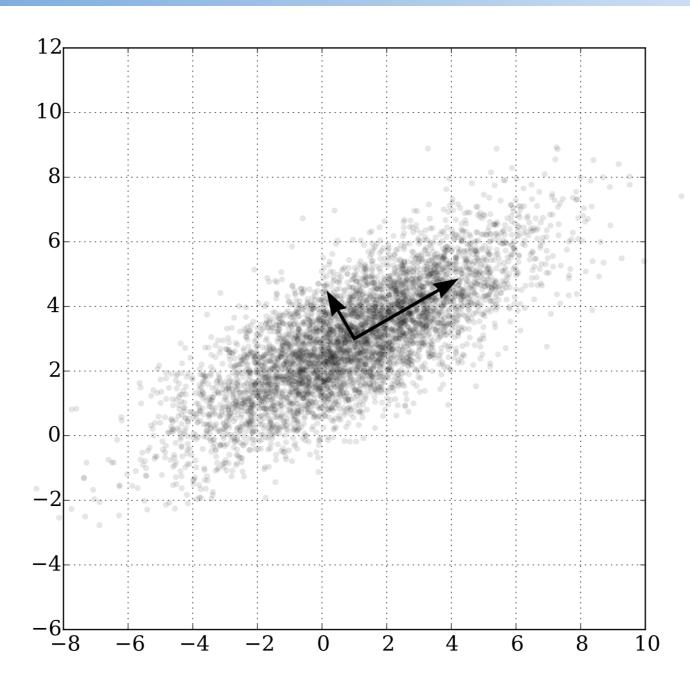




- In situations where the dimensionality of the data exceeds the capabilities of the visualization technique. It is necessary to investigate ways to reduce the data dimensionality, while at the same time preserving, as much as possible, the information contained within.
- Principal Component Analysis (PCA) read more and see this implementation
- Multidimensional Scaling (MDS) read more and more
- Non-linear dimension reduction techniques:
 - Self-organizing Maps (SOMs) read more
 - **♦ Local Linear Embeddings (LLE)** <u>read more</u>
 - ♦ t-distributed Stochastic Neighbor Embedding (t-SNE) read more



Principal Component Analysis (PCA)

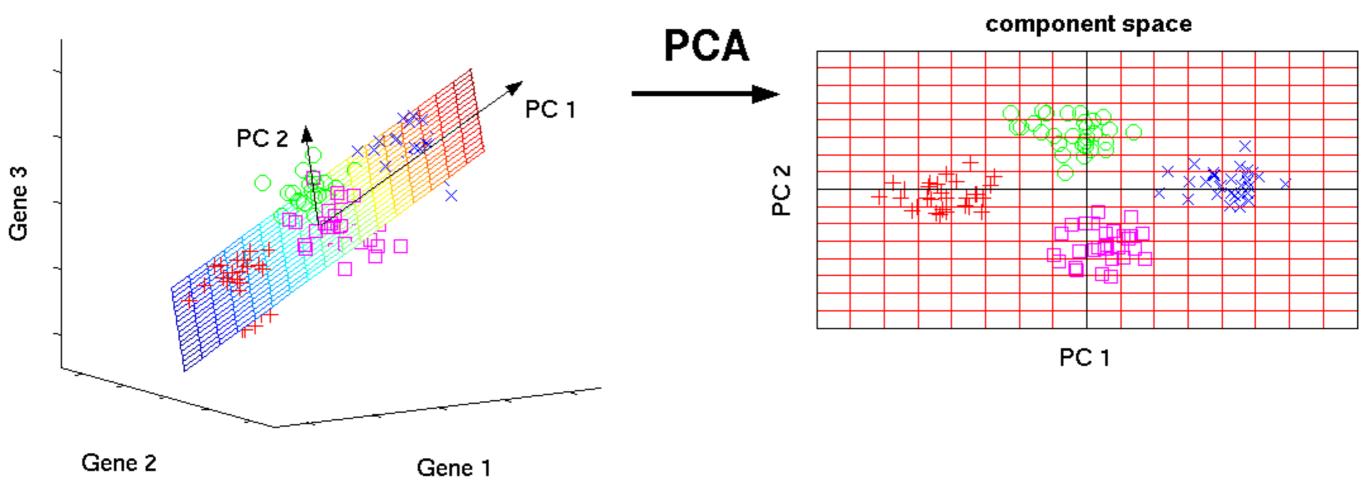


https://en.wikipedia.org/wiki/Principal_component_analysis



Principal Component Analysis (PCA)

original data space



http://www.nlpca.org/pca_principal_component_analysis.html



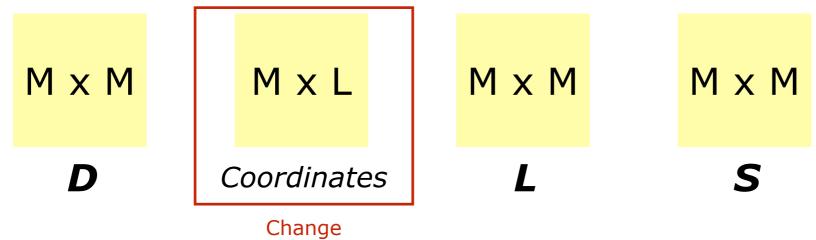
Multidimensional scaling (MDS)

- Projecting M points in N dimensions into L dimensions (L=2 or 3) display space.
- The key goal is to attempt to maintain the N-dimensional features and characteristics of the data through the projection process, e.g., relationships that exist in the original data must also exist after projection.
 - ◆ The projection may also unintentionally introduce artifacts that may appear in the visualization and are not present in the data.
- 1. Create a Similarity M x M Matrix (D) (could be distance)
- 2. Create a coordinates Matrix M x L and fill randomly or other method (ex: PCA)
- 3. Create an $M \times M$ matrix (L) based on L coordinates. Also a similarity matrix.
- 4. Repeat
 - 1. Compute the stress matrix S (an M x M Matrix), as the difference between D and L.
 - 2. Shift the positions of points in L-dimensional space (their L coordinates) in a direction that will reduce their individual stress levels.
- 5. Until S is small or has not changed significantly



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Multidimensional scaling (MDS)

- There are many possible variants on this algorithm, including:
 - Different similarity and stress measures
 - Different initial and termination conditions
 - Different position update strategies
- As in any optimization process, there is the potential to fall into a local minimal configuration that still has a high level of stress.
 - Common strategies to alleviate this include occasionally adding a random jump in the position of a point to see if it will converge to a different location
- Obviously, the results are not unique: minor changes in the starting conditions can lead to dramatically different results.



Iris flower data set



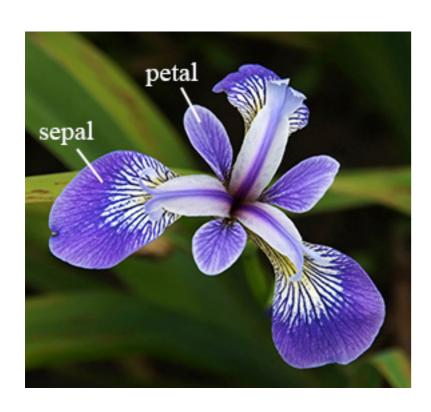


Iris versicolor



Iris virginica

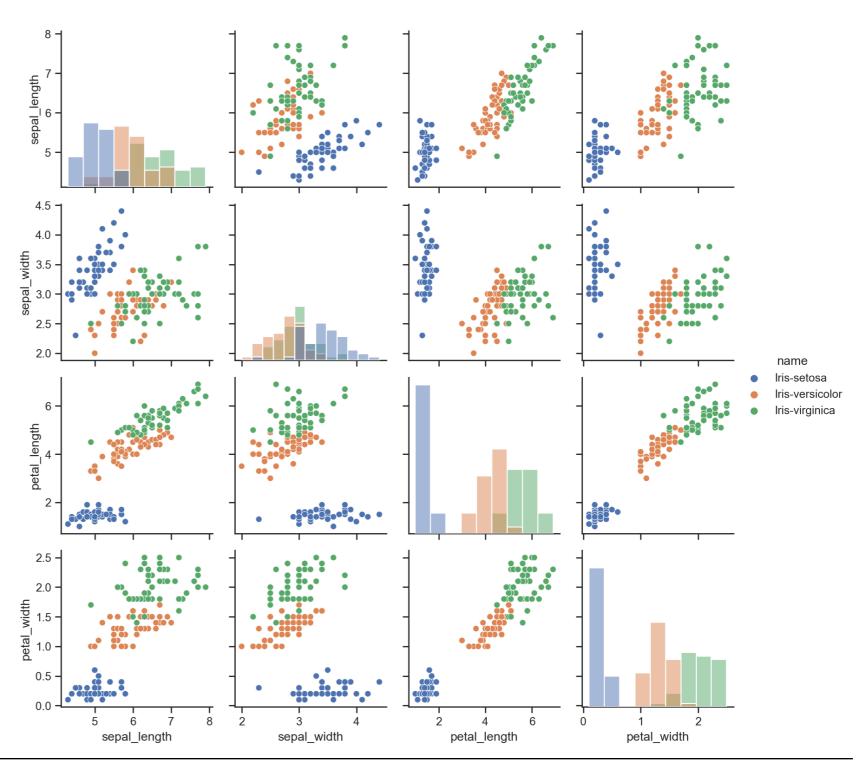
Iris setosa



Iris setosa

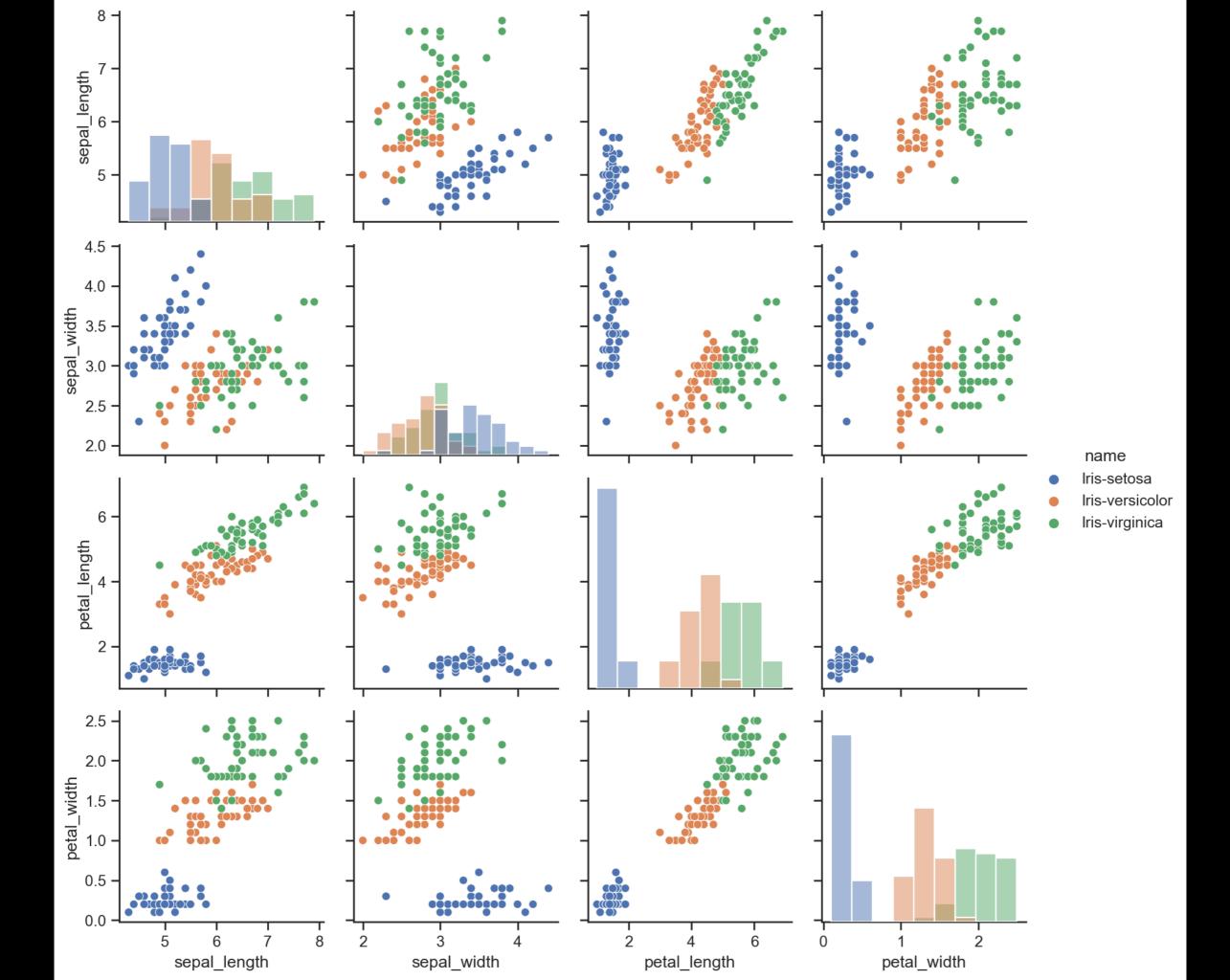
Iris versicolor

Iris virginica

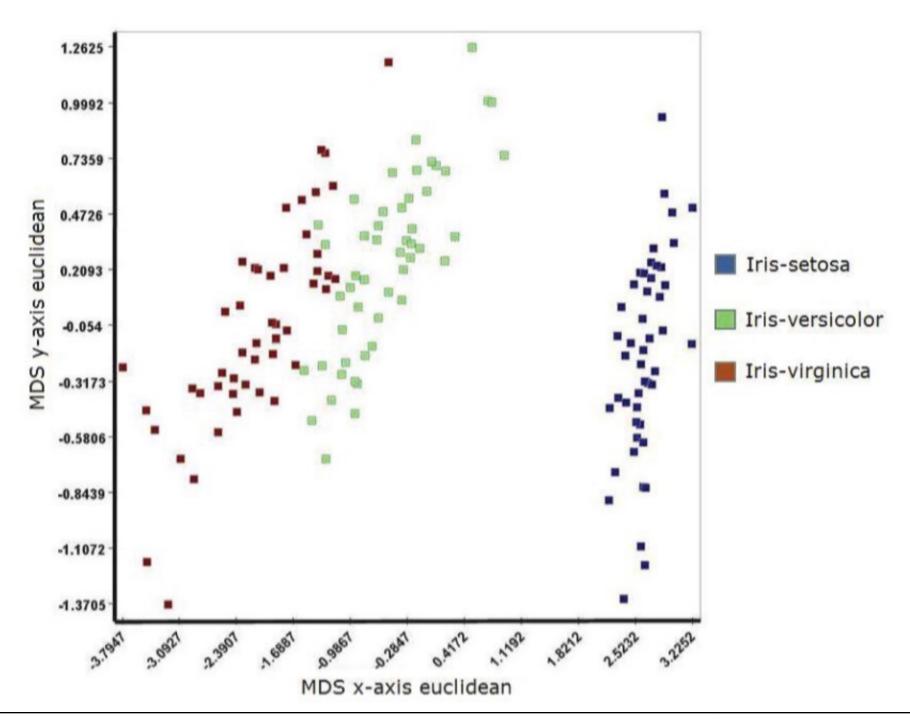




Visualization Techniques for Multivariate Data - 36



Iris data set projected using MDS

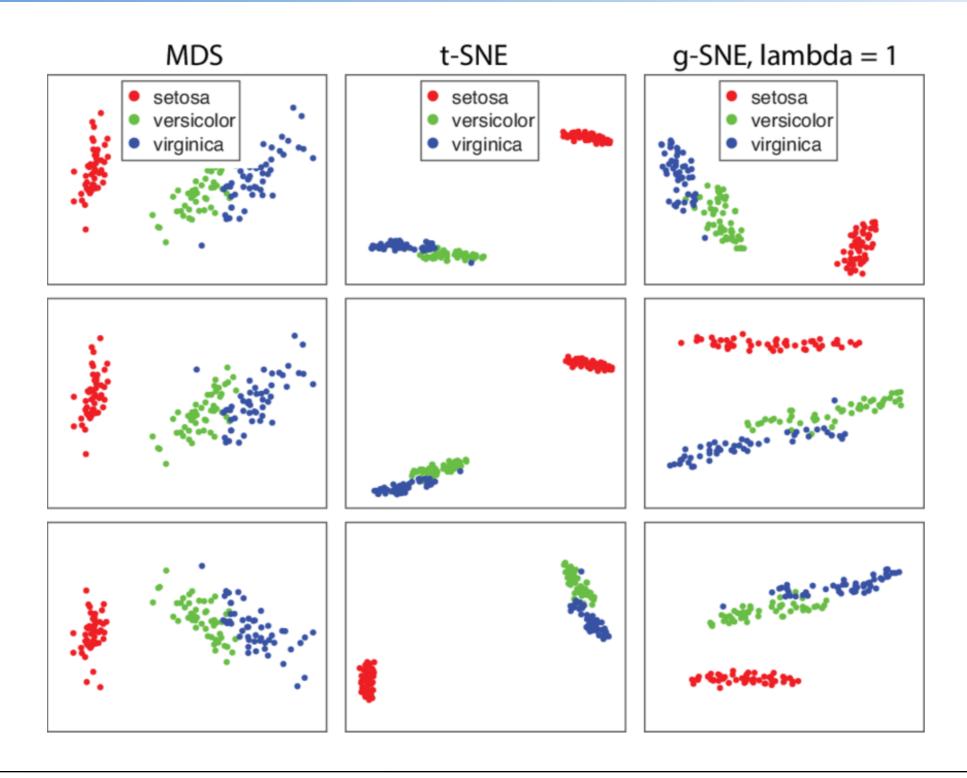


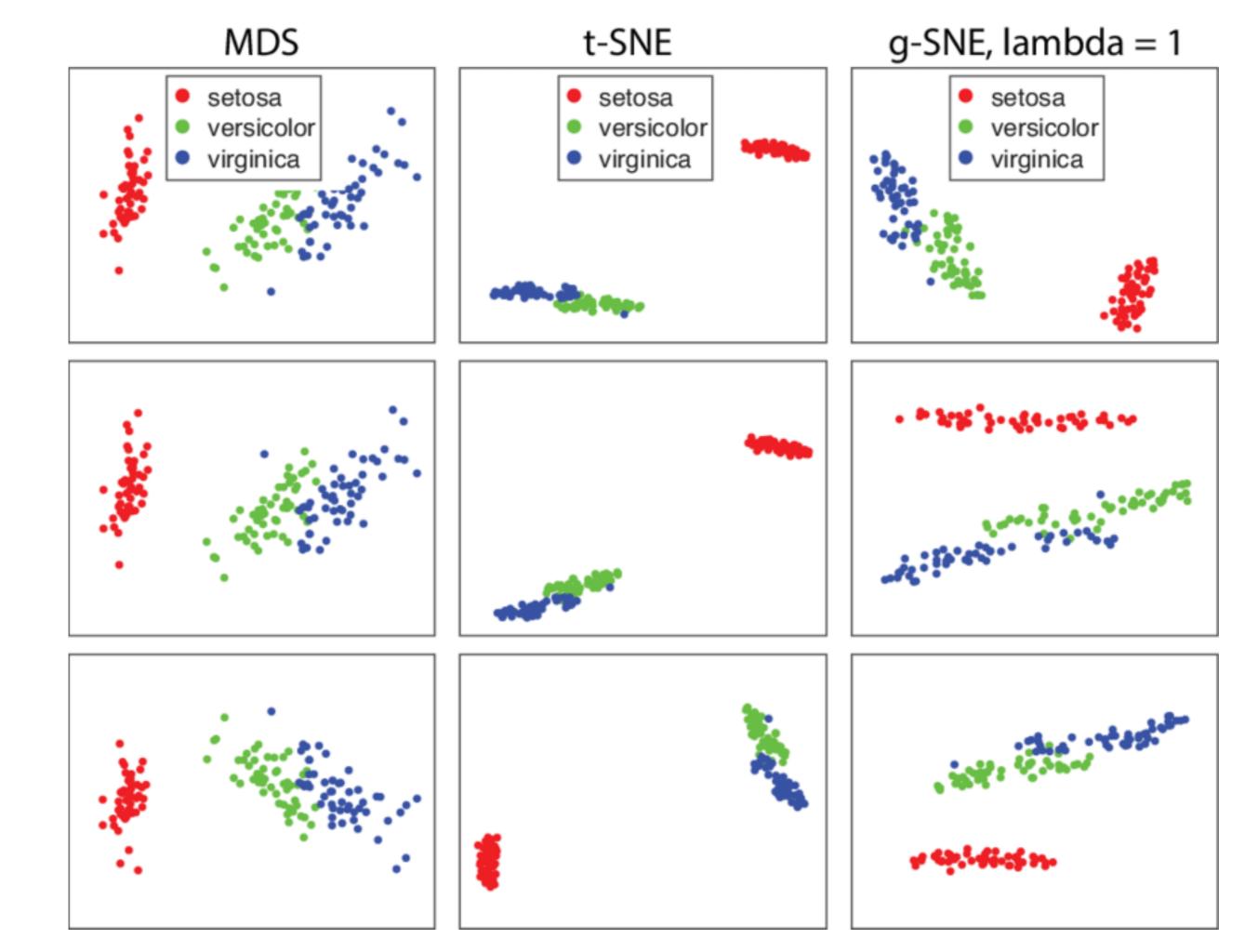


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 - t-distributed Stochastic Neighbor Embedding (t-SNE) read more



Using global t-SNE to preserve inter-cluster data structure





- RadViz: is a force-driven point layout technique that is based on <u>Hooke-s Law</u> for equilibrium.
- For an N-dimensional data set, N anchor points are placed on the circumference of the circle to represent the fixed ends of the N springs attached to each data point.
- Different placement and ordering of the anchors will give different results, and points that are quite distinct in N dimensions may map to the same location in 2D.

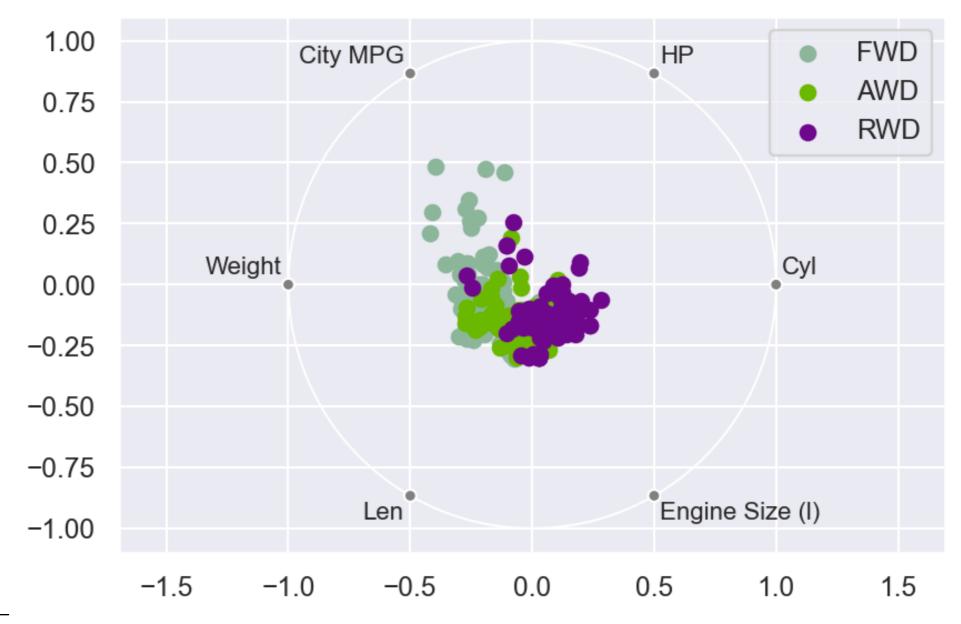


DIMENSIONAL ANCHORS: A GRAPHIC PRIMITIVE FOR MULTIDIMENSIONAL MULTIVARIATE INFORMATION VISUALIZATIONS, Patrick Hoffman, Georges G. Grinstein

Visualizing Multivariate Data with Radviz

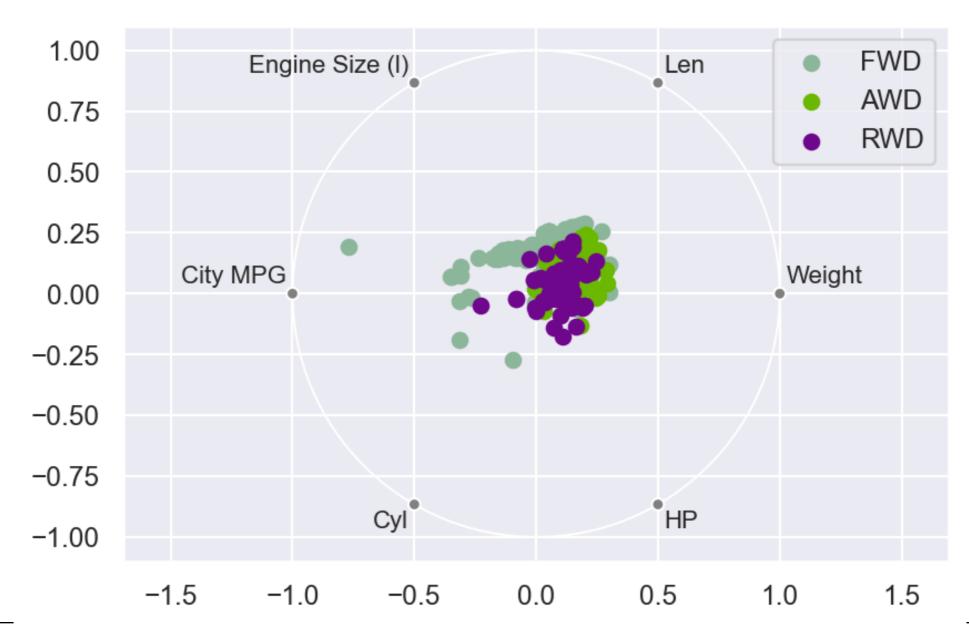


RadViz: different views of the same data set in RadViz, using manual reordering of dimensions.



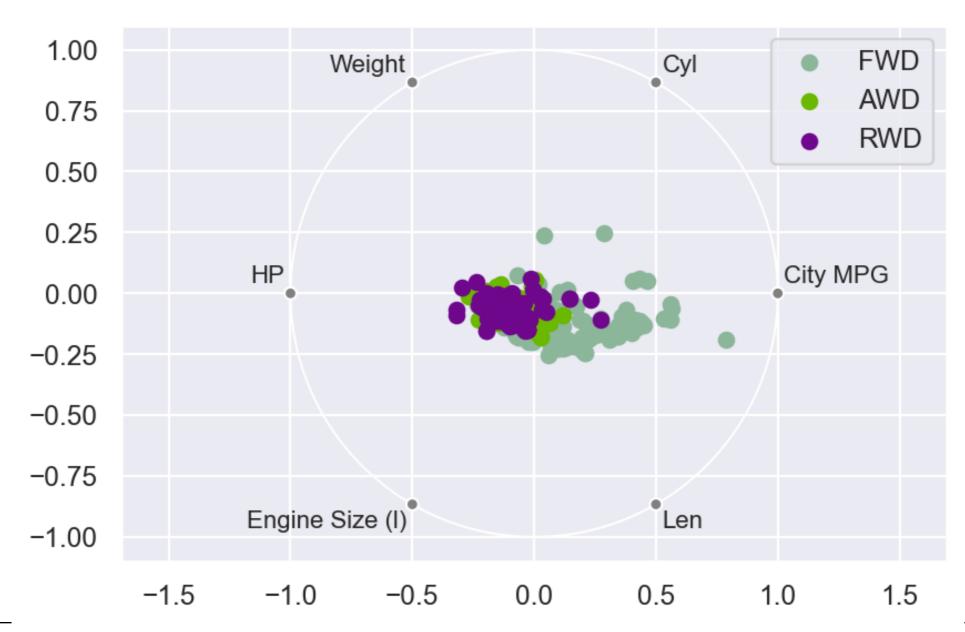


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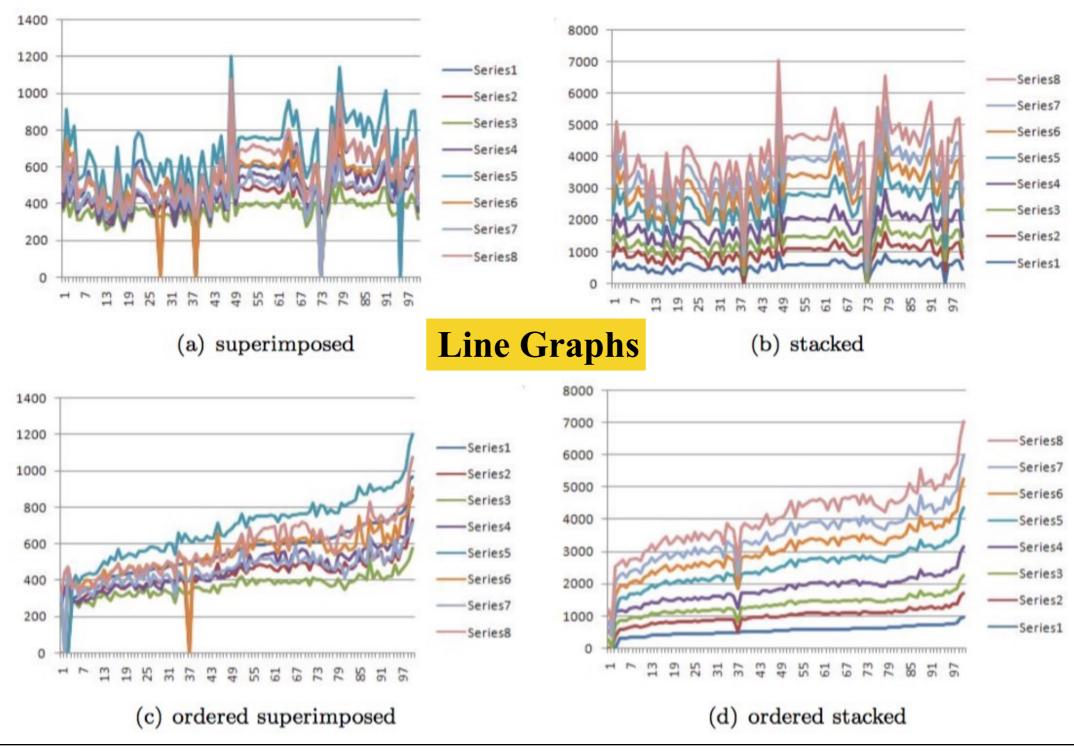




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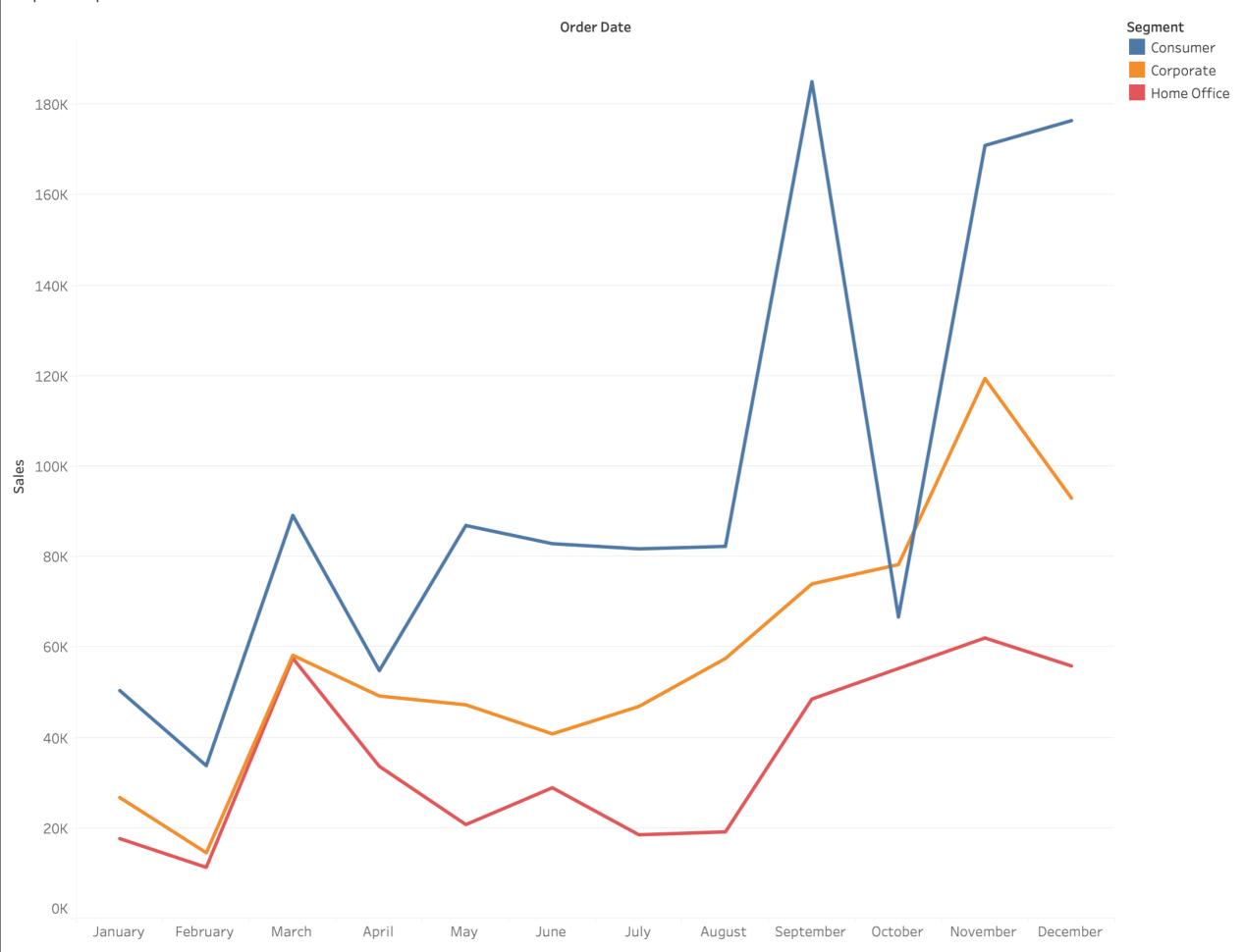
Line-Based Techniques







Superimposed - Discrete



Superimposed - Continuous Segment Consumer 60K Corporate Home Office 55K 50K 45K 40K 35K Sales 30K 25K 20K 15K 10K 5K ОК

2020

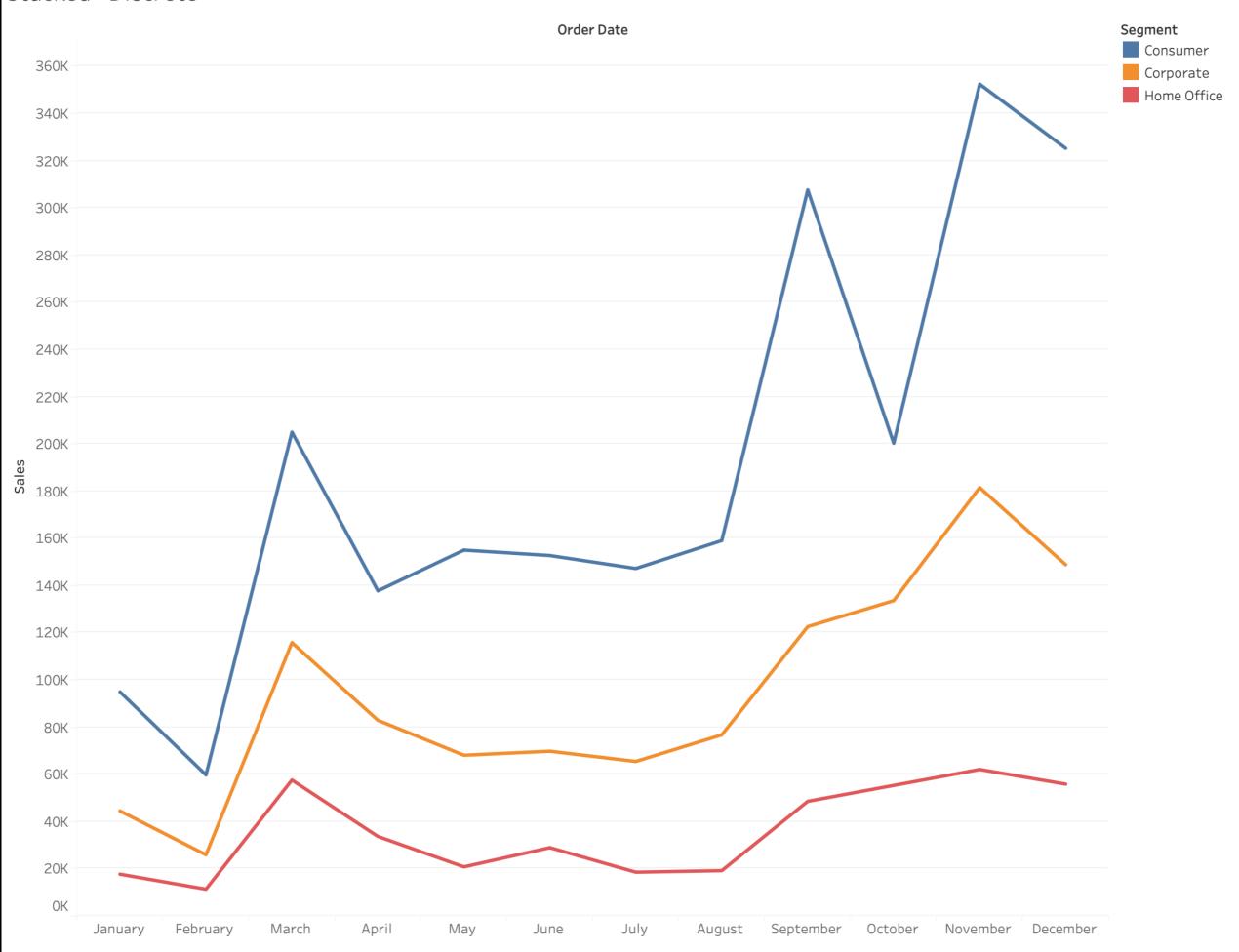
Month of Order Date

2021

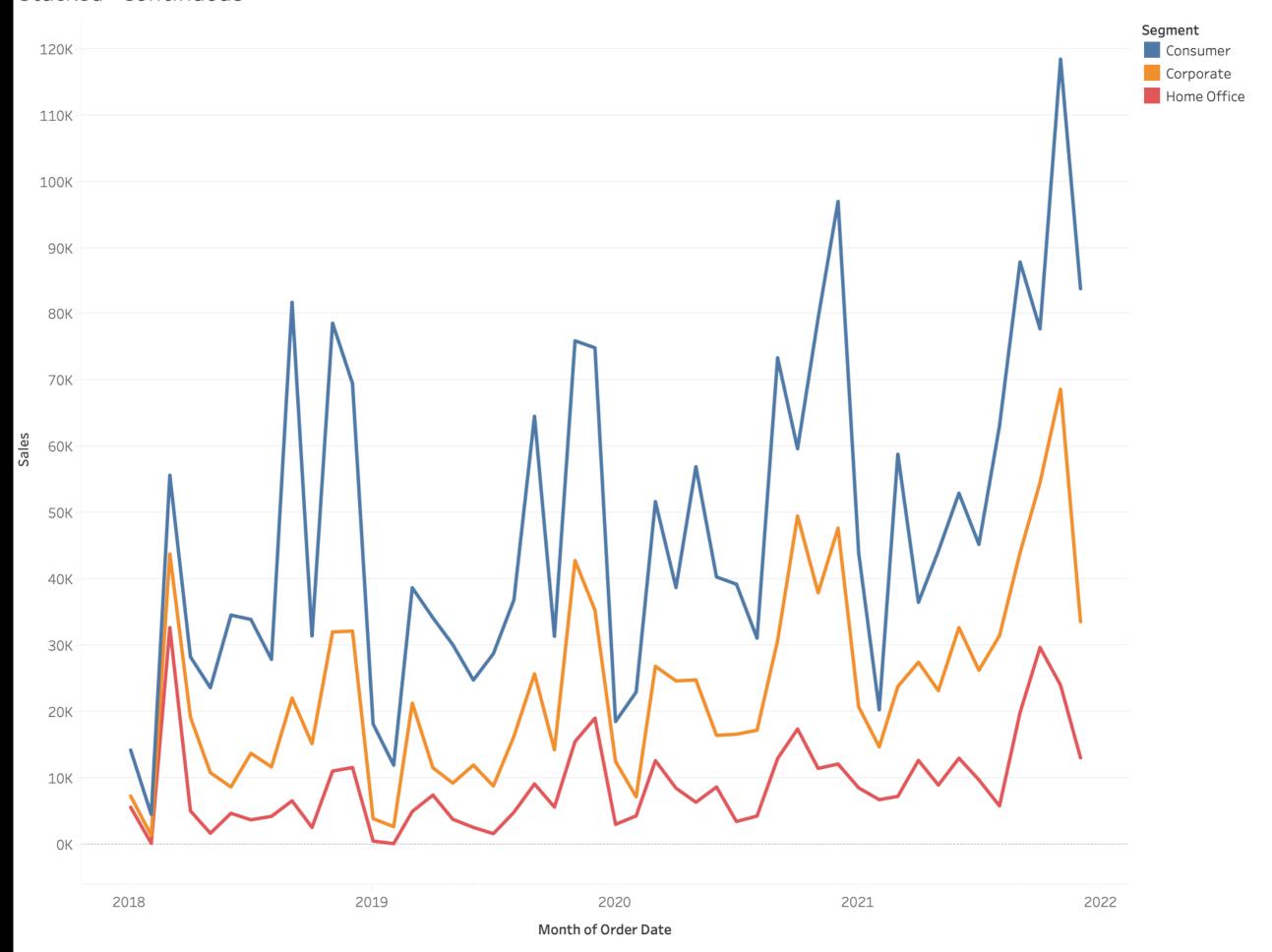
2022

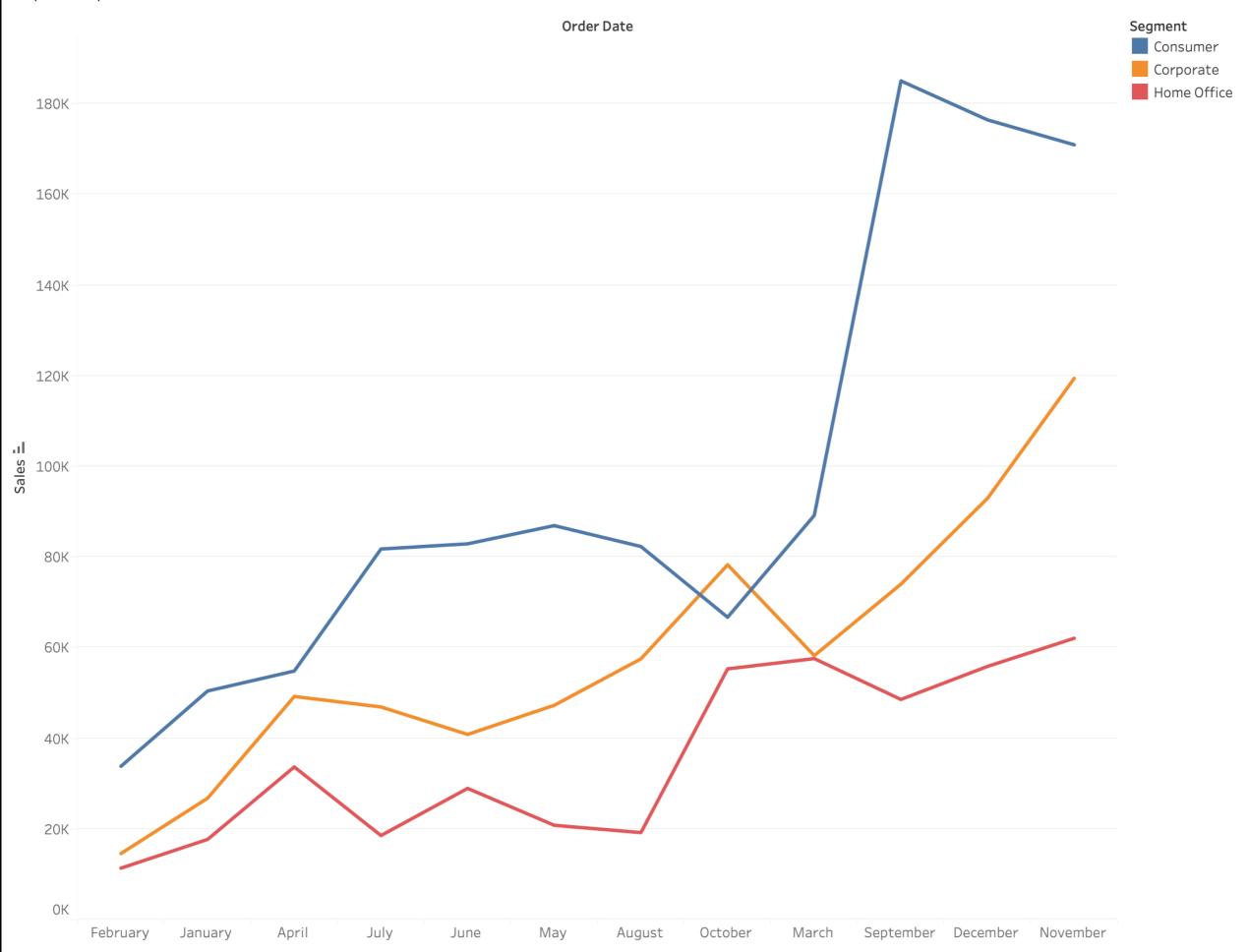
2019

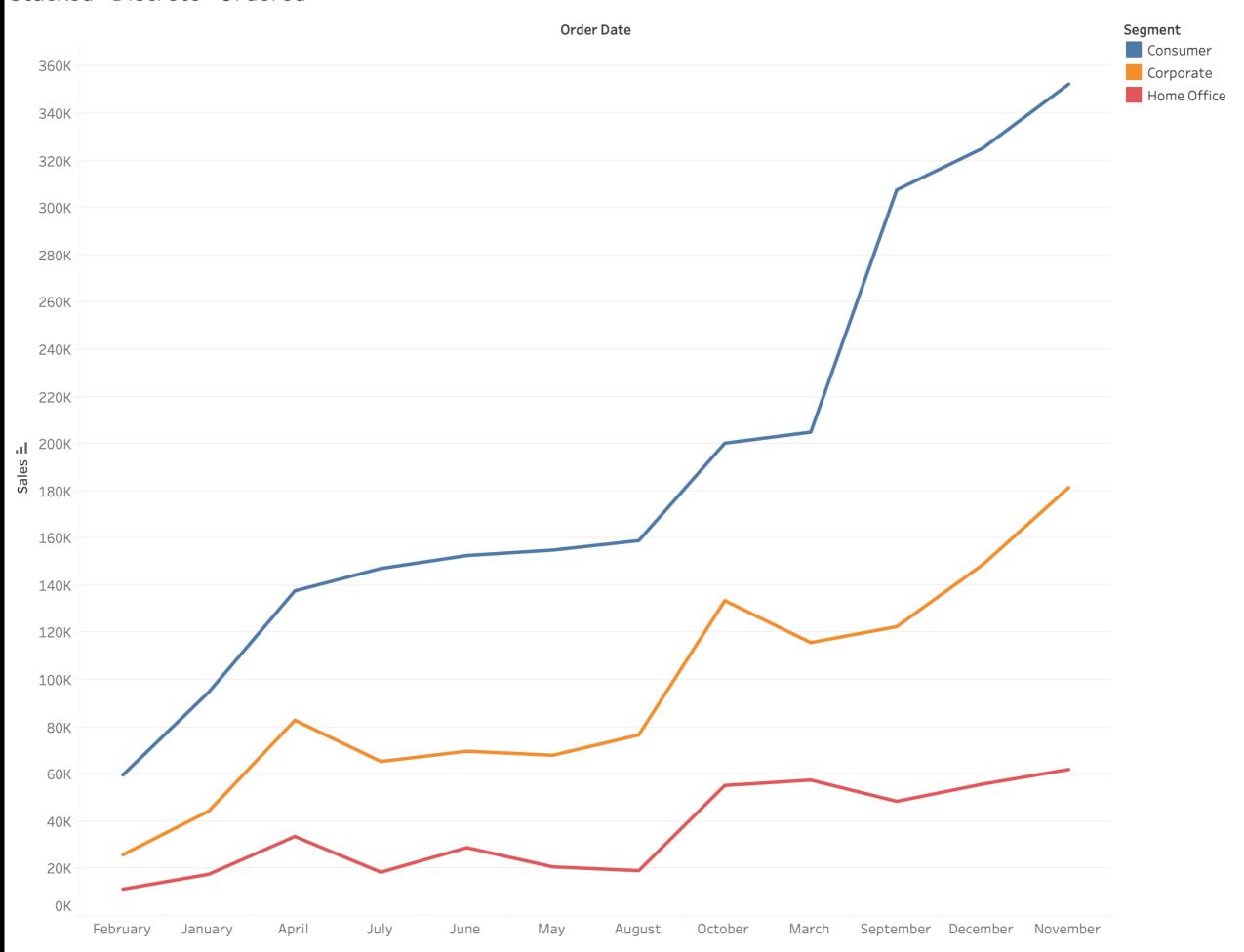
2018



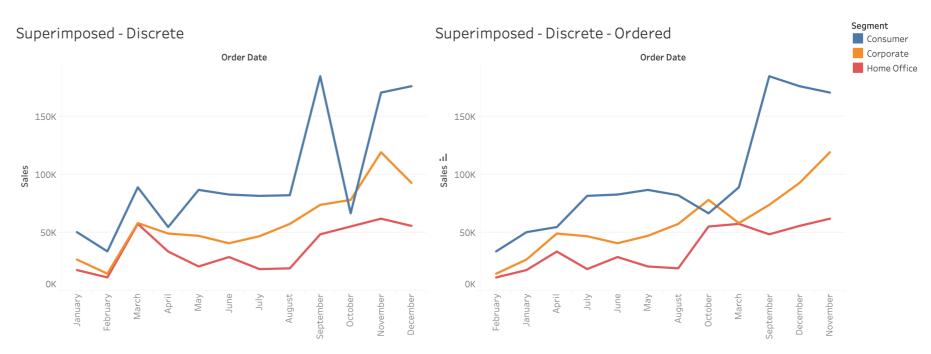
Stacked - Continuous





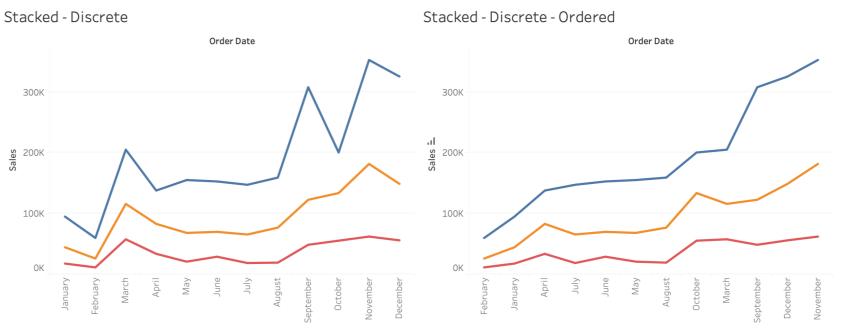


When Superimpose?

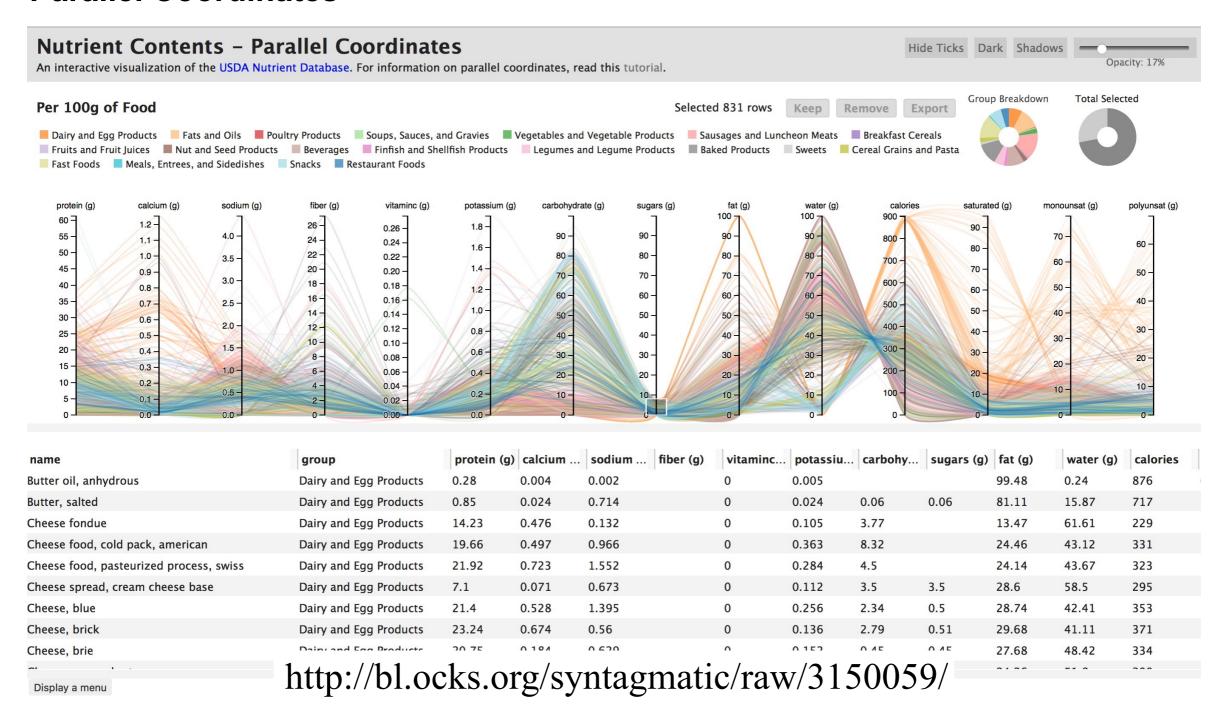


- When Order?
 - Not possible

Possible but



Parallel Coordinates





Inselberg in 1985

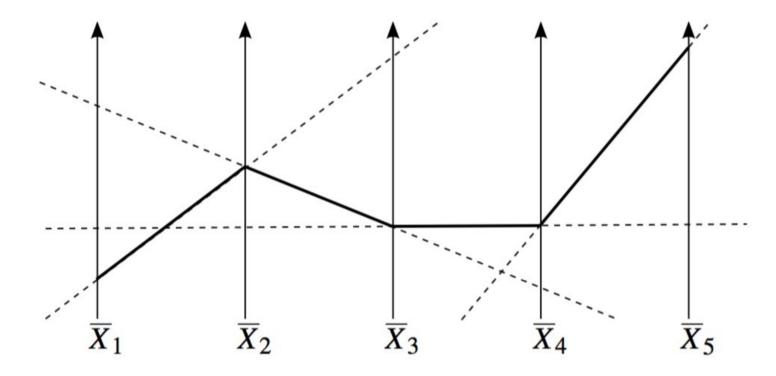


Figure 3: Constructing parallel coordinates with five dimensions represented by N=5 vertical lines. Points in the plane are represented by lines joining the corresponding coordinates at the respective axes. Typically, only the line segments between the axes are drawn (represented by the bold polyline).

State of the Art of Parallel Coordinates
J. Heinrich and D. Weiskopf



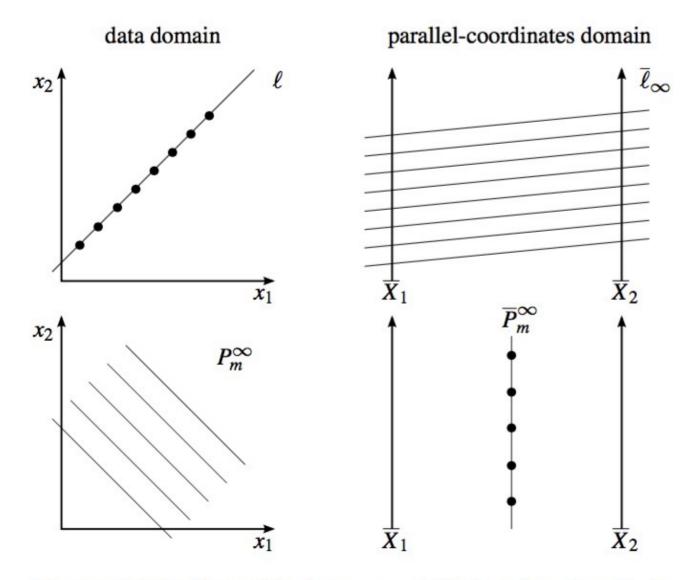


Figure 4: The line with slope m=1 in the data domain is mapped to the ideal point $\bar{\ell}_{\infty}$ in parallel coordinates (top). The vertical line $\bar{P}_m^{\infty}: x = \frac{d}{1-m}$ in parallel coordinates is represented by the ideal point P_m^{∞} with slope m in the data domain. Both domains are considered projective planes.

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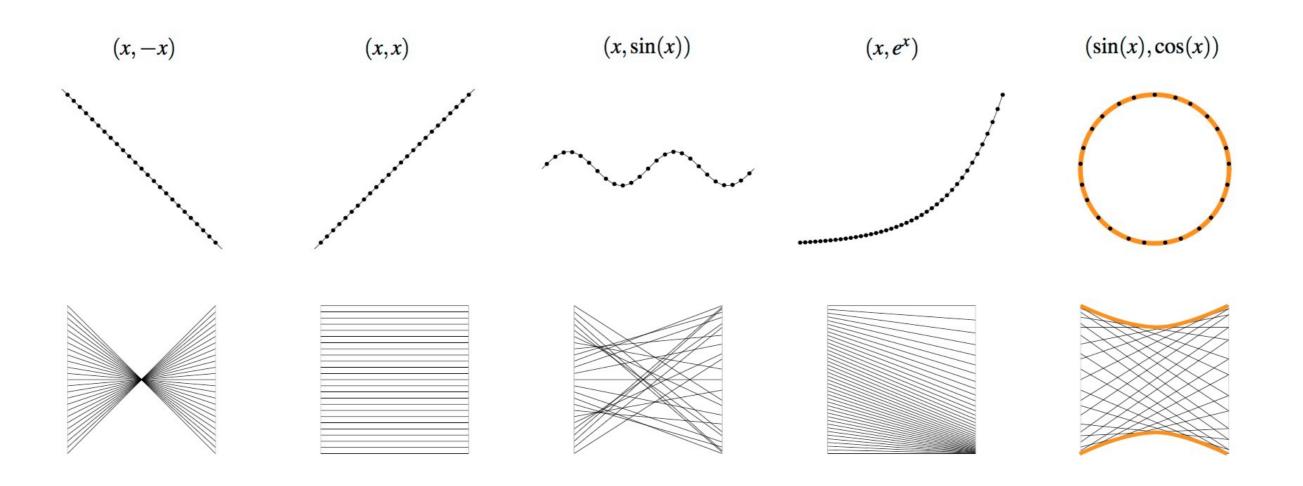
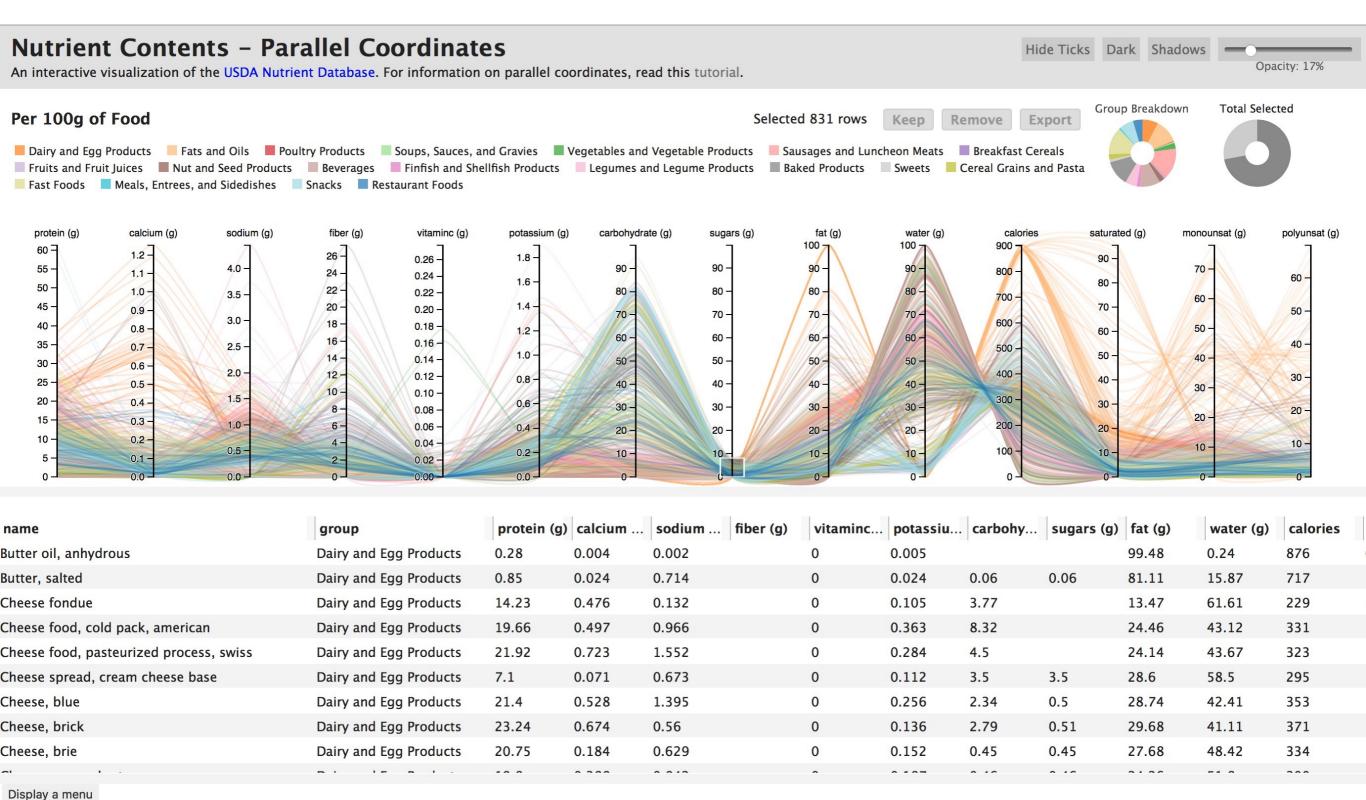


Figure 5: Common patterns in Cartesian coordinates (top) and their dual representation in parallel coordinates (bottom). The envelope of lines is highlighted for the ellipse-hyperbola duality.

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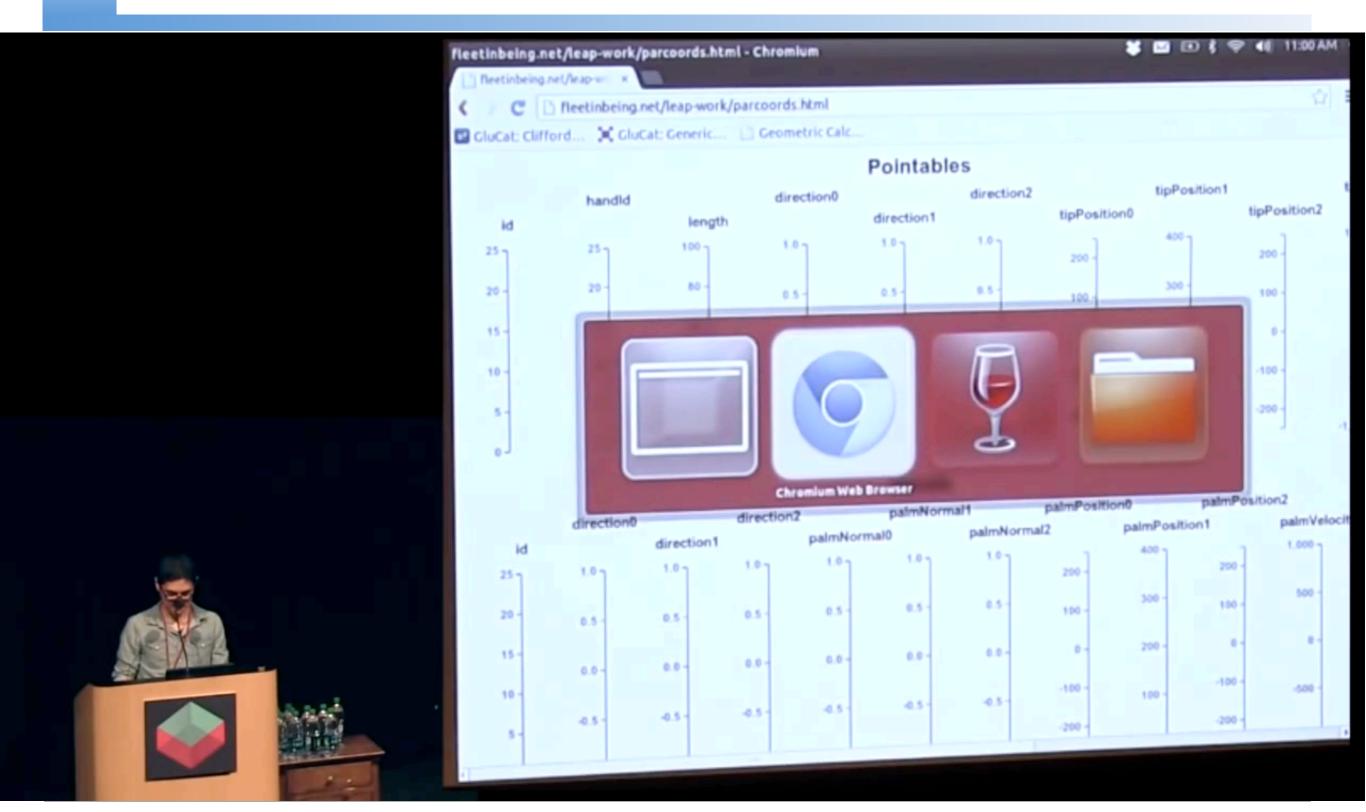
http://bl.ocks.org/syntagmatic/raw/3150059/



Kai Chang

Visually Exploring Multidimensional Data

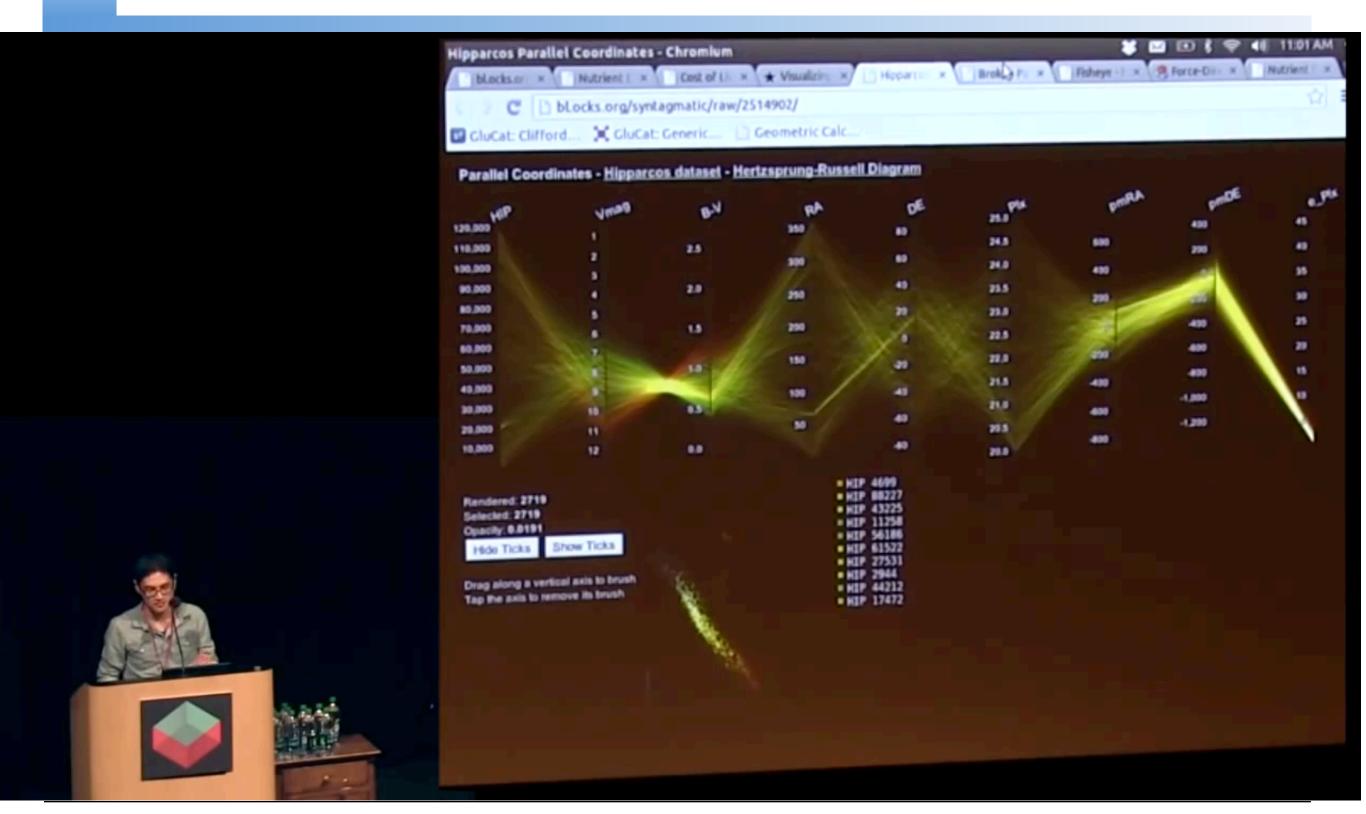












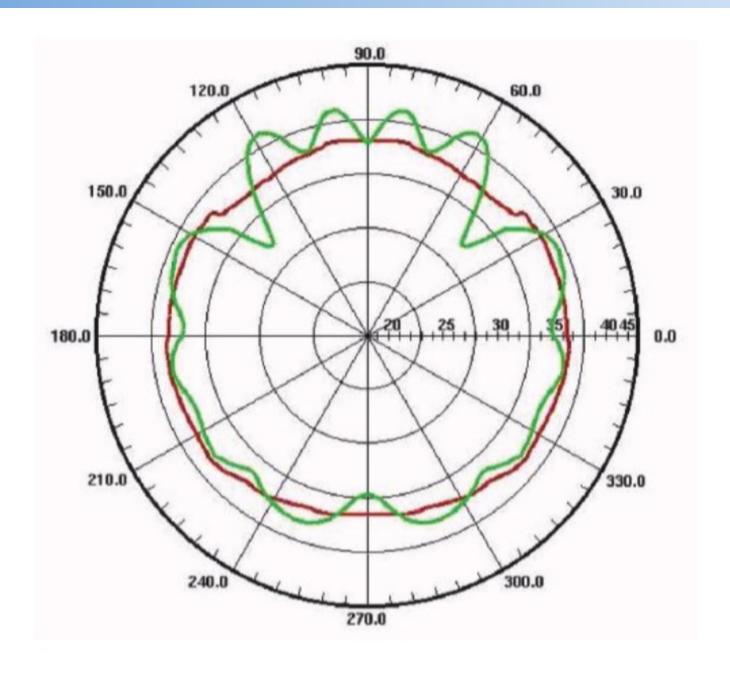


- A brief tutorial on ||-coords (https://eagereyes.org/techniques/parallel-coordinates)
- A D3 library (<u>https://syntagmatic.github.io/parallel-coordinates/</u>)
- Some very special videos, from Alfred Inselberg's tutorial at iV 2016, at Lisbon (<u>FB</u> and <u>Twitter</u>):
 - Part1
 - Part 2
 - Part 3



- Radial Axis Techniques
 - circular line graph;
 - polar graphs: point plots using polar coordinates;
 - circular bar charts: like circular line graphs, but plotting bars on the base line;
 - circular area graphs: like a line graph, but with the area under line filled in with a color or texture;
 - circular bar graphs: with bars that are circular arcs with a common center point and base line.

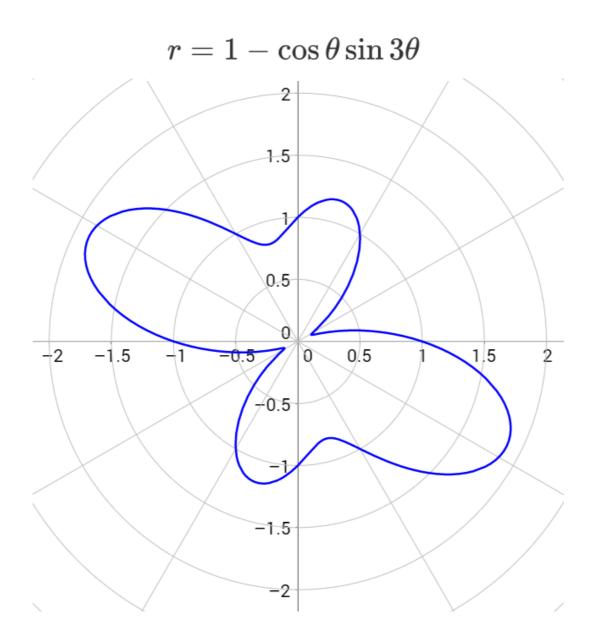




An example of a circular line graph. (Image courtesy http://www.cemframework .com/img/PolarPlot1.png.)



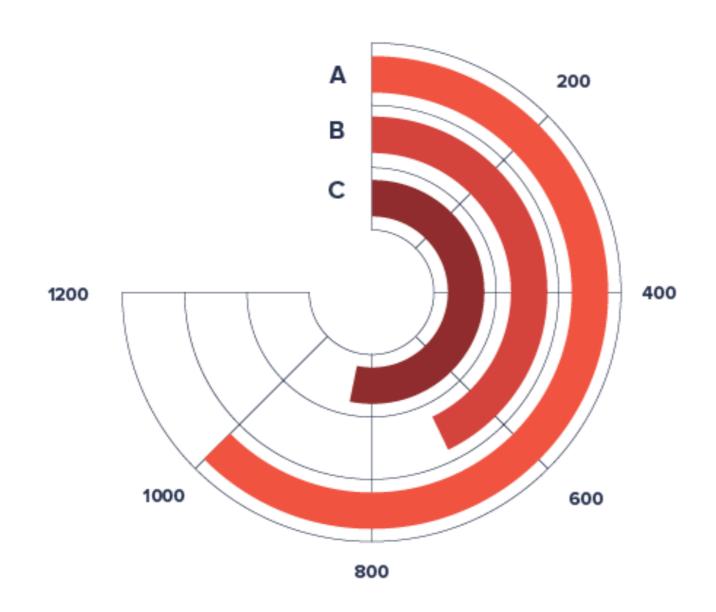
polar graphs - point plots using polar coordinates



https://brilliant.org/wiki/polar-curves/

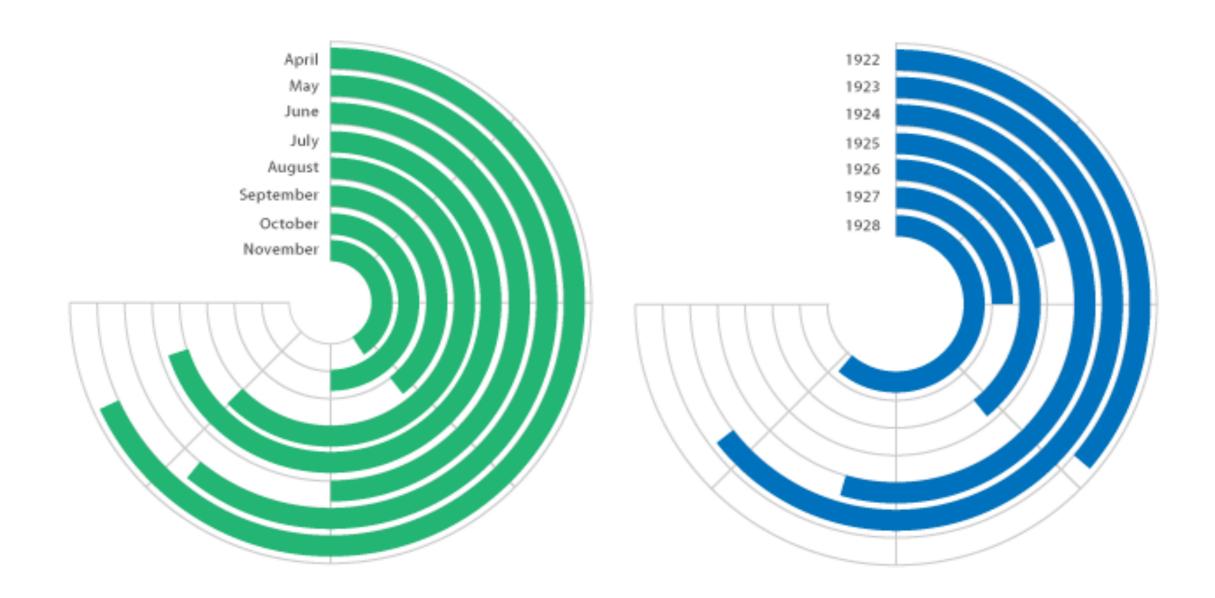


circular bar charts: like circular line graphs, but plotting bars on the base line





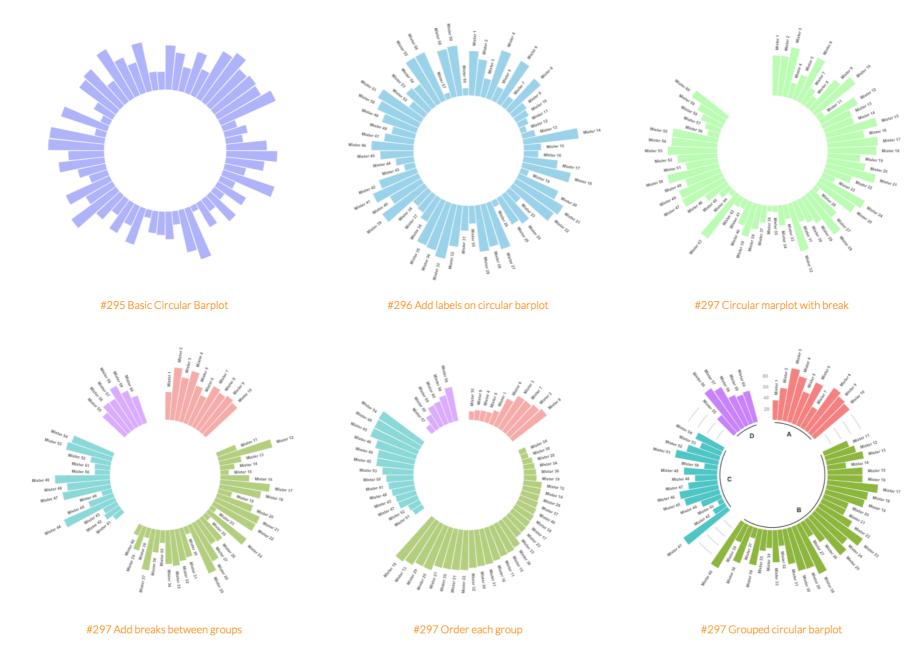
circular bar charts: like circular line graphs, but plotting bars on the base line



https://datavizcatalogue.com/methods/radial bar chart.html

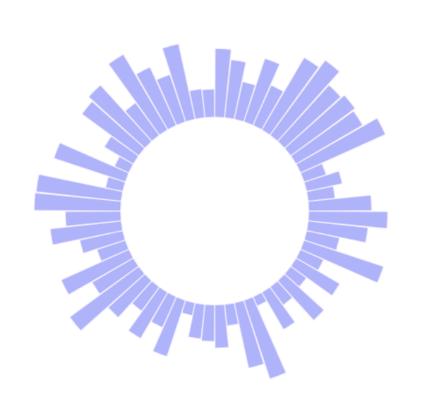


circular bar graphs: with bars that are circular arcs with a common center point and base line.

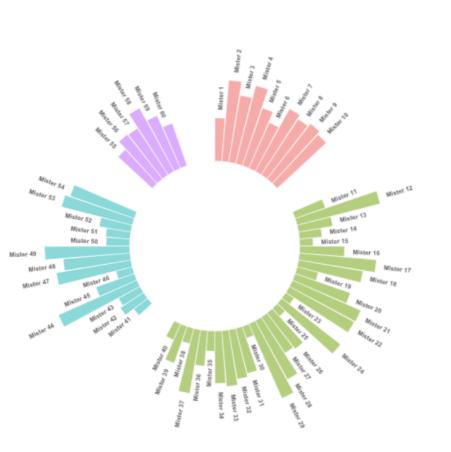


https://www.r-graph-gallery.com/circular-barplot/





#295 Basic Circular Barplot



Mister 45

Mister 47

Mister 43

Mister 42

Mister 42

Mister 42

Mister 41

Mister 42

Mister 42

Mister 43

Mister 43

Mister 44

Mister 47

Mister 40

Mister 41

Mister 42

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Mister 44

Mister 47

Mister 42

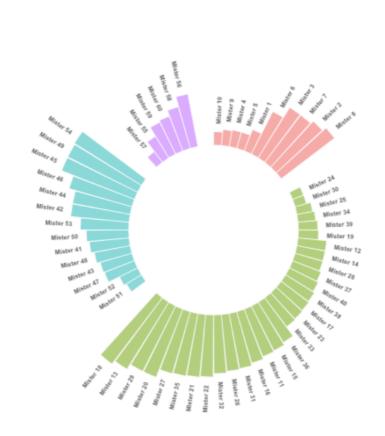
Mister 43

Mister 44

Mister 47

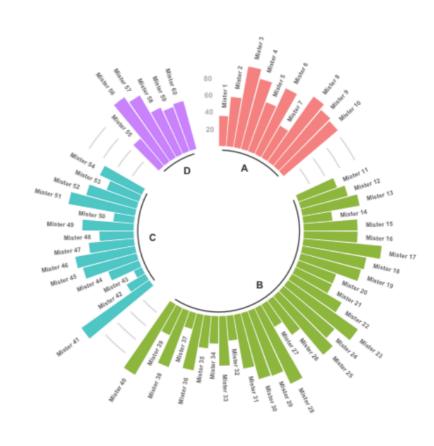
Mister 40

#296 Add labels on circular barplot



Mister 53
Mister 52
Mister 51
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Mister

#297 Circular marplot with break

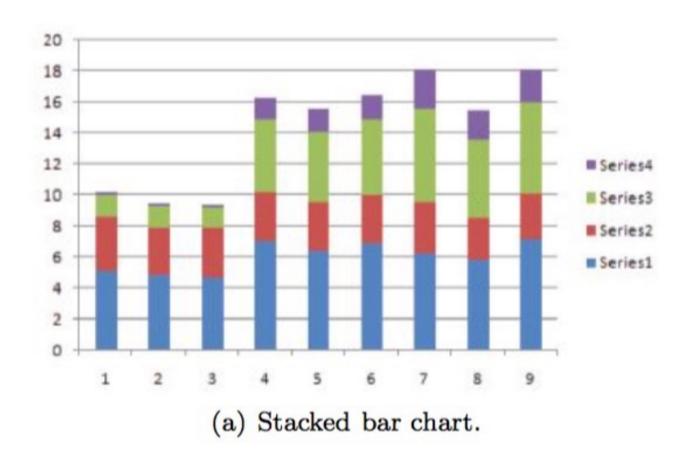


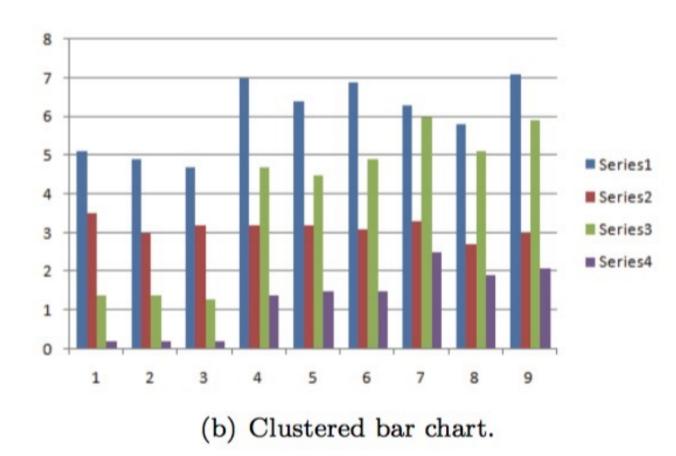
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Region-Based Techniques

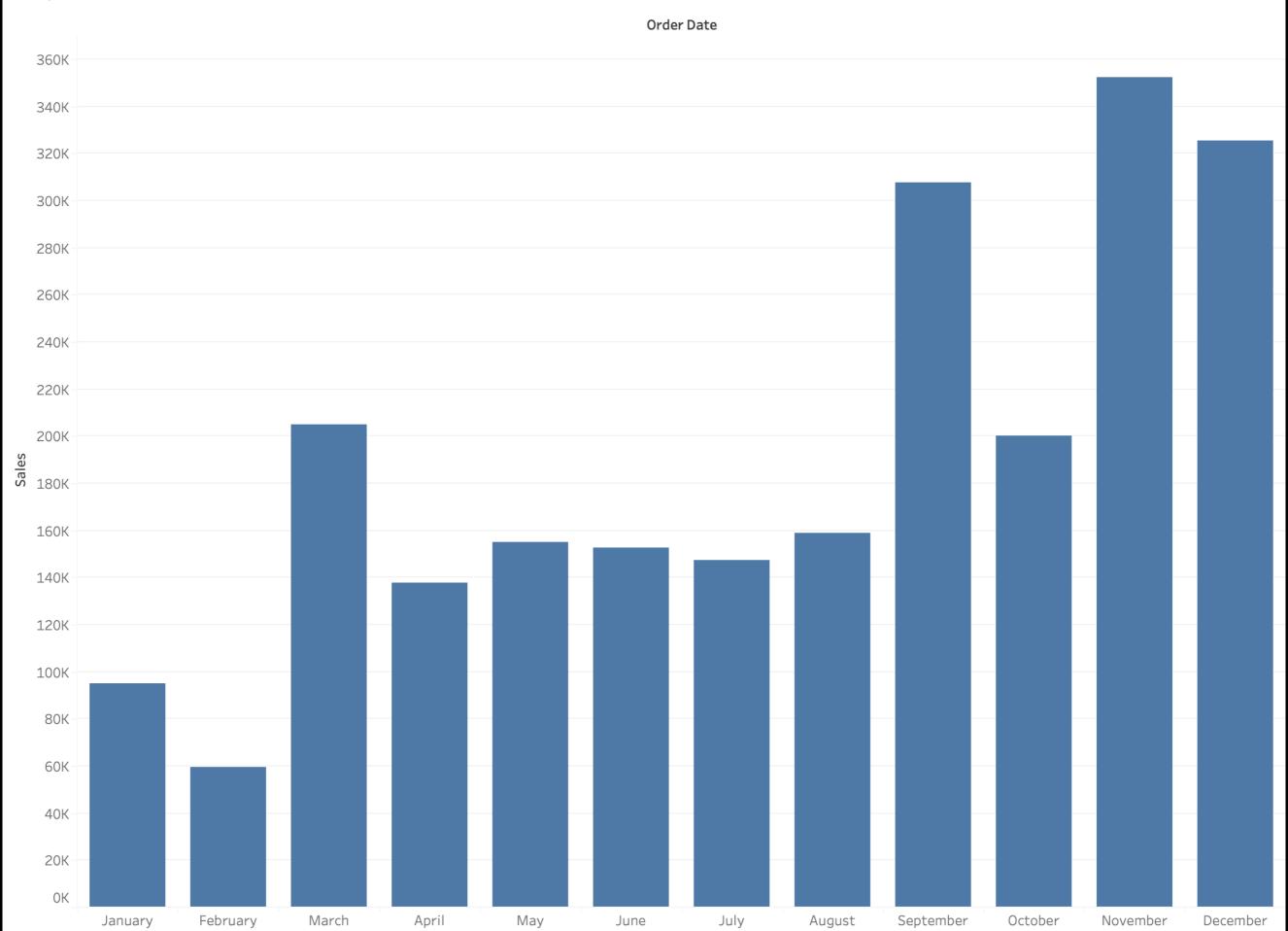


Bar Charts and Area Charts



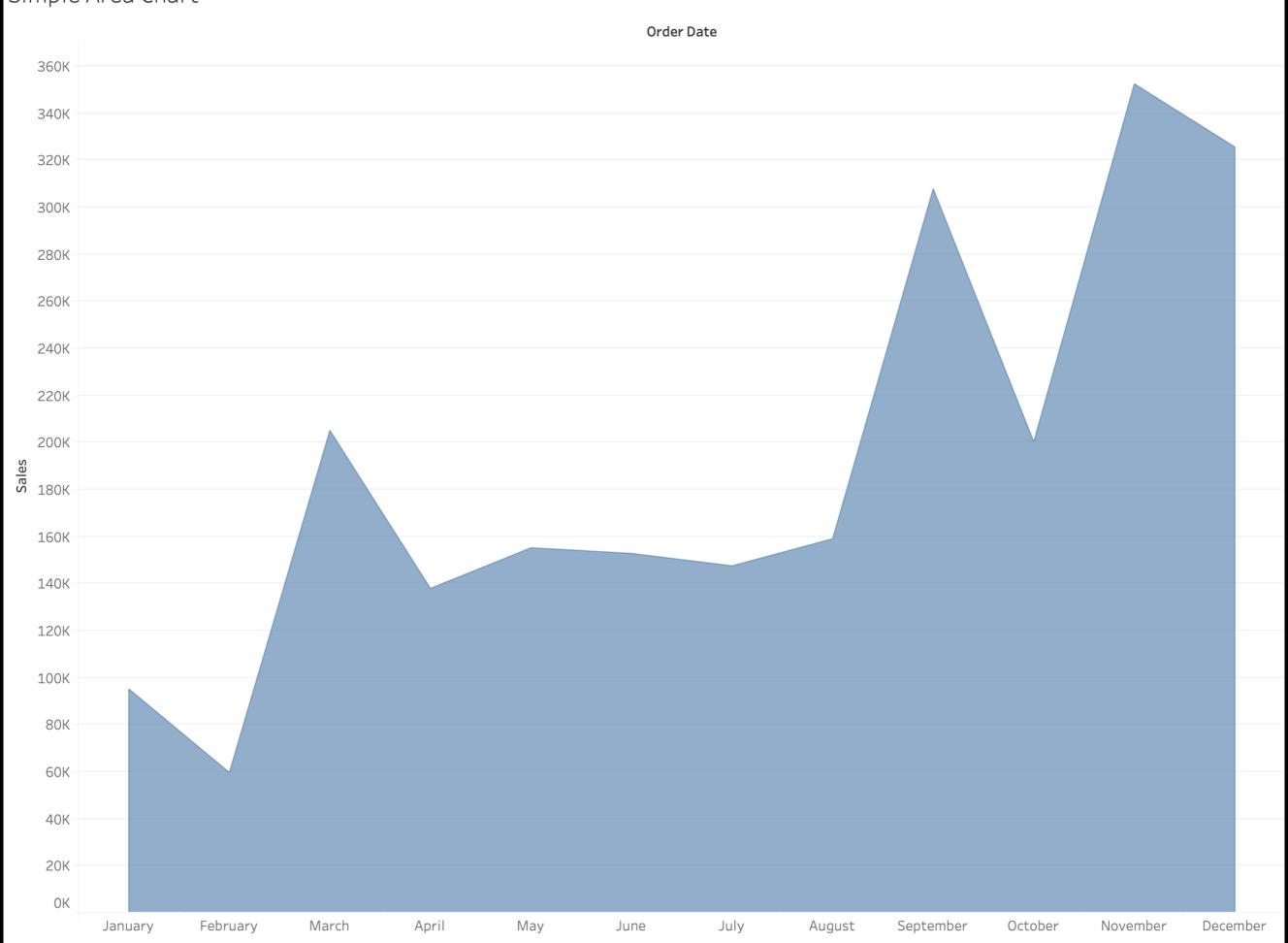




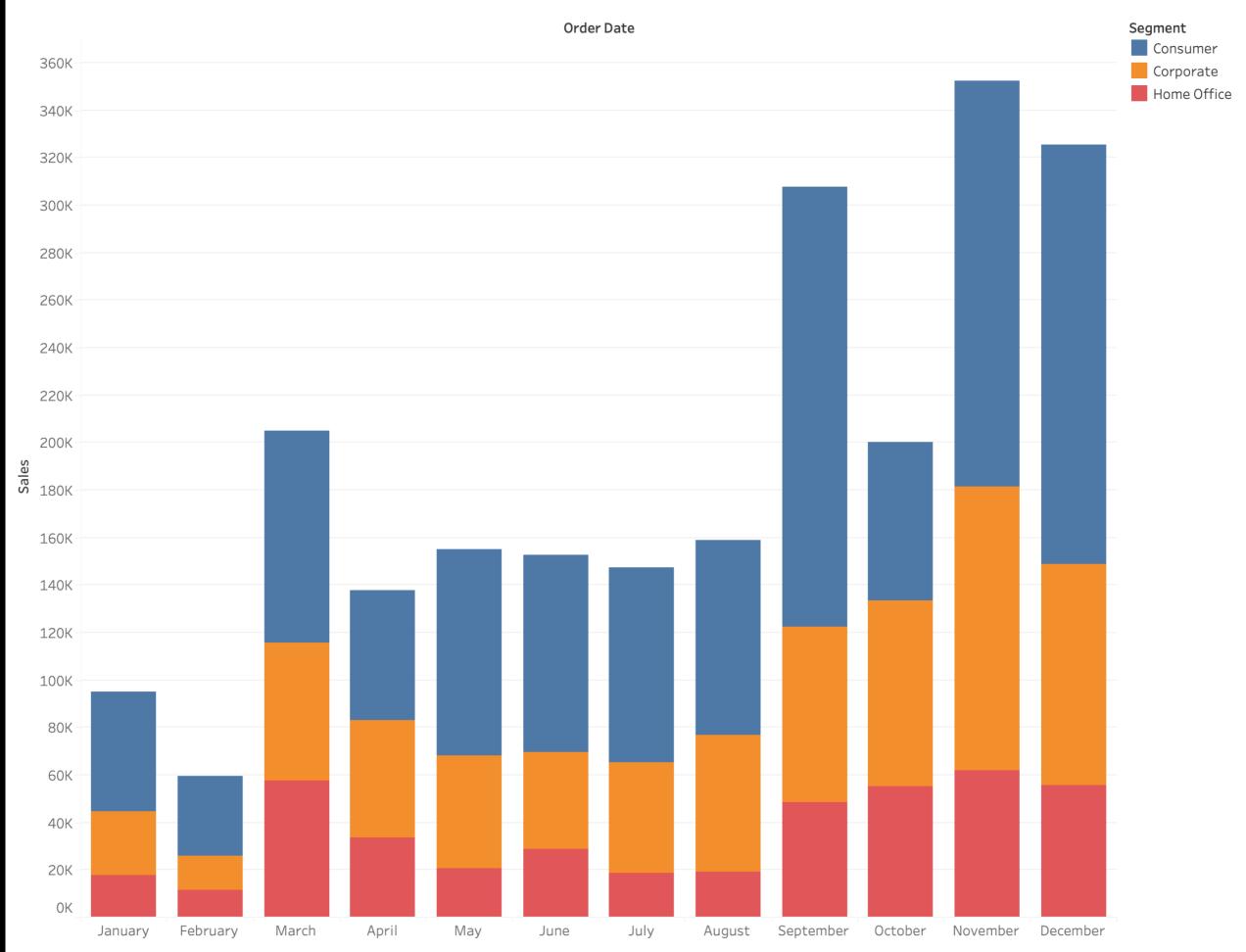


Sum of Sales for each Order Date Month.

Simple Area Chart

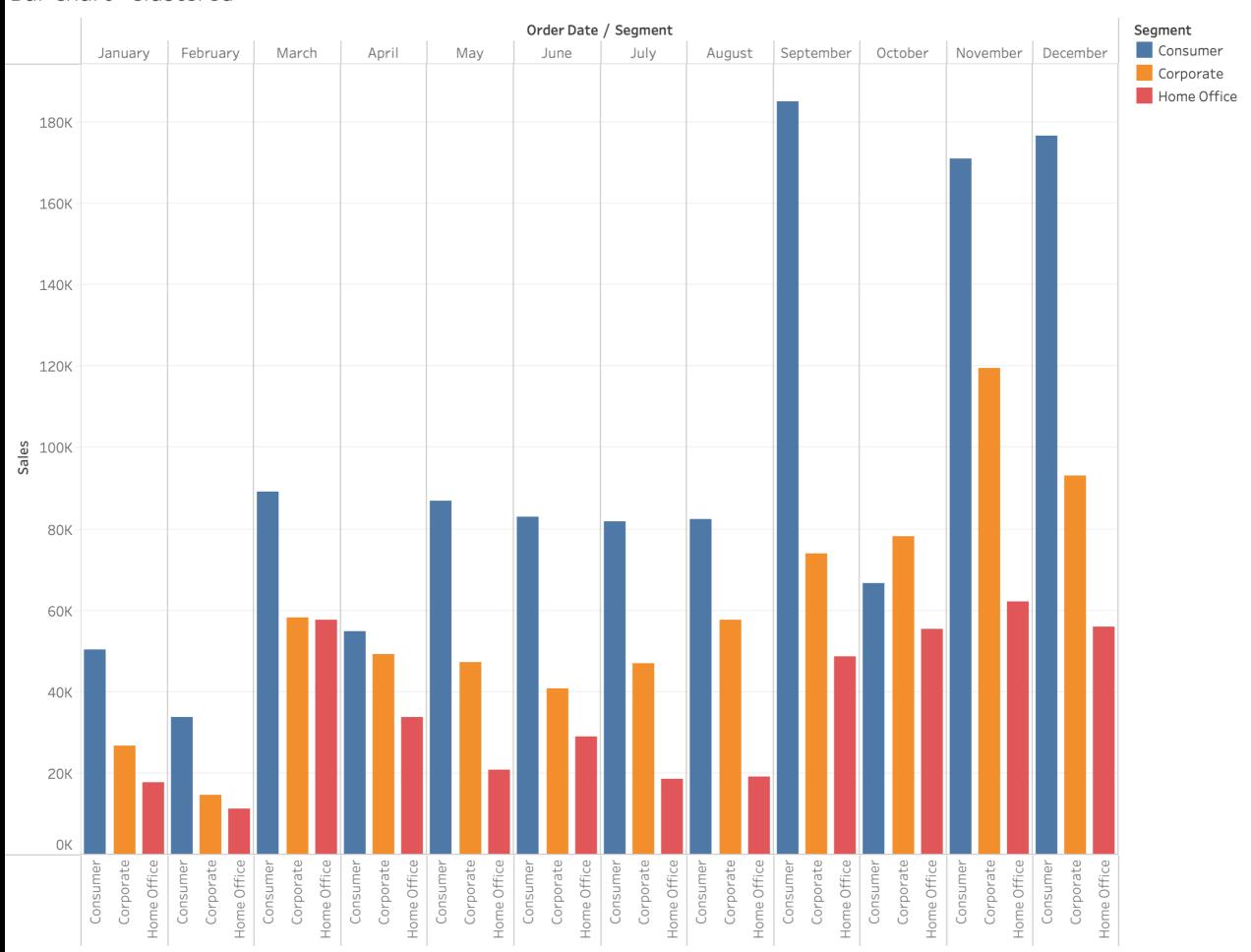


Sum of Sales for each Order Date Month.

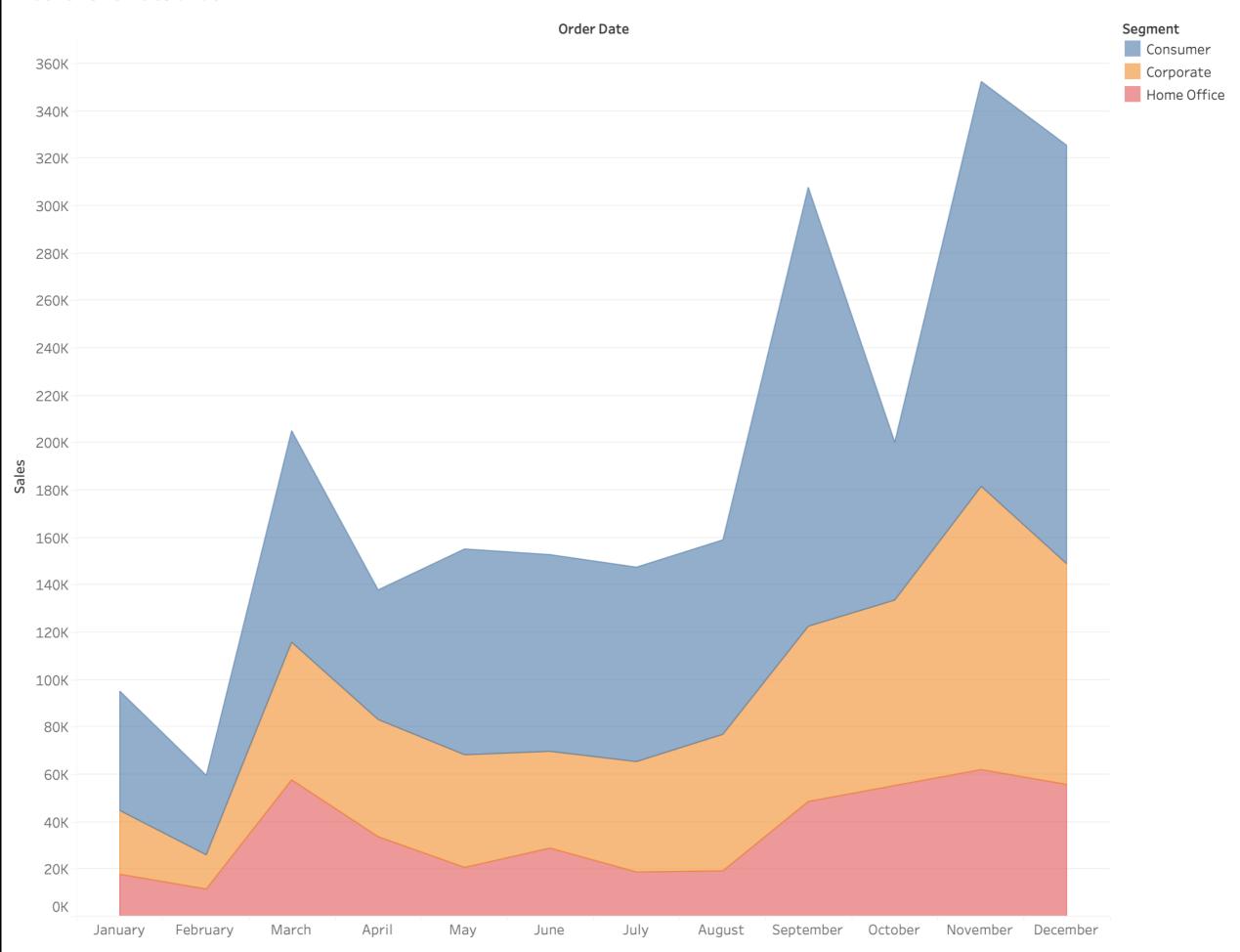


Sum of Sales for each Order Date Month. Color shows details about Segment.

Bar Chart - Clustered

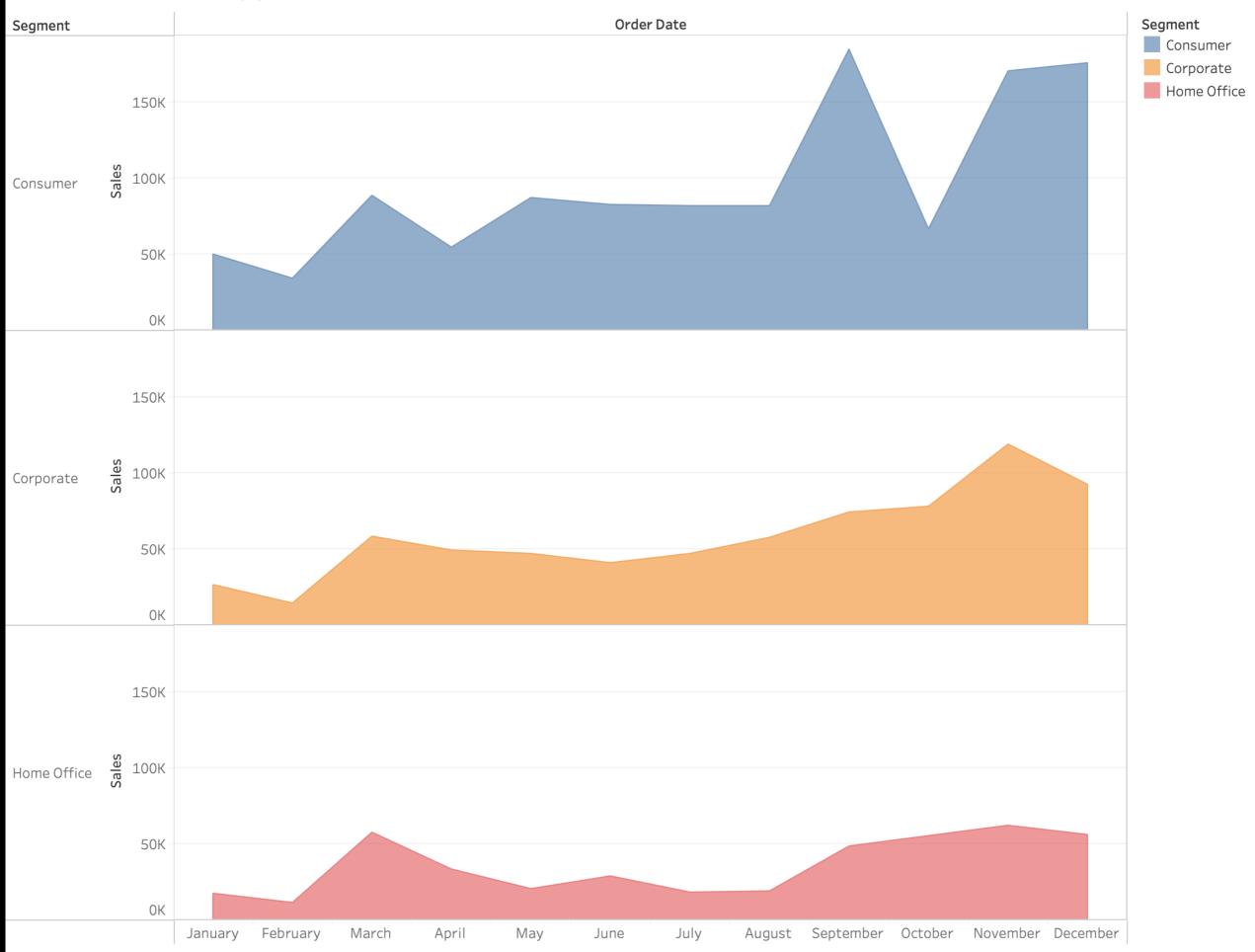


Sum of Sales for each Segment broken down by Order Date Month. Color shows details about Segment.

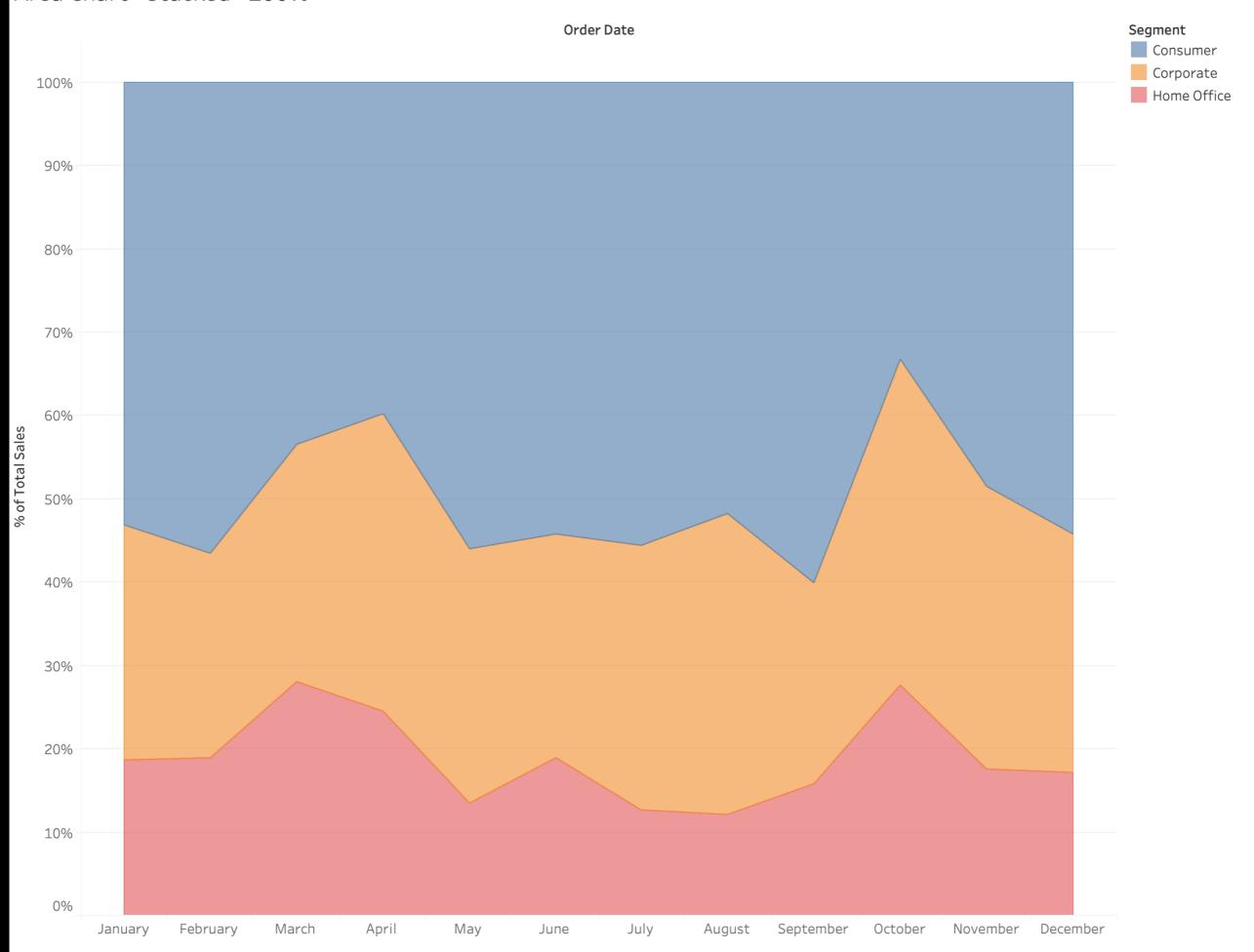


Sum of Sales for each Order Date Month. Color shows details about Segment.

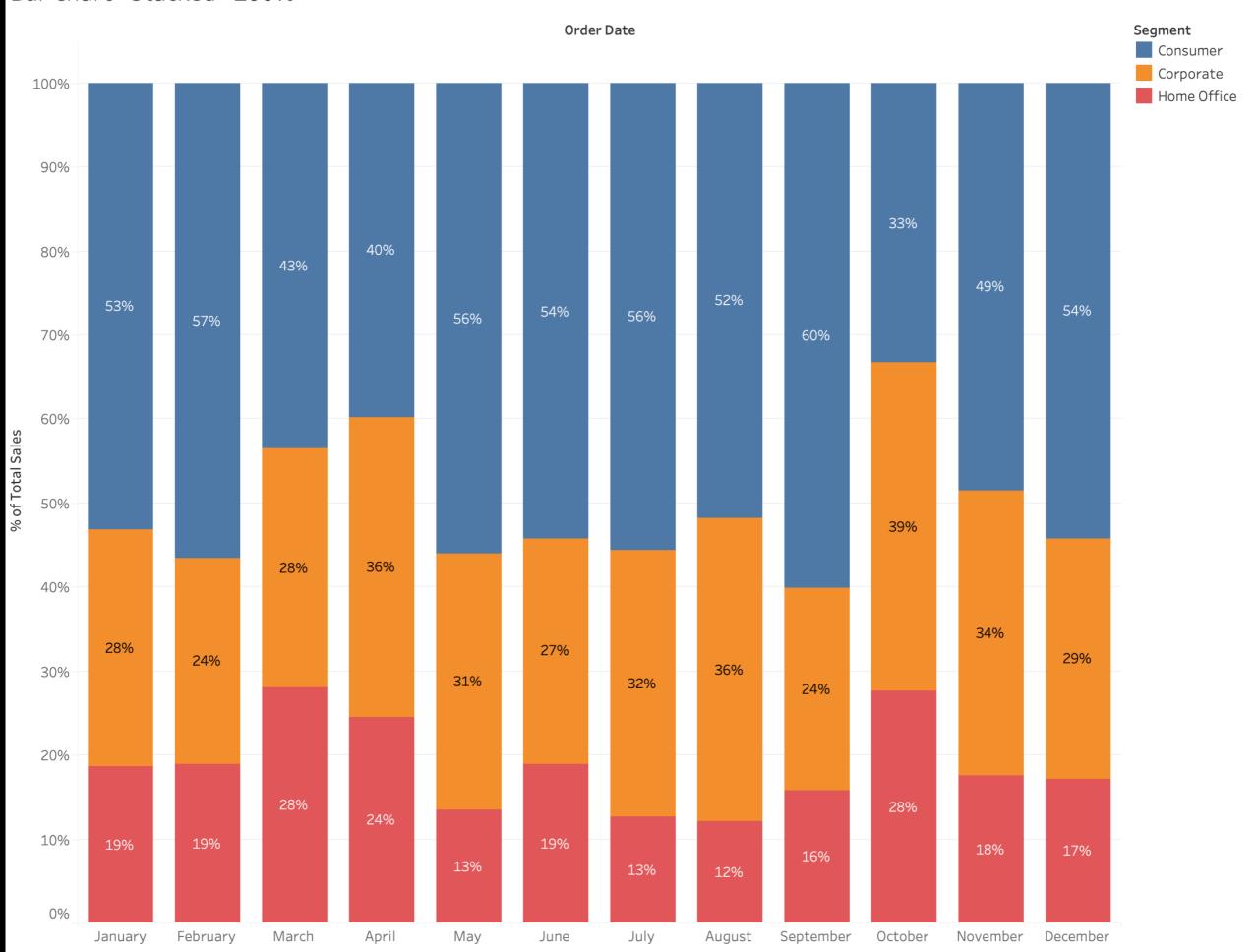
Area Chart - Stacked (2)



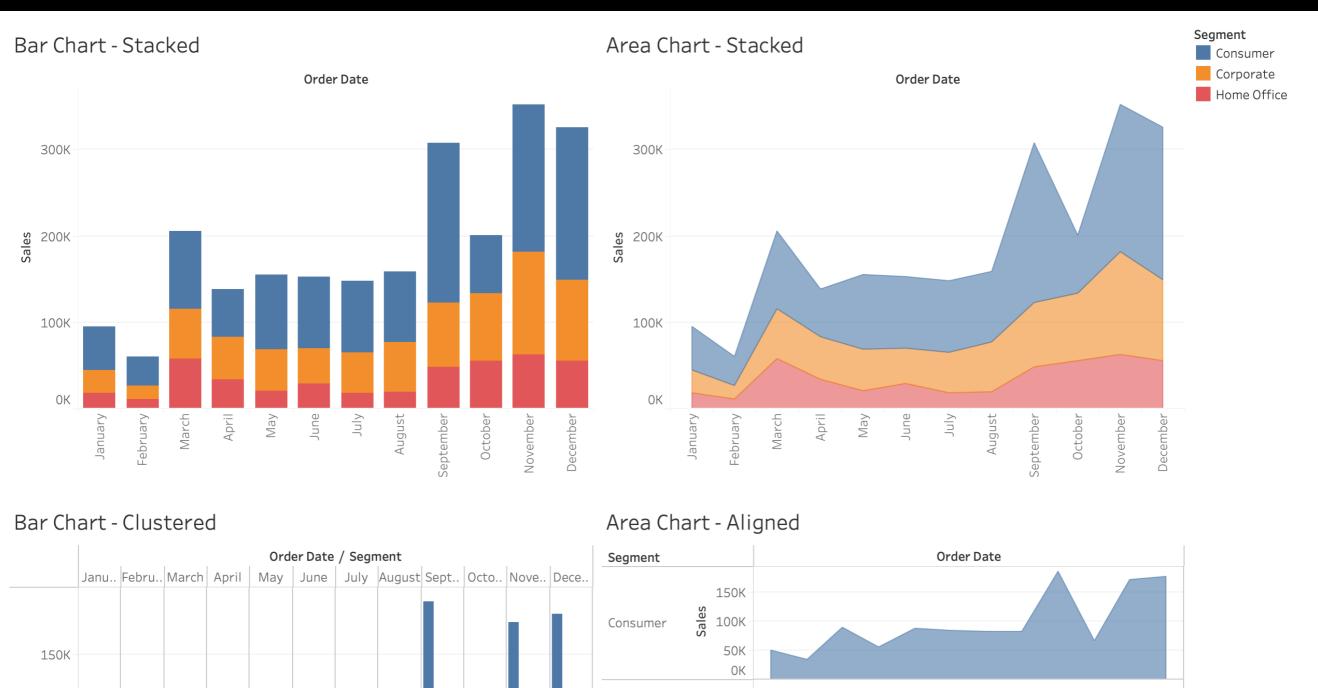
Sum of Sales for each Order Date Month broken down by Segment. Color shows details about Segment.

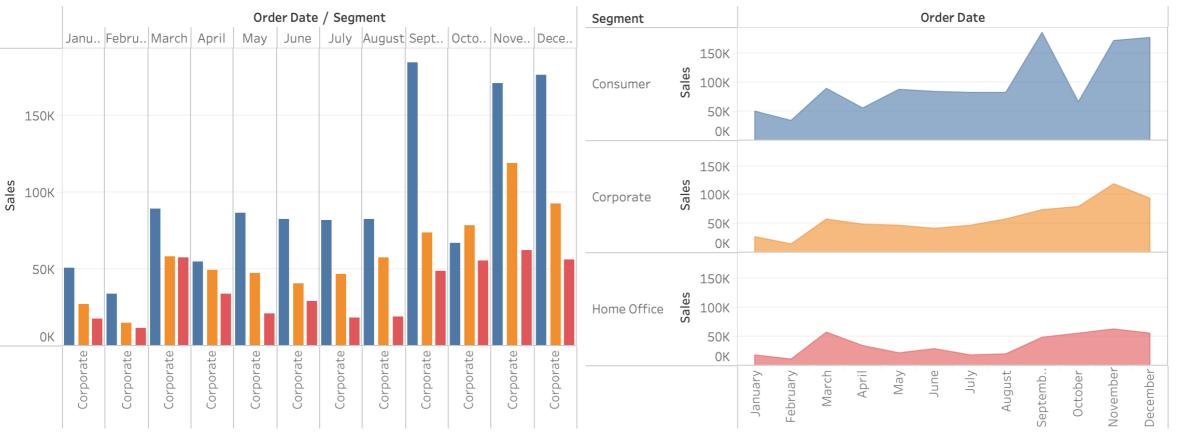


% of Total Sales for each Order Date Month. Color shows details about Segment.

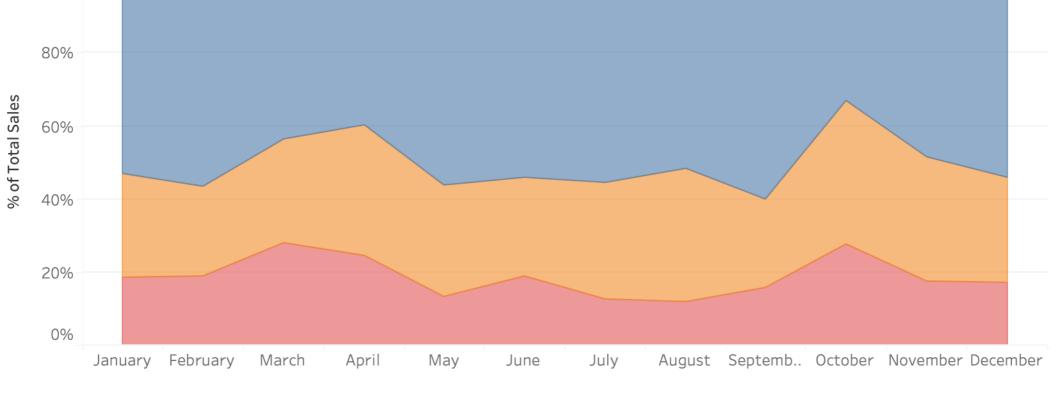


% of Total Sales for each Order Date Month. Color shows details about Segment.

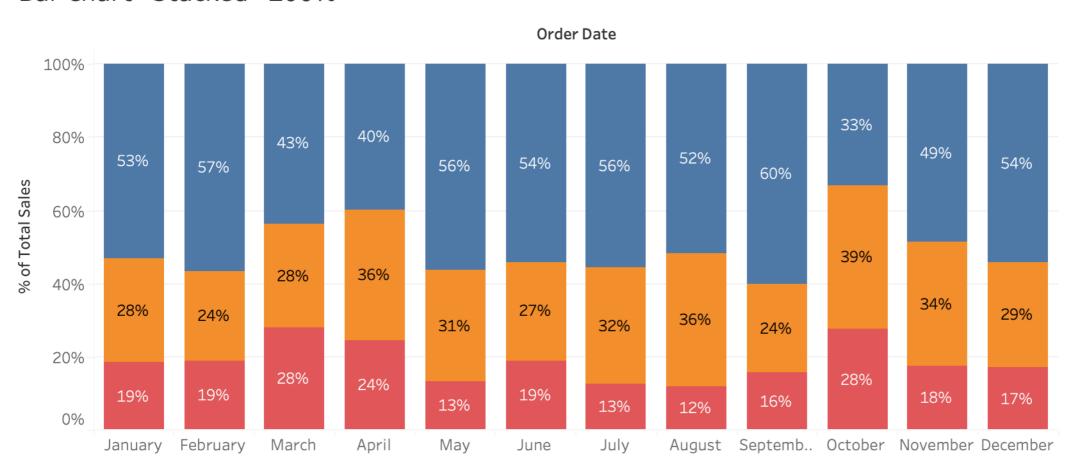




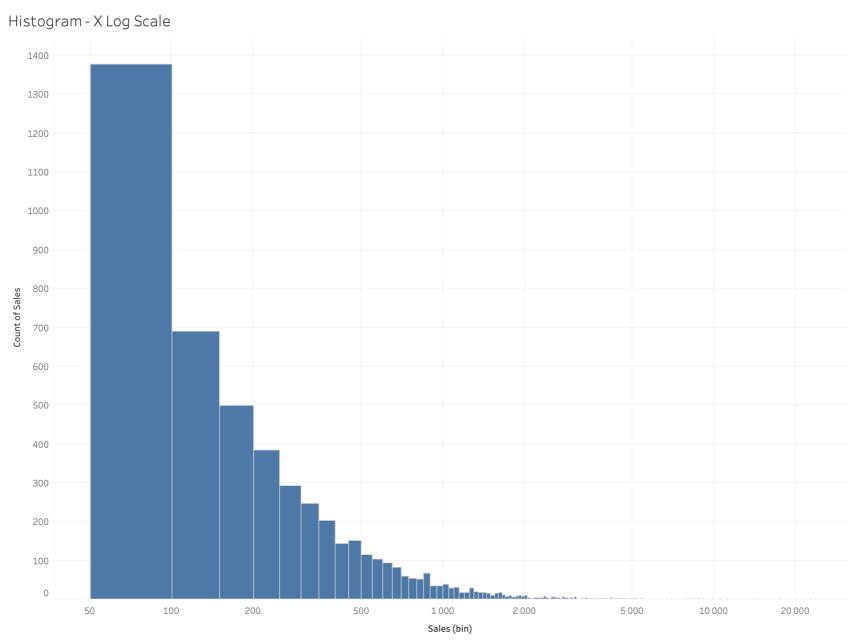




Bar Chart - Stacked - 100%

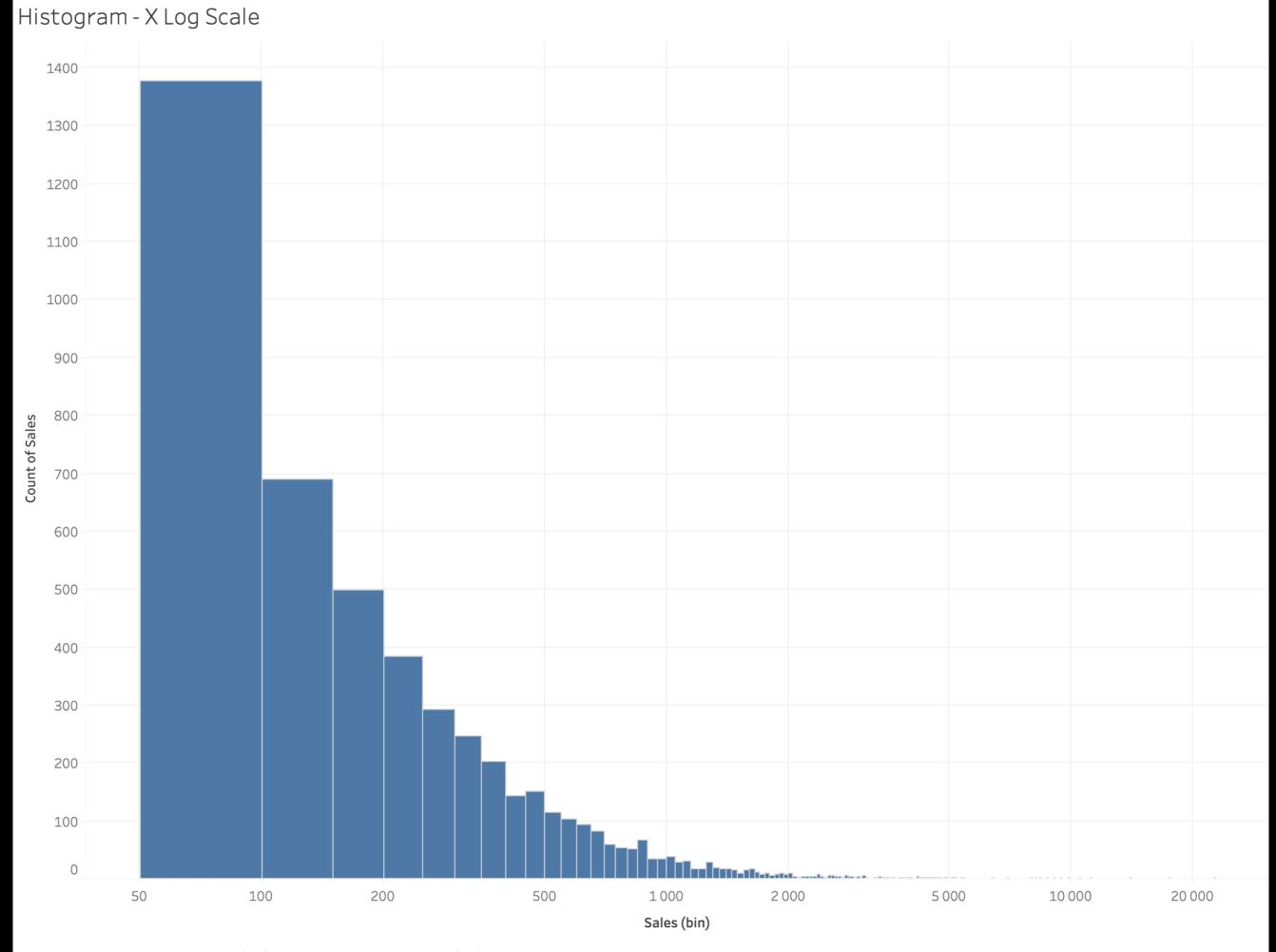


Histogram for continuous variables

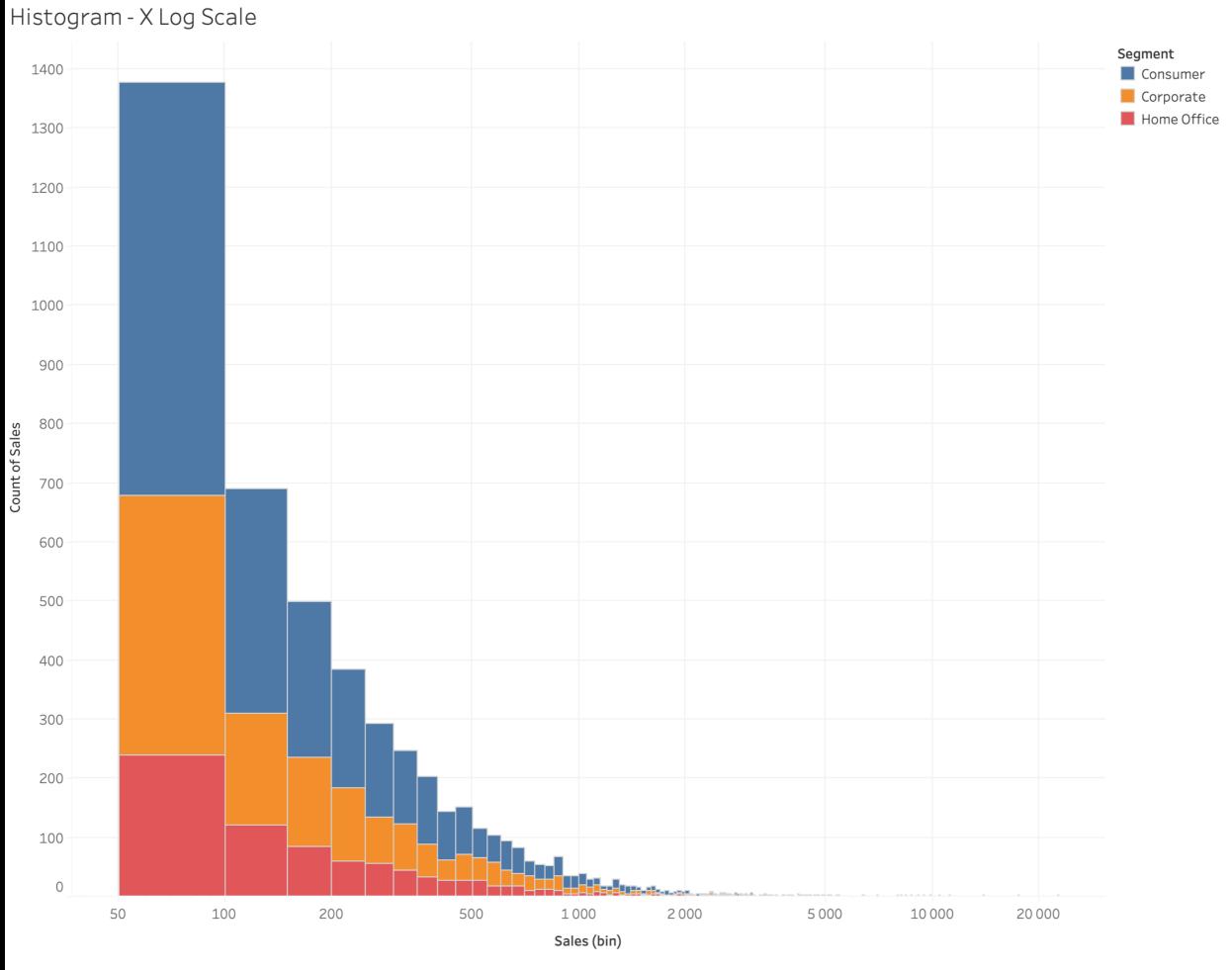


The trend of count of Sales for Sales (bin). The view is filtered on Sales (bin), which includes greater than and or equal to 2,225073859e-308 and keeps Null values



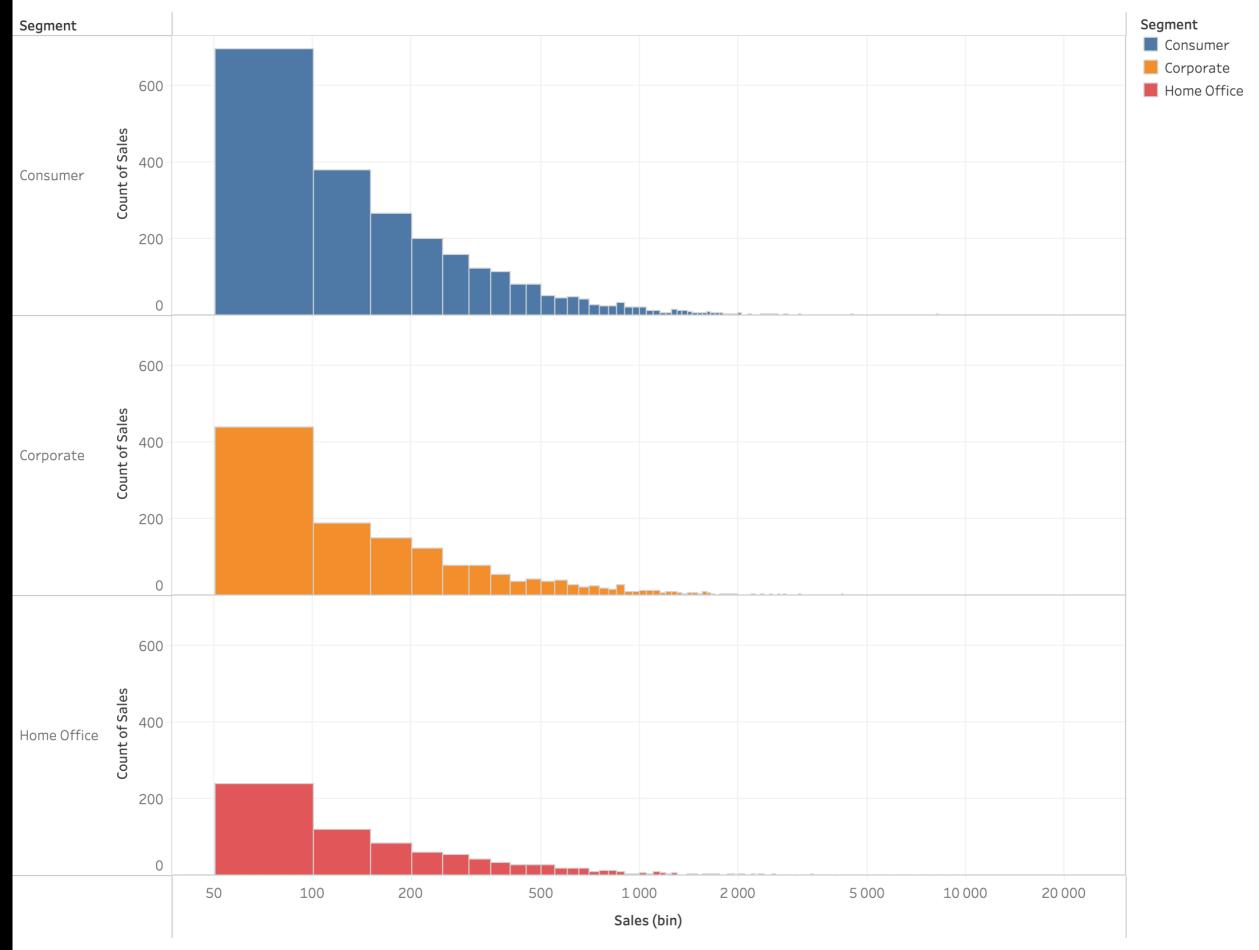


The trend of count of Sales for Sales (bin). The view is filtered on Sales (bin), which includes greater than and or equal to 2,225073859e-308 and keeps Null values.



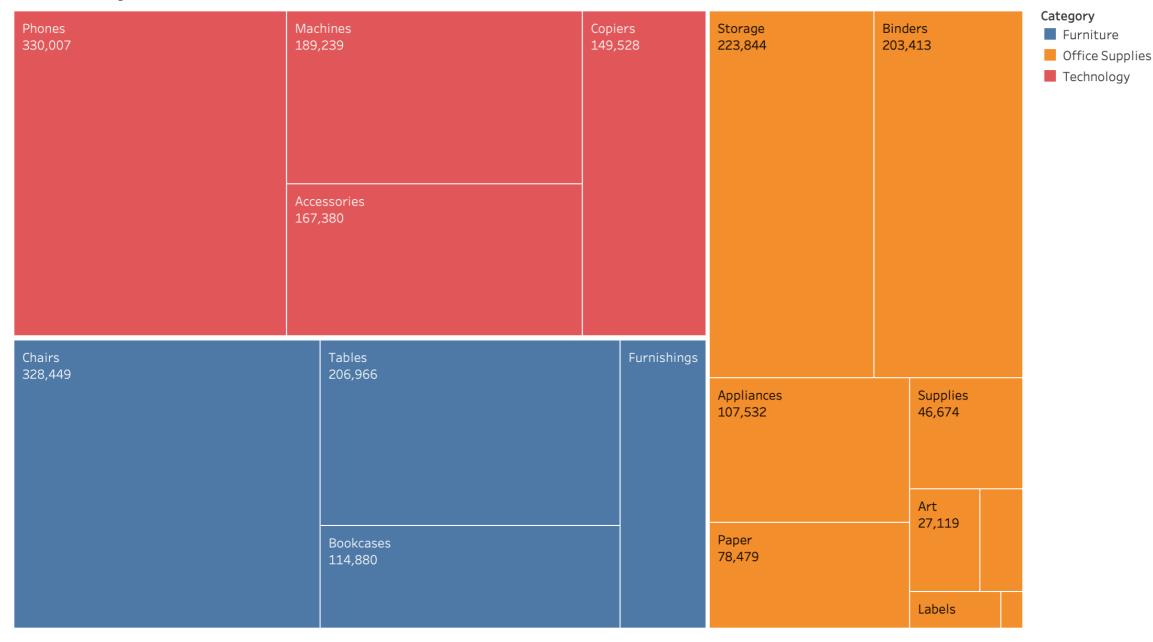
The trend of count of Sales for Sales (bin). Color shows details about Segment. The view is filtered on Sales (bin), which includes greater than and or equal to 2,225073859e-308 and keeps Null values.

Histogram - X Log Scale



The trend of count of Sales for Sales (bin) broken down by Segment. Color shows details about Segment. The view is filtered on Sales (bin), which includes greater than and or equal to 2,225073859e-308 and keeps Null values.

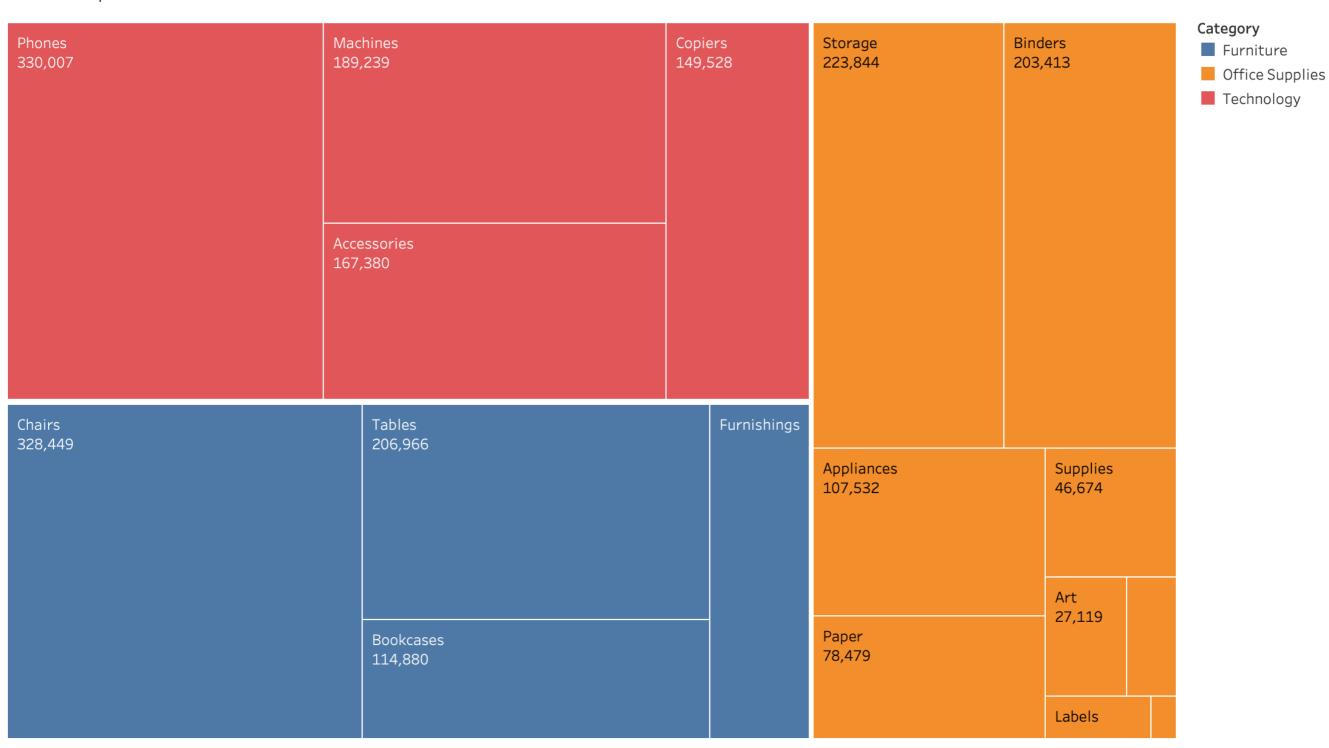
Tree Maps



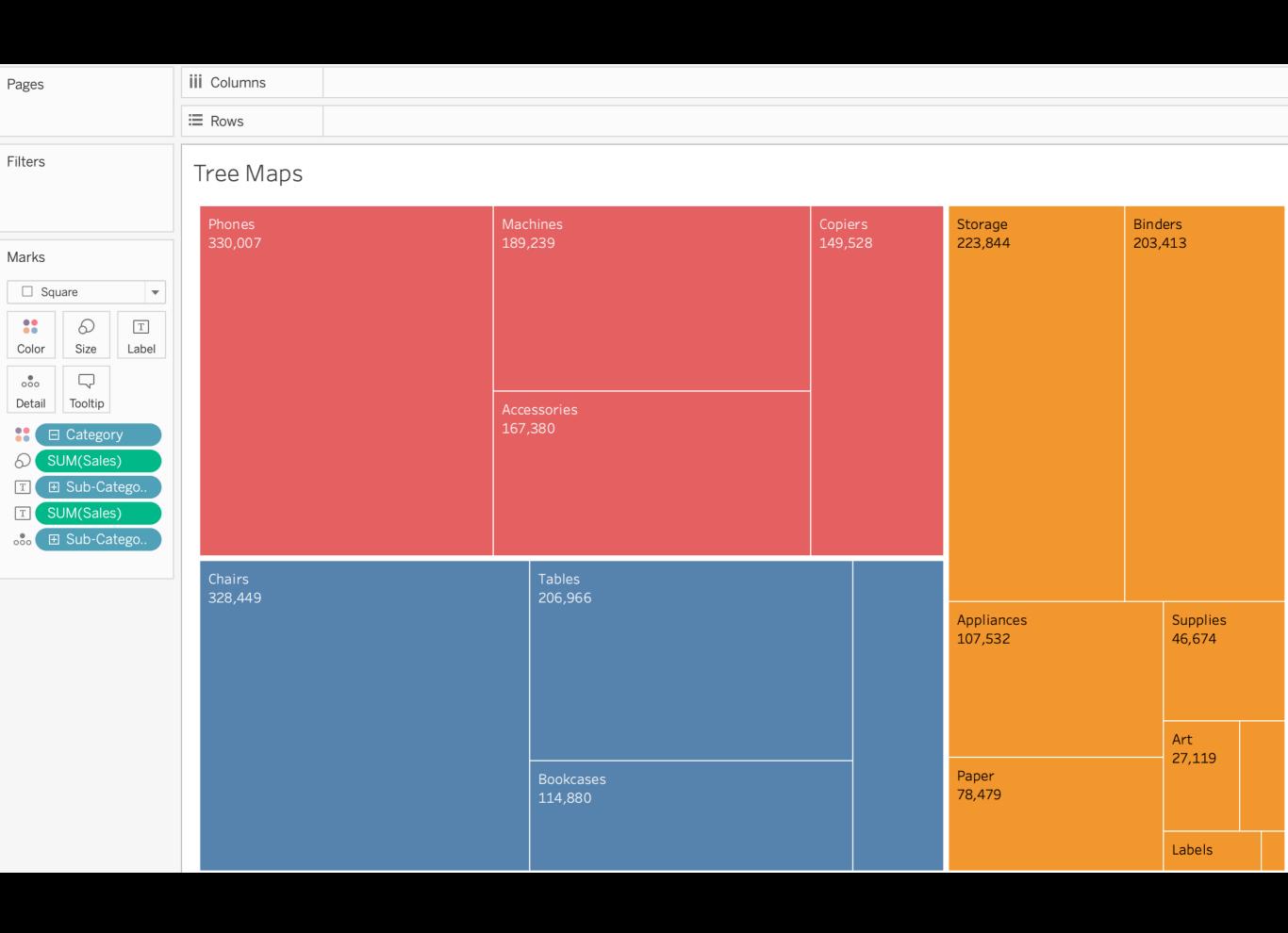
Sub-Category and sum of Sales. Color shows details about Category. Size shows sum of Sales. The marks are labeled by Sub-Category and sum of Sales. Details are shown for Sub-Category.

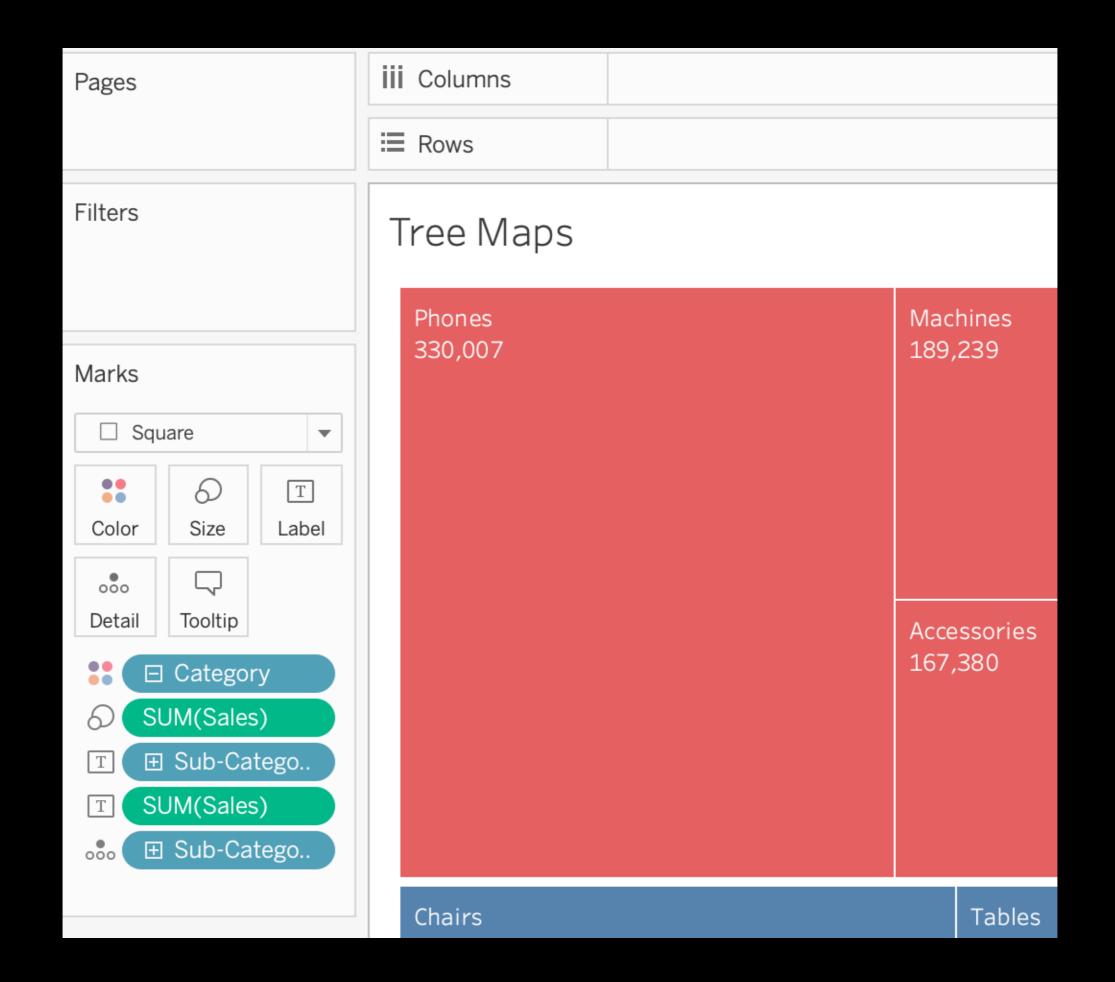


Tree Maps

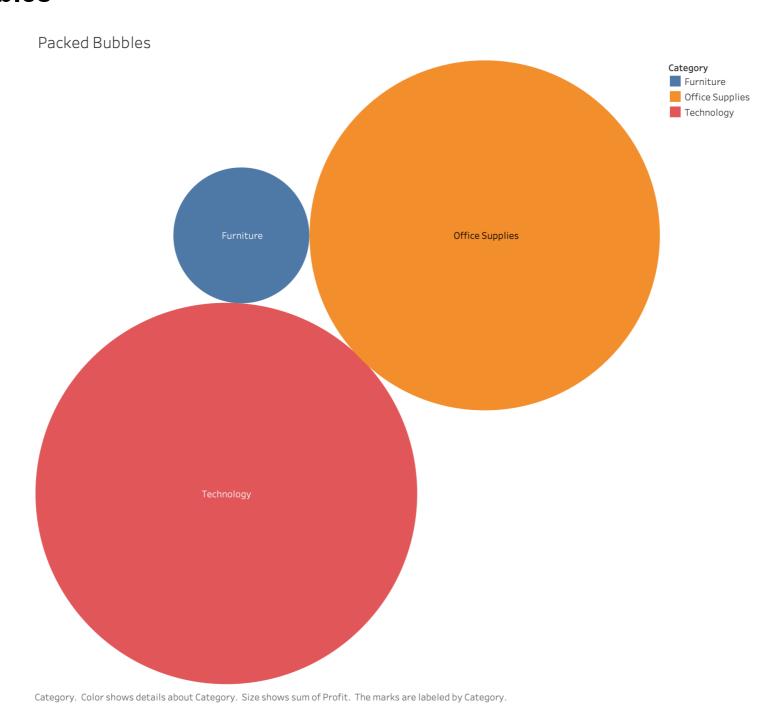


Sub-Category and sum of Sales. Color shows details about Category. Size shows sum of Sales. The marks are labeled by Sub-Category and sum of Sales. Details are shown for Sub-Category.

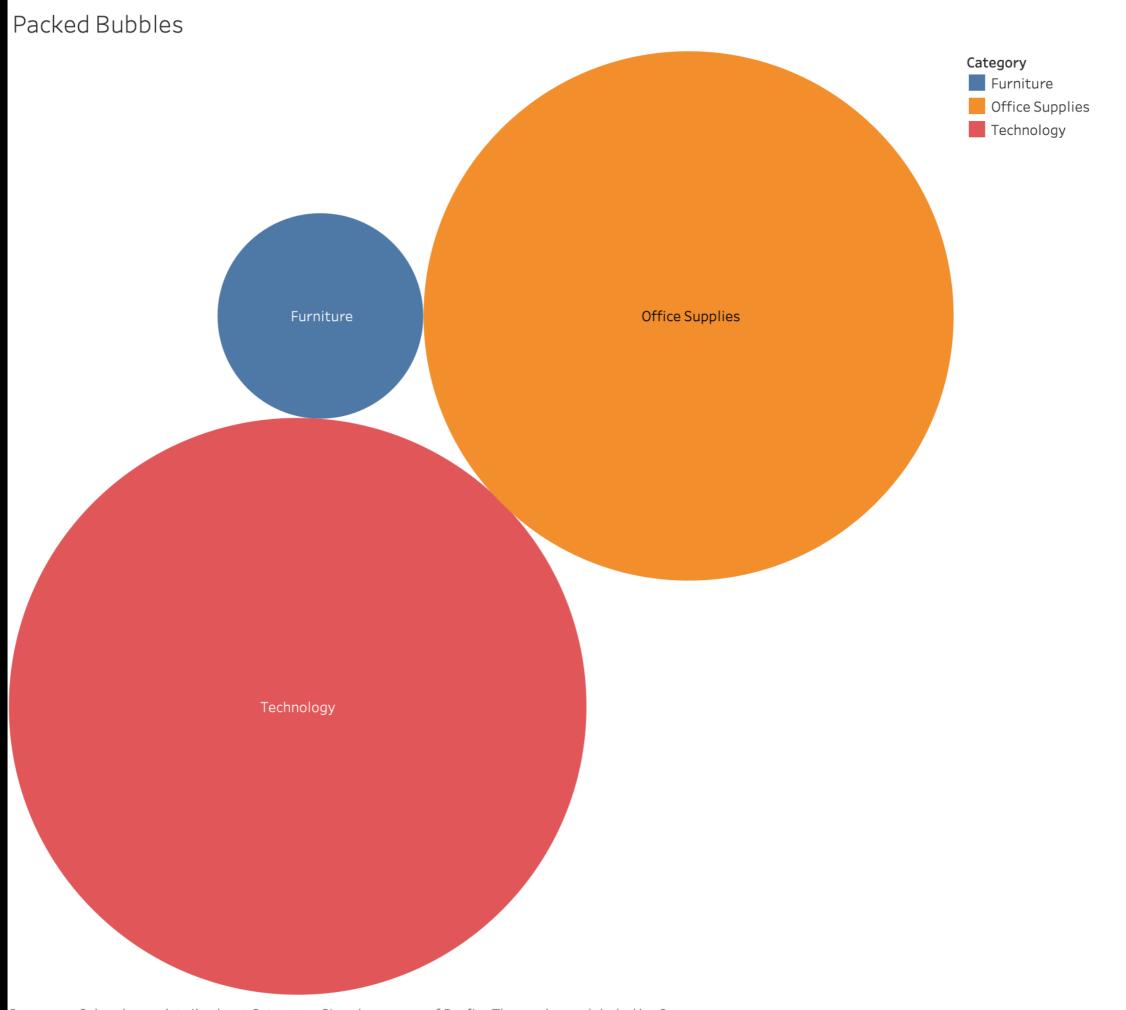




Stacked Bubbles



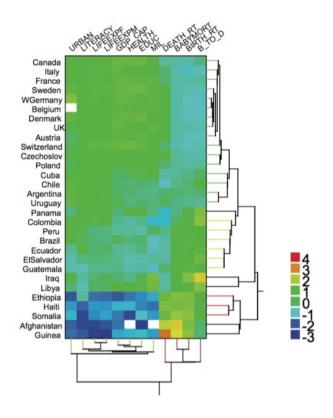




Category. Color shows details about Category. Size shows sum of Profit. The marks are labeled by Category.

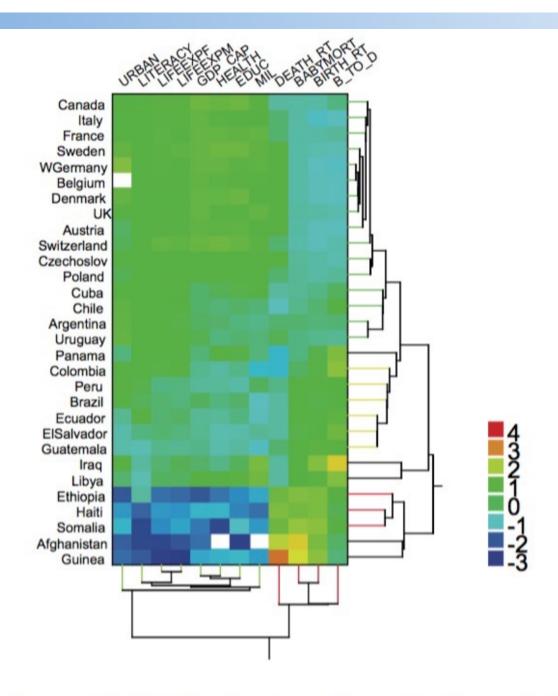
Tabular Displays

Heatmaps are created by displaying the table of record values using color rather than text. All data values are mapped to the same normalized color space, and each is rendered as a colored square or rectangle.



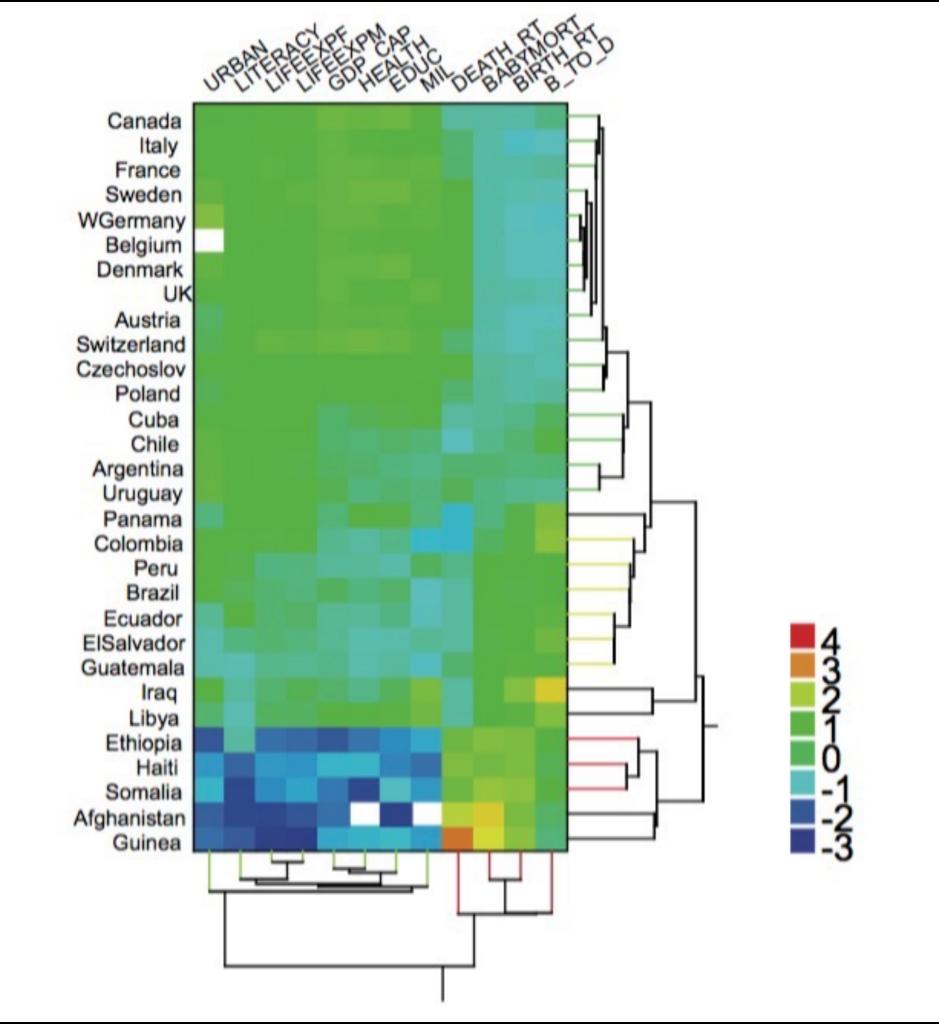
A heatmap showing social statistics for several countries from a U.N. survey. Rows and columns have been reordered via clustering. (Image courtesy Leland Wilkinson [459].)





A heatmap showing social statistics for several countries from a U.N. survey. Rows and columns have been reordered via clustering. (Image courtesy Leland Wilkinson [459].)





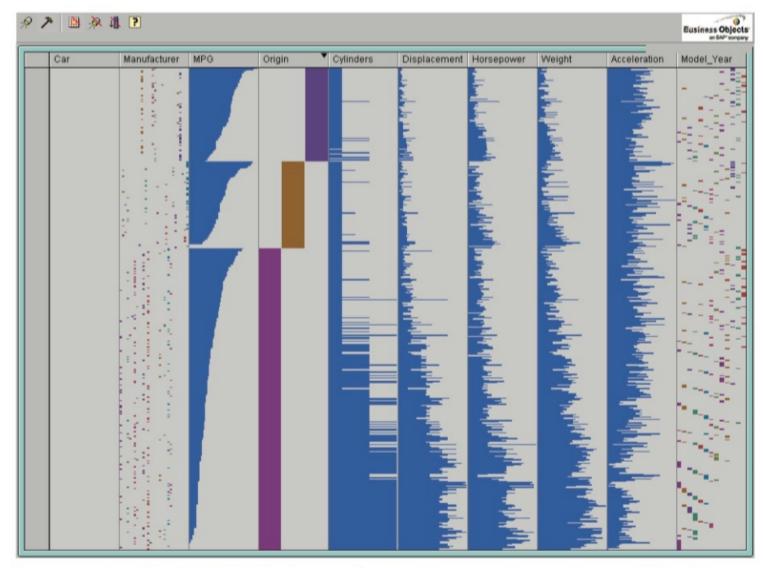
Heat Table

		Segment		Sales	
Sub-Category	Consumer	Corporate	Home Office		
Phones	169,933	91,153	68,921	560	172,863
Chairs	172,863	99,141	56,445		
Storage	100,492	79,791	43,560		
Tables	99,934	70,872	36,160		
Binders	118,161	51,560	33,691		
Machines	79,543	60,277	49,419		
Accessories	87,105	48,191	32,085		
Copiers	69,819	46,829	32,880		
Bookcases	68,633	34,006	12,241		
Appliances	52,820	36,589	18,124		
Furnishings	49,620	25,001	17,084		
Paper	36,324	23,883	18,272		
Supplies	25,741	19,435	1,497		
Art	14,252	8,590	4,276		
Envelopes	7,771	5,943	2,763		
Labels	6,709	4,102	1,675		
Fasteners	1,681	783	560		

Sum of Sales (color) broken down by Segment vs. Sub-Category.

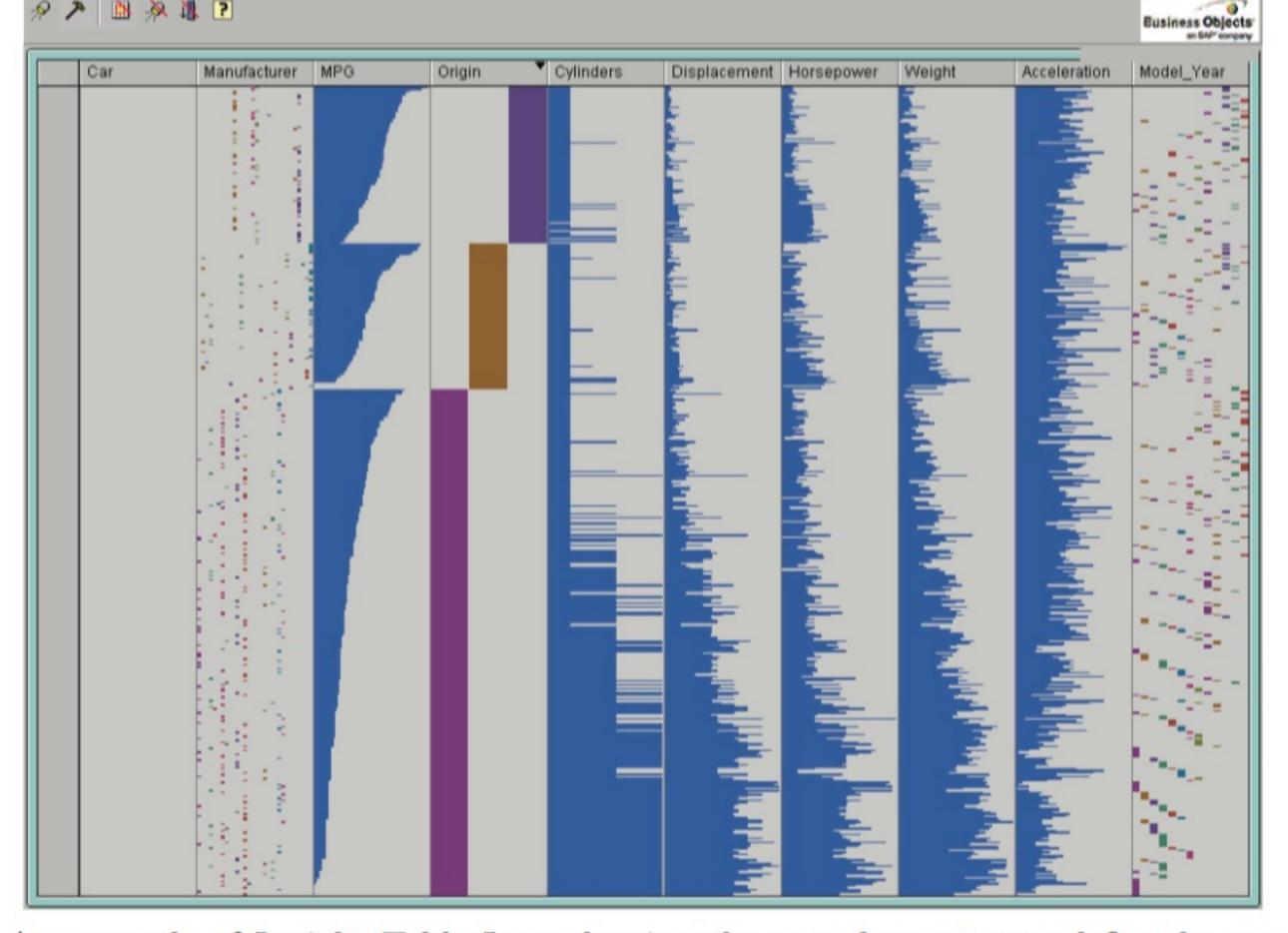
■ table lens combines all these ideas and includes a level-of-detail mechanism for providing panning and zooming capabilities to display whole table views, while still providing some detail

through local table lenses



An example of Inxight Table Lens showing the cars data set sorted first by car origin and then by MPG.





An example of Inxight Table Lens showing the cars data set sorted first by car origin and then by MPG.

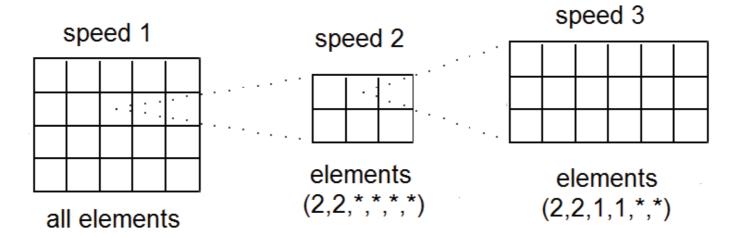
Dimensional Stacking

- Begin with data of dimension 2N + 1 (for an even number of dimensions there would be an additional implicit dimension of cardinality one).
- Select a finite cardinality/discretization for each dimension.
- Choose one of the dimensions to be the dependent variable. The rest will be considered independent
- Create ordered pairs of the independent dimensions (N pairs) and assign to each pair a unique value (speed) from 1 to N.
- The pair corresponding to speed 1 will create a virtual image whose size coincides with the cardinality of the dimensions (the first dimension in the pair is oriented horizontally, the second vertically).



Dimensional Stacking

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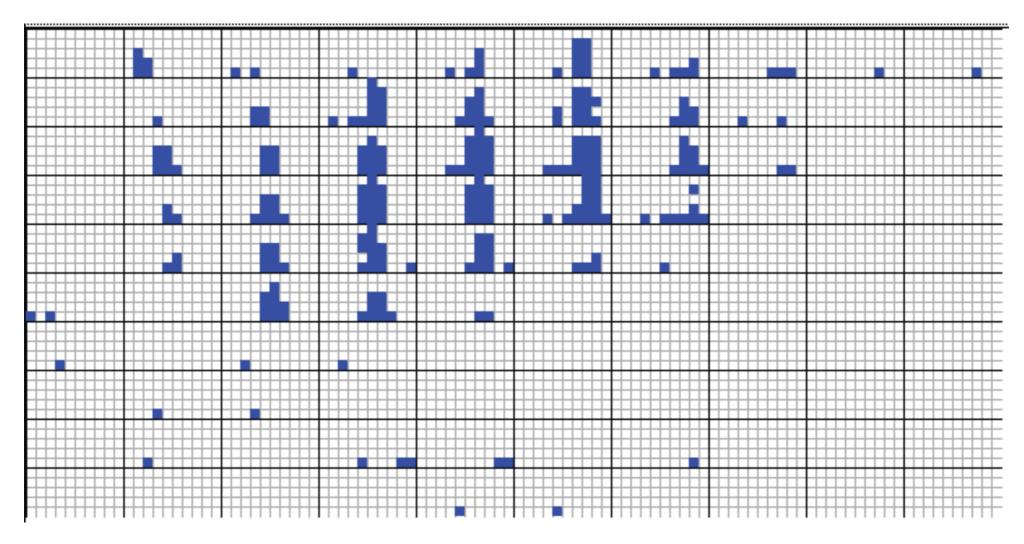


Conceptualization of dimensional stacking; collapsing six dimensions into two dimensions.

d1,..., d6 have cardinalities 4, 5, 2, 3, 3, and 6, respectively

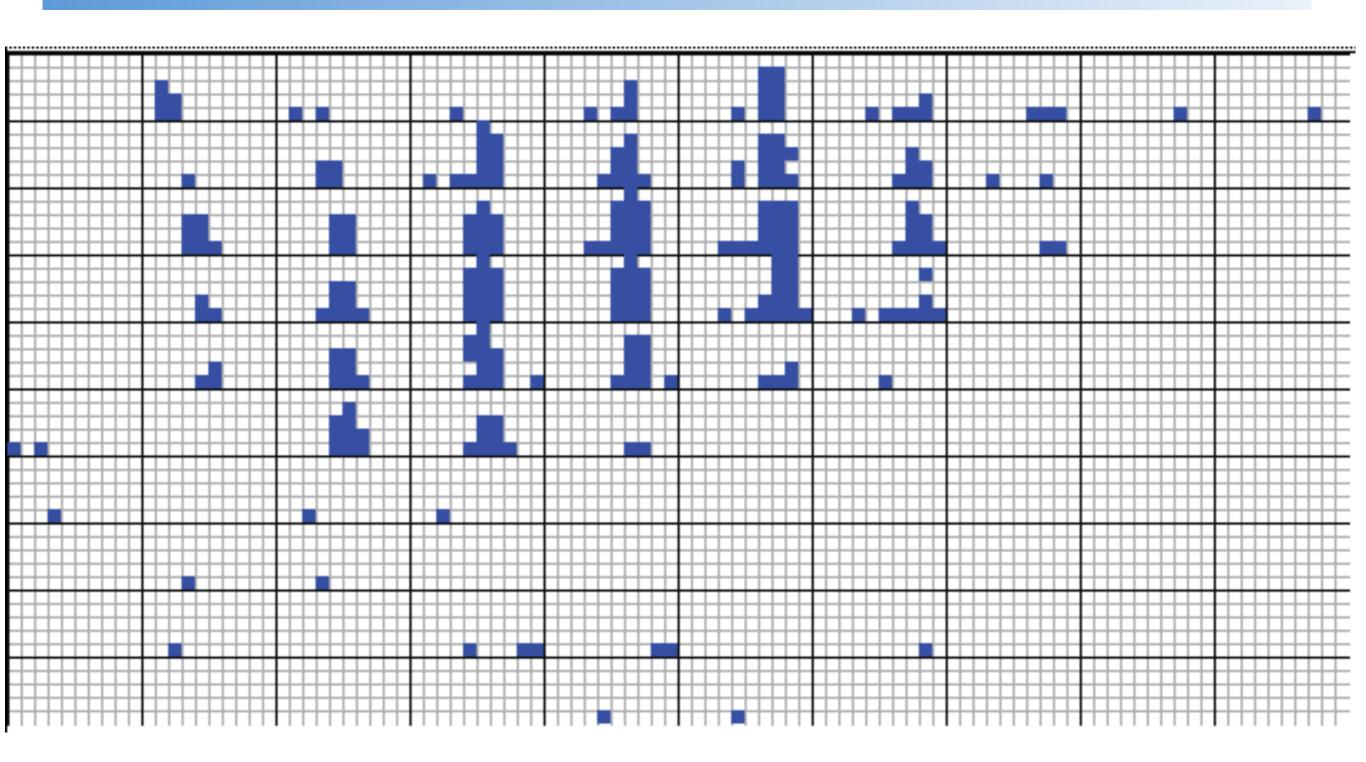


Dimensional Stacking

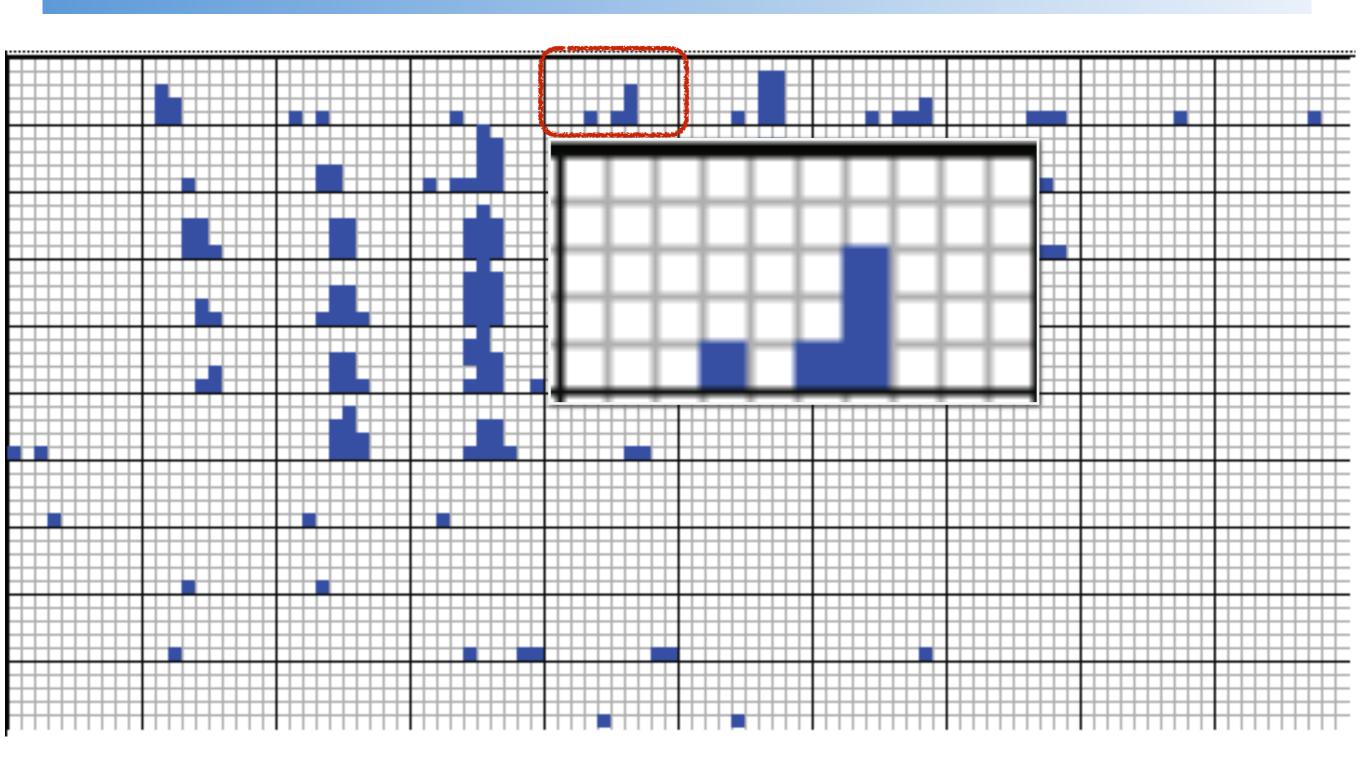


An example of 4D data visualized using dimensional stacking. The data consists of drill-hole data, with three spatial dimensions, and the ore grade as the fourth dimension.











Interactive Data Visualization

Combinations of Techniques



Multivariate Data: Combinations of Techniques

- Glyphs and Icons
- Dense Pixel Displays
- Many others



Multivariate Data: Combinations of Techniques

Glyphs and Icons

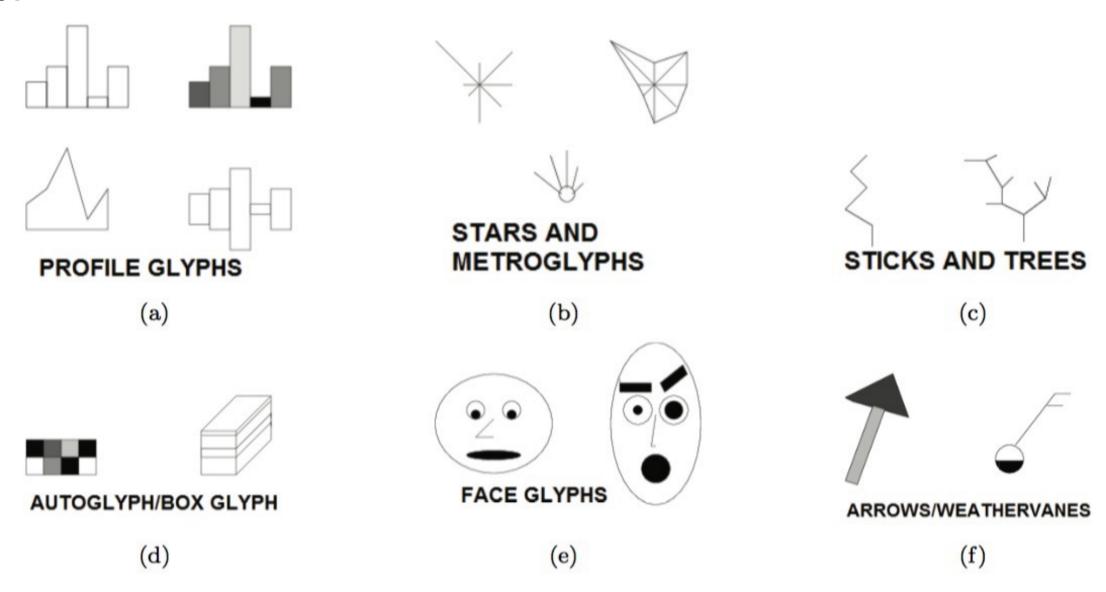


Figure 8.20. Examples of multivariate glyphs (from [445]).

Interactive Data Visualization

Further Reading and Summary



Further Reading

Recommend Readings

 Interactive Data Visualization: Foundations, Techniques, and Applications, Matthew O. Ward et all, 2015, pages 285-314.

Supplemental readings:

Visualization Analysis & Design , Tamara Munzner, Chapter 7



What you should know

Point based techniques

- Classical point base techniques have a limited dimensionality Scatter based
- Dimension reduction or selection for data viz

Line based

- Classical line based
- Radial Axis Techniques
- Parallel coordinates techniques and related stuff

Region based

- Reordering the data in graphical tables
- Combination Techniques
 - Dense
 - Glyphs

